

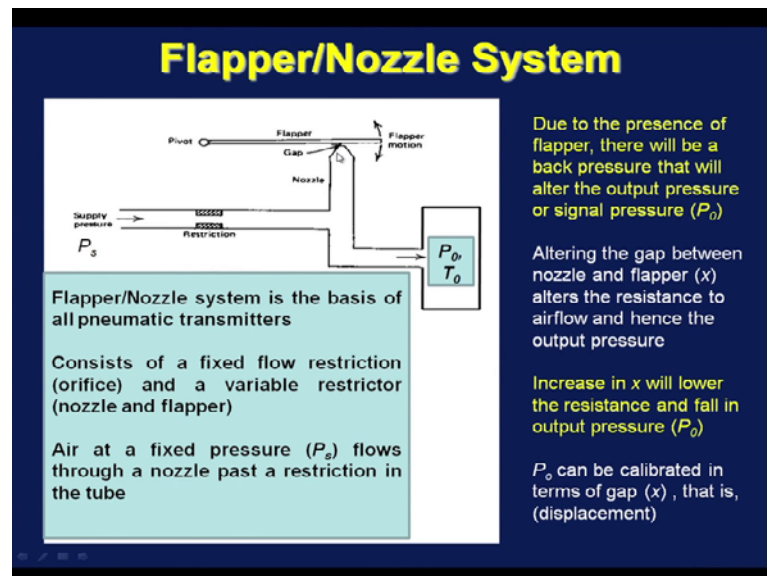
Process Control and Instrumentation
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Lecture No. # 41
Transducer Elements

In we previous lecture we started talking about, Transducer Elements. We define Transducer Elements as those devices which receives, strain or displacement as input and gives us electrical output. In general transducer elements are those devices which converts the form of the signal to a more convenient form. However, we are interested in those electro mechanical transducers, which gives us electric electrical output and receives displacement or stray in as output.

We said that will discuss one pneumatic transducer namely flapper nozzle systems and various electro mechanical transducers such as, LVDT or linear variable differential transformers strain gauge, piezoelectric transducer and capacitive type transducer. We started our discussion on flapper nozzle systems.

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So, let us continue with Flapper Nozzle systems. Flapper nozzle system is the basis of all pneumatic transmitters, it consist of a fixed flow restriction. Which is an orifice and a

variable restrictor in the form of a nozzle and flapper. Here at a fix pressure say, P s flows through the nozzle pass this restriction given by RFS.

Due, to the presents of the flapper there, will be a back pressure. That will alter the output pressure or signal pressure. Altering the gap between the nozzle and flapper, alters the resistance to yet flow and hence the output pressure. Increase in the gap between nozzle and the flapper will lower the resistance and fall in output pressure. Therefore, the output pressure or signal pressure represented here, by P0 can be calibrated in terms of the gap that exists between flapper and the nozzle which is displacement.

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Flapper/Nozzle System

Approximate static sensitivity calculation:

- Assume flow through the restrictions incompressible
- Let, orifice diameter: d_o , nozzle diameter: d_n
- Fluid density: ρ ; assume equal discharge coefficient (C_d)

Flow through orifice:

$$q_1 = C_d \left(\frac{\pi d_o^4}{4} \right) \sqrt{2\rho(P_s - P_o)}$$

Flow through nozzle:

$$q_2 = C_d (\pi d_n x_i) \sqrt{2\rho(P_o - P_{amb})}$$

Assuming flow continuity and $P_{amb} = 0$ gage:

$$q_1 = q_2$$

$$\Rightarrow \frac{P_o}{P_s} = \frac{1}{1 + \frac{16d_n^2 x_i^2}{d_o^4}}$$

The sensitivity dP_o/dx_i thus varies with x_i . It has maximum at: $x_i = 0.14 \frac{d_o^2}{d_n}$

When x_i is sufficiently large, P_o/P_s becomes almost constant. P_o/P_s is linear between 0.15 and 0.75. For $P_s = 20$ psi, this corresponds to 3-15 psi and this is the limits of industrial control pressure!

Let us, we try to find out Approximate static sensitivity for Flapper Nozzle system. Let us, assume flow through the restrictions incompressible. So, we assume flow through orifice and flow through nozzle incompressible. Let the orifice dia the represented by d_o and the nozzle dia be represented by d_n . We represent fluid density by ρ and we assume that, the discharge coefficient for orifice and the discharge coefficient for nozzle are same.

So now, flow through the orifice can be represented by this equation. So, flow through orifice q_1 is equal to discharge coefficient multiplied by πd_o^4 to the power 4 divided by 4 into square root of 2 into ρ into P_s minus P_o . Where P_s is the separate pressure, and P_o is the signal pressure. Similarly the flow through nozzle can be represented by this

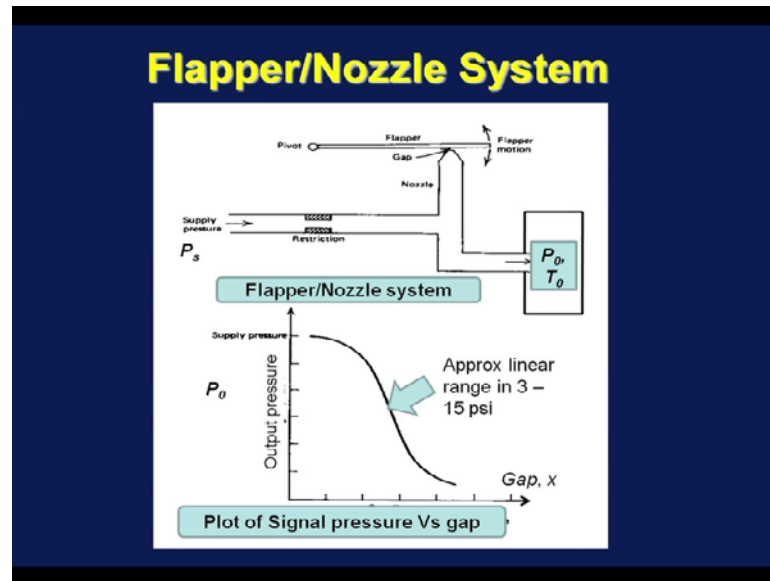
equation. Which is q_2 equal to C_d multiplied by ϕ times d_n times x_i into square root of 2 into ρ into P_0 minus P_{ambient} .

Where C_d is different coefficient d_n is the diameter of the nozzle, x_i is the gap between the nozzle and the flapper ρ is the fluid density, P_0 is the signal pressure and P_{ambient} equal to ambient pressure. Now, if we assume flow continuity the flow through orifice should be equal to flow through nozzle. If we assume P_{ambient} equal to 0 gauge pressure then, we can equate after equating q_1 equal to q_2 and after some rearrangement we can write P_0 by P_s as this equation.

So, we assume flow continuity and P_{ambient} equal to 0 gauge pressure. So, equate q_1 equal q_2 with P_{ambient} equal to 0. Then we do some rearrangement and can write P_0 by P_s equal to 1 by $1 + 16$ into d_n square into x_i square divided by d_o to the power 4. Now, P_0 is the signal pressure and P_s is the separate pressure. So, P_0 by P_s can also be taken as normalized signal pressure or output pressure.

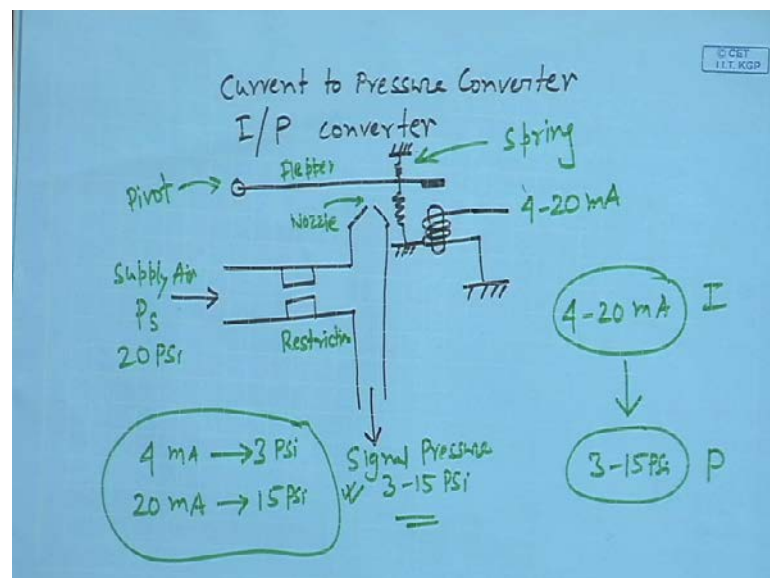
So, now clearly seen that the sensitivity which can be represented as $\frac{dP_0}{dx_i}$ of this where is we x_i . So, the displacement sensitivity of the flapper nozzle system, which can be found for this equation as $\frac{dP_0}{dx_i}$ of this part of the equation. And it can be seen that sensitivity has the maximum at x_i equal to 0.14 into d_o square by d_m . When x_i is sufficiently large P_0 by P_s becomes almost constant. So, for sufficiently large value of x_i or sufficiently large displacement P_0 by P_s which is normalized output pressure becomes almost constant or in other words tend to saturate. However, P_0 by P_s is linear between 0.15 to 0.75 for (Refer Time: 08:18) pressure P_s equal to 20 PSI this corresponds to 3 to 15 Psi, and this is the limits of in the scale control pressure.

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So, this is the plot of P_o vs x when we plot output pressure or signal pressure, but this is the gap between the nozzle and the flapper. It can be seen that for large values of gap or displacement, this part of the graph tends to saturate. So, it will become almost constant. But, it has a linear part which is this part and it is approximately linear in the range of 3 to 15 PSI. Flapper nozzle system is an important application in converting a current signal to a pressure signal.

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A Converter is converts Current signal to Pressure signals, finds important applications in process control system. We can use a flapper nozzle system to make such a device which will receive electrical signal and gives as pressure signal as output. We call them current to pressure converter or I of lig P converter. This works as for us, so we have a flow restriction here. This is supplier 20 PSI this is the nozzle and this is Flepper and this is the Pirot, this is the Signal pressure or output pressure. this is a spring. Frequently will may be interested in converting a current signal to a pressure signal. IP converter gives a linear way of translating 4 to 20 mile ampere current to 3 to 15 PSI pressure signal.

If, I send 4 to 20 mile ampere current through this coil a force will be produce that will pull down the flapper. As it pulls down the flapper the gap between the flapper and the nozzle changes. So, the signal pressure accordingly changes high current will produce high pressure. So, adjustment of the spring can be made such that, I can calibrate the system so that 4 mile ampere corresponds to 3 PSI pressure and 20 mile ampere corresponds to 15 PSI pressure.


So, I can convert a current signal between 4 to 20 mile ampere to a pressure signal between 3 to 15 PSI. So, it is working principle is very simple is essentially a flapper nozzle system. Here, we have passing a current through this coil which produces of force which pulls down the flapper.

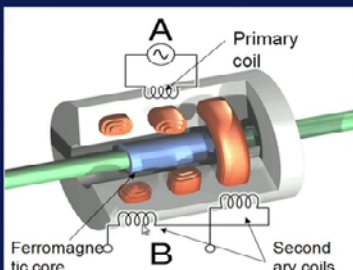
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Linear Variable Differential Transformer (LVDT)

- Electromechanical device that produces electrical output proportional to displacement of a movable core: **Displacement Transducer**
- Most commonly used variable **inductance transducer** in industry

Ferromagnetic core is physically connected to the object whose displacement is to be measured





Labels in diagram: Primary coil, Ferromagnetic core, B, Secondary coils

A soft iron core provides magnetic coupling between a single primary coil (A) and two identical secondary coils (B), connected in series opposition

When core slides through transformer, a certain portion of the coils are affected. This induces a unique voltage

As a pulls down the gap between the nozzle and the flapper changes. Which will cause a change in the signal pressure, adjustment of the spring can be met. So, that we can celebrate the instrument such that, 4 when I, am passing 4 mile ampere current through this coil the signal pressure will be 3 PSI and when I am passing 20 mile ampere current the signal pressure will be 15 PSI. So, 4 to 20 mile ampere current signal can be converted to a 3 to 15 signal PSI pressure signal.

Let us now talk about, another electrical transducer and we talk about, Linear Variable Differential Transformer commonly known as LVDT. LVDT is an electronic mechanical device that produces electrical output proportional to displacement of a movable course. So, it is a displacement transducer is most commonly used variable inductance transducing industry. So, is an inducting type transducer, or variable type in the variable inducted type transducer. LVDT looks like this. And if you look at inside of this, we see that there is a soft iron core or ferromagnetic core and there is a primary coil represented by A here and there are two identical secondary coils.

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Transducers: LVDT

The diagram illustrates the internal structure of an LVDT. On the left, a cross-section shows a central armature (iron core) that can move vertically. It is surrounded by a primary coil and two secondary coils. The 'affected zone' is indicated as the area where the core's displacement affects the magnetic flux. On the right, a cross-sectional view shows the core assembly with a magnetic shield, ferrite core, and the primary and secondary coils. Below this is a circuit diagram showing the primary coil connected to an AC source V_i and the two secondary coils connected in series to provide an output voltage V_o .

Core: Nickel Iron Alloy, Ferrite

The whole sensor is enclosed and shielded so that no field extends outside it and hence cannot be influenced by outside fields

The sensitivity of typical LVDTs is in the range of 1 to 5 v/v/cm
 Displacement: ± 0.002 cm to several cm

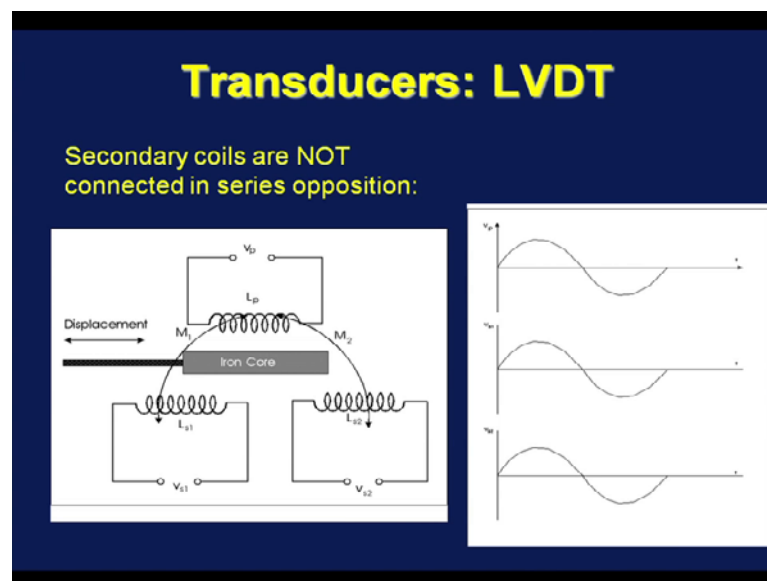
Primary coil is excited by a sinusoidal voltage of amplitude 1 V to 15 V and frequency 50 Hz to 20 kHz

So, this soft iron core provides magnetic coupling between a single primary coil and two identical secondary coils. This two identical secondary coils are connected in serious opposition. So, when the core slides through the transformer shorten portion of the coil affected and this induces a unique voltage. This core is physically connected to the object, whose displacement is to be measured. So, is the object move the core also slides

for the transformer. So, certain portion of the secondary coils are effected which will induce a unique voltage. And this voltage will be taken as a direct measure of the displacement.

So, this is the primary coil and these are two identical secondary coils. Which are connected in serious opposition. That this two secondary coils are connected it is serious opposition is clear from this circuit diagram. Usually the core is measured of alloy nickel iron alloy ferrite, primary coil is excited by a sinusoidal voltage of amplitude 1 volt to 15 volts and frequency 50 hurts to 20 hertz. The whole sensor is enclosed and shielded. So, that no field extends outside it and hence can all influence by outside fields. Look at this two circuit diagrams, in one case the core is centrally located. When it is centrally located equal parts of these two secondary coils are affected. When the core is pushed up, only this part of the only this secondary coil is affected, but the other secondary coil is not.

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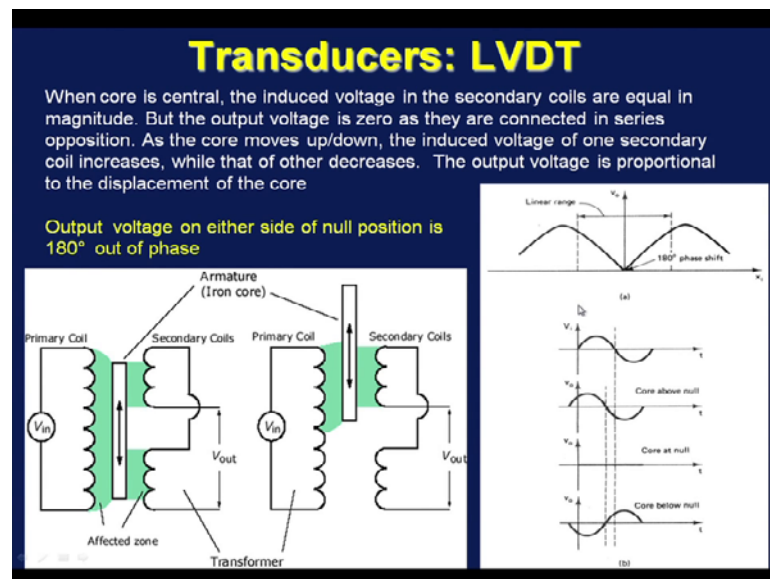


The core will move up or come down as the object moves as the object changes position. Because, this core is physically connected to the object. So, different amount of voltage will be induced in this two coils and thus the output voltage will change as the position of the core changes. LVDT is a highly sensitive instrument for highly sensitive transducer, the sensitivity of typical LVDT is in the range of 1 to 5 volt per centimeter.

And it can measure a displacement as low as plus minus 0.002 centimeter and can measure up to several centimeters.

Let us now, consider the circuit diagram of the LVDT again. So, this is the primary coil and these are two secondary coils. This is the iron core, which is connected physically to the object whose displacement I want to measure. So, this core moves like this or this. For the time being let us, assume that the two secondary coils are not connected in series opposition. Since, this two secondary coils are identical in all respect equal amount of voltage will be induced in both the coils. So, if I excite the primary coil by this signal I may get these signals for the secondary coils. Now if, there connected in series opposition since, the magnitude are equal and since there connected in series opposition the output voltage will be 0.

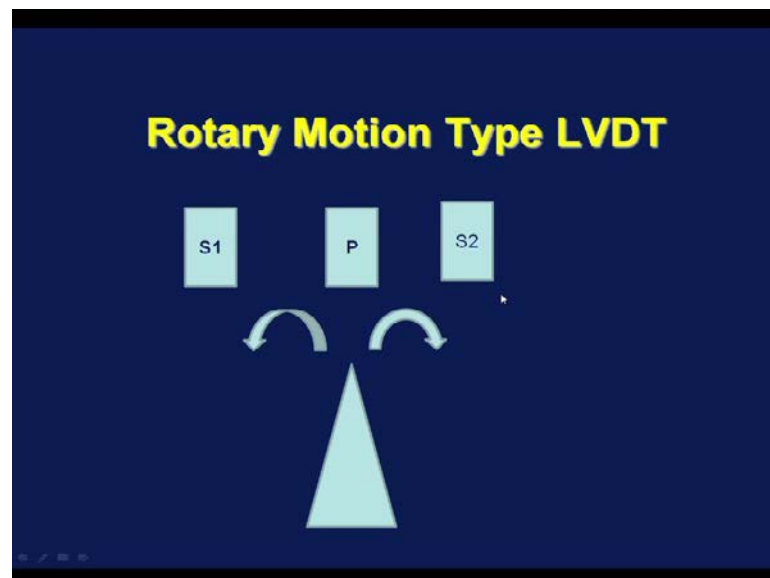
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As can be seen from here, when the core is central the induced, voltage in the secondary coils are equal in magnitude. But, the output voltage is 0 as there connected in series opposition. As the core moves up or down the induce voltage of one secondary coil increases that of other decreases. The output voltage is promotional to the displacement of the core. If you look at this, plots when the core is centrally located output voltage is 0. Because equal amount of voltages are induced in both the secondary coils. And since, secondary coils are connected in series opposition the output voltage is 0.

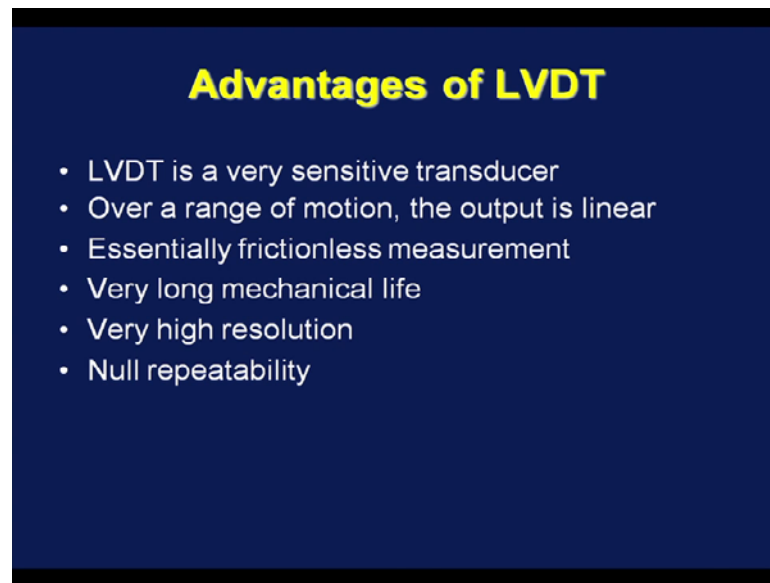
So, if I excite the primary coil by say this signal, I will get 0 voltages output. When the core is centrally located or we say core at null. If the core moves up or comes down, I will have non0 voltages output. Because as the core moves up or comes down the induce voltage of one secondary coil increases while that of other decreases. So, when the core is above null position which shown by this figure. I will get output signal like this, while core is below null. So, when this core is push down I will get output voltage as this. Output voltage on either side of null position is 180 degree out of phase, as you can see. When we plot the output voltage verses the displacement of the core. So, as if I start from here, I push the core down it takes centrally located position I push it further it goes below null. So, the output voltage will undergo 180 degree phase shift. If you look at this figure and this three figures we understand that the output voltage will undergo 180 degree phase shift.

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We can also have Rotary Motion type LVDT which is schematically represented by this. We have a primary coil we have two secondary coils, and this is connected to the object whose rotary motion I have to measure. So, as it rotates like this different portion of this two secondary coils are connected. So, output voltage changes accordingly.

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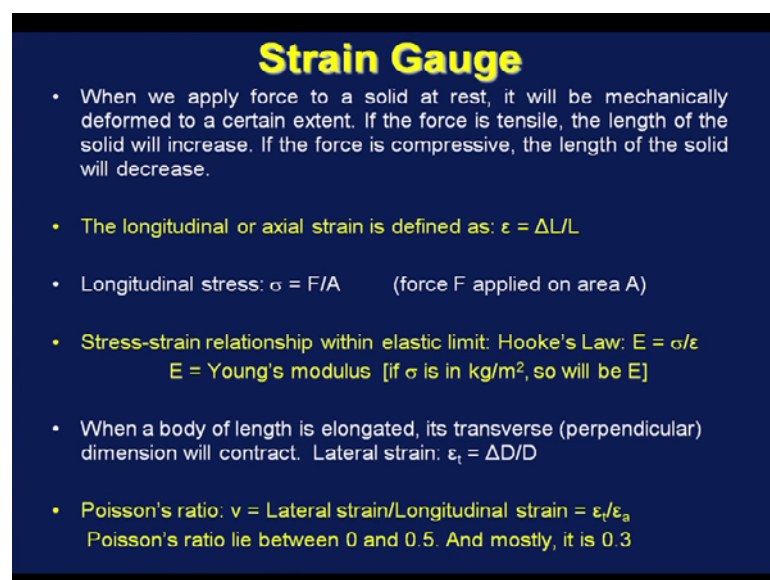


Advantages of LVDT

- LVDT is a very sensitive transducer
- Over a range of motion, the output is linear
- Essentially frictionless measurement
- Very long mechanical life
- Very high resolution
- Null repeatability

There are several advantages associated with LVDT. LVDT is a very sensitive transducer its sensitivity is the range of 1 to 5 volt per centimeter. Over a range of motion the output is linear, you can see here over a range of motion the output is linear. So, we have a linear range it offers essentially frictionless measurement. It has very long mechanical life, it has very high resolution, it also has good null repeatability.

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Strain Gauge

- When we apply force to a solid at rest, it will be mechanically deformed to a certain extent. If the force is tensile, the length of the solid will increase. If the force is compressive, the length of the solid will decrease.
- The longitudinal or axial strain is defined as: $\epsilon = \Delta L/L$
- Longitudinal stress: $\sigma = F/A$ (force F applied on area A)
- Stress-strain relationship within elastic limit: Hooke's Law: $E = \sigma/\epsilon$
 $E = \text{Young's modulus}$ [if σ is in kg/m^2 , so will be E]
- When a body of length is elongated, its transverse (perpendicular) dimension will contract. Lateral strain: $\epsilon_t = \Delta D/D$
- Poisson's ratio: $\nu = \text{Lateral strain/Longitudinal strain} = \epsilon_t/\epsilon_a$
Poisson's ratio lie between 0 and 0.5. And mostly, it is 0.3

Let us now talk about, Strain Gauge which is another electrical transducer which receives strain as input and gives us electrical signal as output. Let us, start with some

basic definitions that you are already familiar with. When we apply force to a solid tray it will mechanically deformed to a certain extend. If the force is tensile nature, the length of the solid will increase if the force is contrastive. The length of the solid will increase. The longitudinal strain or axial strain is defined as change in length divided by original length. So, we represent axial strain or the longitudinal strain as ΔL divided by L . Longitudinal strains is defined as force divided by areas. So, forced F applied on area A . Force divided by area is longitudinal stress the stress-strain relationship within elastic limit is given by Hooks law with says, youngs modulus E equal to stress divided by strain. Strain is unit place because it is ratio of two lines.

So, if stress is in kg per meter square youngs modulus also be in kg per meter square. When a body of length is longitudinal its transverse or perpendicular dimension will contract, we call this lateral strain. Which can be represented as ΔD divided by D when ΔD is the change in diameter and D is the original diameter. Poissons ratio says, poissons ratio is the ratio of lateral strain to longitudinal strain. So, poisson ratio new is F silent t by F silent A is the ratio of transfer strain or lateral strain to longitudinal strain. We write new equal to minus F silent t by F silent a where F silent t is the transfer strain and F silent A is axial strain. Poisson ratio lies between 0 and 0.5 and mostly it is 0.3.

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Strain Gauge

- Strain measurement is essentially measurement of very small, about 1 micrometer, displacement
- **Methods:**
 - **Mechanical:** Use levers and gears to measure ΔL after magnification [early days: extensometer uses many levers to magnify strain so that it becomes readable]
 - **Electrical:** Change in resistance or inductance or capacitance
 - **Optical:** Use interference, diffraction, and scattering of light waves
- **Most commonly used method: Electrical: change in resistance: Resistive Strain Gauges**

Strain measurement is essentially measurement of very small displacement by very small we main as small as 1 micro meter. There are various methods for measurement of strain there are, mechanical methods, electrical methods, as well as optical methods. Mechanical methods use levers and gears to measure change in length after magnification. For example, early days we use extensometer to magnify strain extensometer uses many levers to magnify strain so, that it becomes readable. Electrical methods uses the properties such as, change in assistance or inductance or capacitance to measure strain. Optical methods use uses interference, deflection and scattering of levers. The most commonly use method is electrical method that uses change in resistance of a resister when it is strain. Using this principle we have Resistive Strain Gauges transducer.

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Strain Gauge Theory

For a wire of cross-sectional area A , resistivity ρ , and length L the resistance is given by:

$$R = \frac{\rho L}{A}$$

This equation holds good for many common metals and nonmetals at room temperature when subjected to direct or low frequency current

When the wire is stretched, the cross-sectional area A is reduced, which causes the total wire resistance to increase. In addition, since the lattice structure is altered by the strain, the resistivity of the material may also change, and this, in general, causes the resistance to increase further.

To provide a means of comparing performance of various gauges, the gauge factor, or strain sensitivity, of a gauge is defined as:

$$G = \frac{\Delta R / R}{\Delta L / L} = \frac{\Delta R / R}{\epsilon_a}$$

$\frac{\Delta R}{R}$ = fractional change in resistance
 $\frac{\Delta L}{L}$ = fractional change in length

Higher gauge factors are generally more desirable -- the higher the gauge factor the higher the resolution of the strain gauge

For a wire of crosssectional area A resistivity ρ and length L the resistance will given by the familiar equation $R = \rho L / A$. This equations holds good for many common metals and non metals at room temperature when subjected to direct or low frequency current. When the wire is stretched the cross sectional area is reduced, which causes the total wire is resistance to increase. So, when the wire is stretched, we increase the length reduce the area and the resistance does increases. In addition since, the latistructure is altered by the strain the resistivity of the material may also change and this in general causes the resistance to increase further.

To provide a means of comparing performance of various gauges. Let us define something called gauge factor or strain sensitivity. The gauge factor or strain sensitivity can be defined as, $\Delta R / R$ over $\Delta L / L$. So, this is the fractional change in resistance which is $\Delta R / R$ by axial strain or longitudinal strain, which is fractional change in length $\Delta L / L$. So, we define gauge factor as fractional change in resistance divided by fractional change in length. In other words fractional change in resistance divided by axial or longitudinal strain. Higher gauge factors are generally more desirable the higher the gauge factor the higher the resolution of the strain gauge.

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Strain Gauge Theory

$$R = \frac{\rho L}{A} \Rightarrow R = R(\rho, L, A)$$

$$\Delta R = \left(\frac{\partial R}{\partial L}\right) \Delta L + \left(\frac{\partial R}{\partial A}\right) \Delta A + \left(\frac{\partial R}{\partial \rho}\right) \Delta \rho$$

$$\Rightarrow \Delta R = \left(\frac{\rho}{A}\right) \Delta L - \left(\frac{\rho L}{A^2}\right) \Delta A + \left(\frac{L}{A}\right) \Delta \rho$$

Dividing throughout by R

$$\frac{\Delta R}{R} = \frac{\Delta L}{L} - \frac{\Delta A}{A} + \frac{\Delta \rho}{\rho}$$

1st term: Length change

2nd term: Area change

3rd term: Resistivity change

$$\text{If } A = C D^2, \text{ then } \Delta A = 2 C D \Delta D$$

$$\frac{\Delta A}{A} = \frac{2 C D \Delta D}{C D^2} = 2 \frac{\Delta D}{D} = 2 \epsilon_t$$

$$\frac{\Delta R}{R} = \epsilon_a - 2\epsilon_t + \frac{\Delta \rho}{\rho}$$

So, you have a functional relationship between resistance and resistivity length and area. So, we can find out change in resistance ΔR as $\Delta R / R$, $\Delta L / L$ times $\Delta L / L$, plus $\Delta R / R$ $\Delta A / A$ times, $\Delta A / A$ plus $\Delta R / R$ $\Delta \rho / \rho$ times $\Delta \rho / \rho$, $\Delta \rho / \rho$. Now this partial derivatives can be found out from the equation $R = \rho L / A$. So, if I find out this partial derivatives we can write $\Delta R / R$ as ρ / A into $\Delta L / L$ minus $\rho L / A^2$ into $\Delta A / A$ plus L / A into $\Delta \rho / \rho$.

If I now, divide this equation throughout by resistance R. We will have $\Delta R / R$ which is fractional change in resistance as, $\Delta L / L$ minus, $\Delta A / A$ plus, $\Delta \rho / \rho$ by ρ . So, the first term $\Delta L / L$ is fractional change length. The second term this fractional change in area. And the third term is fractional change in resistivity. If we assume the relationship of area with diameter $A = C D^2$ into discover

then, you can write delta A as 2 into C into D delta D. So, then it becomes possible for us to find out delta A by A. And we will see by delta A by delta A is to C D delta D divided by C D square A is C D square. Which is 2 delta D by D and delta D by D is nothing, but lateral strain or transfer strain epsilon t. So, delta A by A becomes to epsilon t. So, the fractional change in desistance delta R by R can be written as epsilon a minus 2 epsilon t plus delta rho by rho. So, this is axial strain minus twice lateral strain plus delta rho by rho.

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Strain Gauge Theory

$$\frac{\Delta R}{R} = \varepsilon_a - 2\varepsilon_t + \frac{\Delta\rho}{\rho}$$

Therefore, Gauge Factor, $F = \frac{\Delta R / R}{\Delta L / L}$

$$= \frac{\varepsilon_a - 2\varepsilon_t + \frac{\Delta\rho}{\rho}}{\varepsilon_a}$$

$$= 1 + 2\nu + \frac{\Delta\rho / \rho}{\varepsilon_a}$$

$$= 1 + 2\nu + \psi E$$

$\frac{\varepsilon_t}{\varepsilon_a} = -\nu = \text{Poisson's ratio}$

$\frac{\Delta\rho / \rho}{\varepsilon_a} = \frac{\Delta\rho / \rho}{\Delta L / L} = \psi E$

Constant for a material, directly proportional to Modulus of Elasticity, E. ψ = Bridgeman coefficient

Material	Composition	Gauge Factor
Advance	Cu 55%, Ni 45%	2 - 2.2
Nichrome	Ni 80%, Cr 20%	2.2 - 2.5
Pure Platinum	Pt 100	~4.8
Semiconductor type		100 - 200 ^{1b}

So, the gauge factor which is delta R by R divided by delta L by L. Can now be found out as epsilon a minus epsilon t plus delta rho by rho divided by axial strain. Which will become 1 plus 2 nu where nu is the poisson ratio, epsilon t epsilon a equal to minus nu plus delta rho by rho epsilon a which axial strain. Now, this term which is delta rho by rho divided by epsilon a, which is delta rho by rho divided by delta L by L is constant for a material and this directly propositional to modulus of elasticity. And the propositional laity constant is known as Bridgeman coefficient.

So, the gauge factor is finally defined as, F equal to 1 plus 2 nu plus epsilon E. I repeat the gauge factor is finally, found out to be as F equal to 1 plus 2 nu plus shy which is Bridgeman coefficient times E which is modulus of elasticity. If I, look at gauge factor of some of the materials that are used for strain gauge. We see that advance which as compassion as copper 55 percent and nickel 45 percent as the gauge factor increase 2.2.

Similarly nichrome which is an alloy of nickel and chromium with nickel 80 percent and chromium 20 percent as gauge factor of 2.2 to 2.5. Pure platinum has higher gauge factor above 4.8. Semiconductor materials are also used for construction of strain gauges. And semiconductor type strain gauges have extremely high gauge factor of the order of 100 to 200.

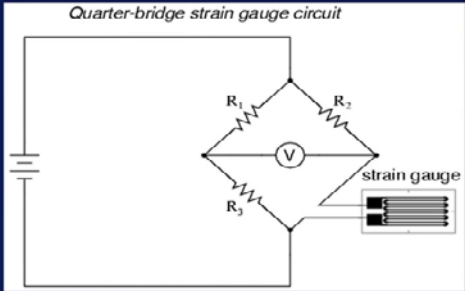
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Strain Gauge

A strain gauge is a passive type transducer whose electrical resistance changes when it is stretched or compressed

The wire filament is attached to a structure under strain and the resistance in the strained wire is measured by Wheatstone Bridge principle

Quarter-bridge strain gauge circuit



- > Un-bonded Type
- > Bonded Type
- > Semiconductor Type

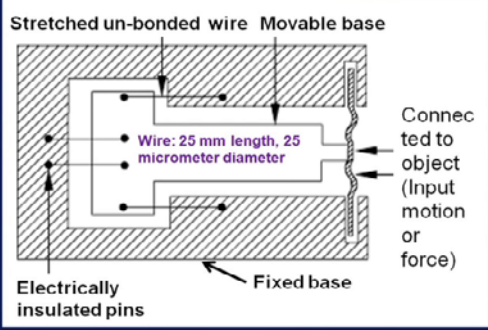
So, How do I measure strain with help of a strain gauge? Strain gauge is usually in the form of a wire filament. It can have various types like bonded type, unbonded type, or semiconductor type. Let us consider this as strain gauge so, this consists of a resistance of wire. Let us say the wire filament is attached to a structure which is under strain. And the resistance in the strain wire is measured by the Wheatstone bridge principle.

So, we take the wire filament which is the strain gauge, attach to the structure whose strain I want to measure. Before the strain gauge is under any strain, we balance the bridge. Now, the strain gauge is under strain so, there will be a change in resistance and there will be an unbalanced current in the Wheatstone bridge. And the unbalanced current will be taken as a direct measure of the strain.

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Strain Gauge Operation

Un-bonded Strain Gauge:



Stretched un-bonded wire Movable base

Wire: 25 mm length, 25 micrometer diameter

Connected to object (Input motion or force)

Electrically insulated pins Fixed base

- > A set of preloaded resistance wire is stretched between two frames: one movable and the other fixed
- > A small motion of the movable base increases tension in two wires while decreasing it in two others.
- > Change in resistance cause Wheatstone bridge unbalance
- > The output voltage is proportional to input displacement

A very small motion (say 50 μm) and very small forces can be measured

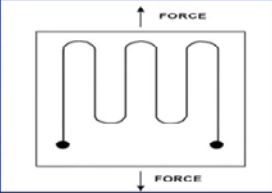
This is the schematic representation of unbounded strain gauge. It consists of a set of preloaded resistance wire, which is stretched between two frames. One is movable and the other is fixed. So, a set of preloaded resistance where is starched between two frames. One is movable and the other fixed. Typically the wire we use is a 25 millimeter length, and 25 micrometer diameter.

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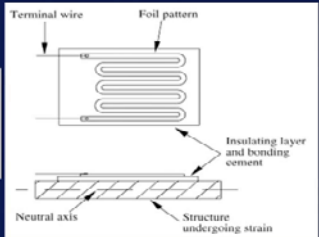
Strain Gauge Operation

Bonded Strain Gauge:

Wire-type



Foil type



Bonded strain gauges are directly bonded to the surface of the specimen being tested, with a thin layer of adhesive cement. They use paper or bakelite as backing material. Useful for measurement of strain, force, torque, pressure, vibrations, etc. They are very sensitive and can measure strains as low as 10^{-7} .

Bonded strain gauges are also made of semiconductor material. Usually, silicon doped with boron (p-type) or silicon doped with arsenic (n-type) are used. High gauge factor, small gauge length are advantages. High temperature sensitivity and nonlinearity are disadvantages.

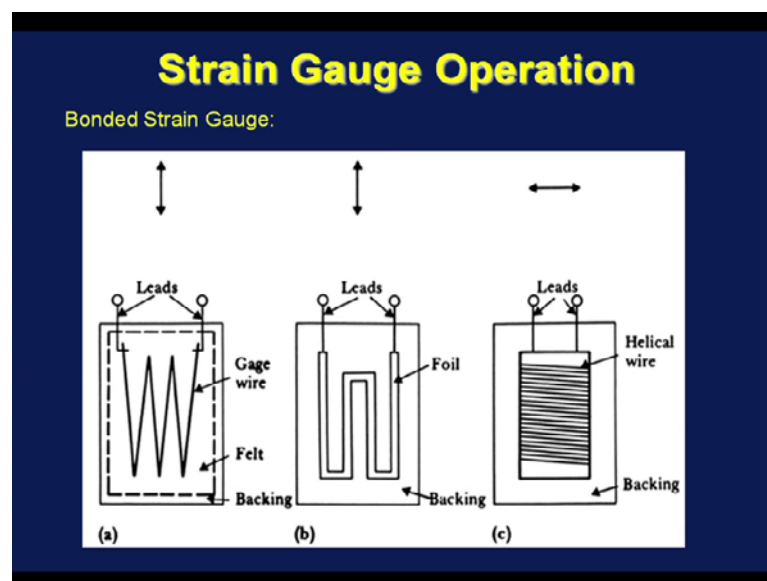
The movable base is connected to the object. So, this receives the input motion or force. So, this unbounded wires will now, be stretched. That will cause a change in resistance

of the wires. And change in resistance will cause Wheatstone bridge unbalance. The output voltage is proportional to input displacement. A very small motion up to 50 micro meter and very small force can be measured.

These are schematics of bounded strain gauge, it can be of wire type or it can be of coil type. Bounded strain gauge is a directly bounded to the surface of the specimen being tested, with a clean layer of adhesive cement. They use paper or bakelite as backing material. So, they use paper or bakelite as backing material, it should be backing. The bounded strain gauges are useful for measurement of strain, force, torque, pressure, vibrations etcetera.

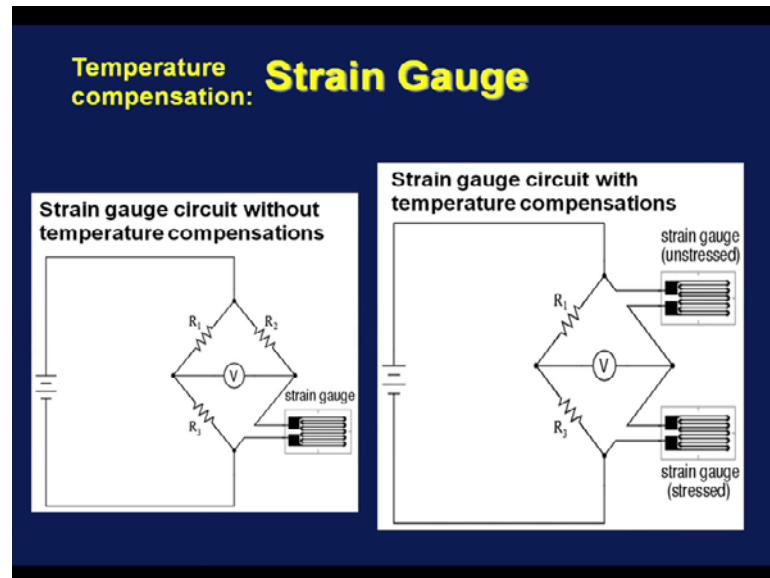
They are very sensitive and can measure strains as low as 10^{-7} . So, this is the structure this undergoing strain. And this is the foil which is bounded on the surface of the structure undergoing strain, with adhesive cement. These are terminal wires which is connect to the 1 arm of the Wheatstone bridge. Bounded strain gauges are also made of semiconductor material. Usually silicon doped with boron gives us P type semiconductor strain gauge, and silicon doped with arsenic gives as n type semiconductor strain gauge. High gauge factor and small gauge length are its advantage. However, How temperature sensitivity and non-linearity are disadvantages?

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This figure again schematically represents various bounded strain gauges. So, these are the gauge wires, this is backing and this is cemented with this. And this leads are connected to the one arm of the Wheatstone bridge.

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Now, the resistance of a wire can also change with changing temperature. So, there is any change in the ambient temperature that will, also try to change the resistance of the strain gauge. So, is not only the strain that will try to change the resistance of the strain gauge. But, also the temperature will also change try to change the resistance of the strain gauge. So, we need to compensate for the changes in temperature. So, this is the circuit diagram we previously discussed. Which does not have any temperature constants compensation. So, one arm of the Wheatstone bridge has the strain gauge. To have a temperature compensation we take two identical strain gauges connected to, 2 arms of the Wheatstone bridge. One strain gauge is stressed so, this is attach to the spaceman whose strain we are going to measure and other one is not strain. So, this is unstressed.

Now, the effect of temperature will be same in both the strain gauges. So, changes in resistance of the strain gauges by temperature alone will be same in both the same gauges. But, the strain gauge that is strained or stressed will have additional change in resistance, which comes from the strain. So, the changes in resistance due to temperature change will be nullified by the change in resistance of this strain gauge cause by temperature which is not strain. So, this way by putting two identical strain gauge. But,

using only one to connect to the spaceman, whose strain I want to measure I can compensate for the changes in temperature.

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Application of Strain gauge

- Strain gages are used to measure displacement, force, load, pressure, torque or weight
- Strain gages may be bonded to cantilever springs to measure the force of bending
- Strain-gage elements also are used in the design of pressure transmitters using a bellows type or diaphragm type pressure sensor
- Semiconductor type strain gauge – high gauge factor

Strain gauge is the used to measure displacement, force, load, pressure, torque, weight. Strain gauges may be bonded to cantilever spring to measure the force of bending. Strain gauge elements are also used in the design of pressure transmitters using a bellows type or diaphragm type pressure sensor. Semiconductor type, strain gauge as very high gauge factor.

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Capacitive Transducers

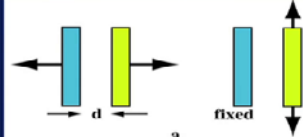


Area=A


$$C = \frac{1}{3.6\pi} \epsilon \frac{A}{d}$$

C: capacitance, pF
 E: dielectric constant, 1 for air (relative permittivity)
 A: area of plates, cm²
 d: distance between plates, cm

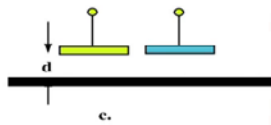
We change area, distance, or dielectric:



a.



b.



c.

Capacitance C between two plates may change due to change of gap or area

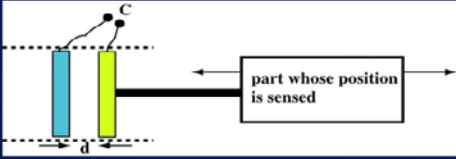
Let us now, briefly talk about capacitive type transducers. We are familiar with this equation for capacitance. Which relates capacitance, to area of plates distance between two plates and the dielectric constant or relative permittivity. So, if we take two plates which is separated by distance d and has area A . The capacitance in picofarads will be $1.36 \times 10^{-12} \frac{\epsilon_r A}{d}$, which is directly proportional to A by d . Where A is area of plates in centimeter square d distance between plates in centimeter.

Now, we can make capacitance transducer by changing area or distance or dielectric medium. Any change in area distance all dielectric, will cause change in the capacitance. Next for example, if this two plates moves in this directions the gap within this two changes. So, there will be changing capacitance. If one plate is fixed another changes the area between the two plates are changing. So, there will be capacitance change. So, I can have variable area Capacitance Transducer or variable distance capacitor transducer.

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Capacitive Transducers

- One plate is fixed while the other is moved by the moving object.
- The position of the moving object causes a change in the capacitance, C
- Capacitance is inversely proportional to the motion and as long as the distances sensed are small, the output is linear.

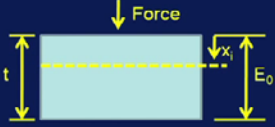


Suppose one plate is fixed when the other is moved by the moving object. So, the position of the moving object causes the change in the capacitance C . Capacitance is inversely proportional to the motion as long as the distance is sensed or small.

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Piezoelectric Transducers

- **Materials**
 - **Natural occurring highly polar crystal**
 - Quartz, Rochelle salt, ammonium dihydrogen phosphate
 - **Synthesized**
 - Barium titanate, Ceramic
 - Lead zirconate titanate
- When a crystalline material like quartz is distorted an electric charge is produced
- Application of a force P causes deformation x_i , producing a charge Q , where $Q = Kx_i$ where K = charge sensitivity constant
- Crystal behaves like a capacitor, carrying a charge across it. Voltage across crystal E_0 is:
$$E_0 = \frac{Q}{C} = \frac{Kx_i}{C} = kC$$



Finally let us briefly talk about, Piezoelectric Transducer. When a crystalline material like quartz is distorted an electric charge is produced. Application of a force P causes deformation x_i producing a charge Q and we can write Q equal to K into x_i . Where K is the charge sensitivity constant. The crystal now, behaves like a capacitor carrying across it. So, voltage across crystal E_0 will be Q by C and Q is $K x_i$. So, we can write E_0 equal to $K x_i$ by C which can be K by C can be consider is another constant K . So, E_0 equal to K into C .

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Piezoelectric Sensors

Advantages:

- Low cost, small size
- High sensitivity and High mechanical stiffness
- Broad frequency range
- Good linearity and repeatability

Disadvantages:

- High Impedance
- Low Power
- Drift with temperature and pressure

So, the voltage that is produced is proportional to the charge. Natural occurring highly polar crystals like quartz, Rochelle, salt, ammonium dehydrogenate phosphate. or synthesized material like barium titanate. Ceramic. lead zirconate titanate. are used for piezoelectric transducers.

Piezoelectric Sensors are advantages like it is have low cost small size high sensitivity and high mechanical stiffness, broad frequency range, good linearity and repeatability. However, it has some disadvantages as well it has high impedance low power and drift with temperature and pressure.