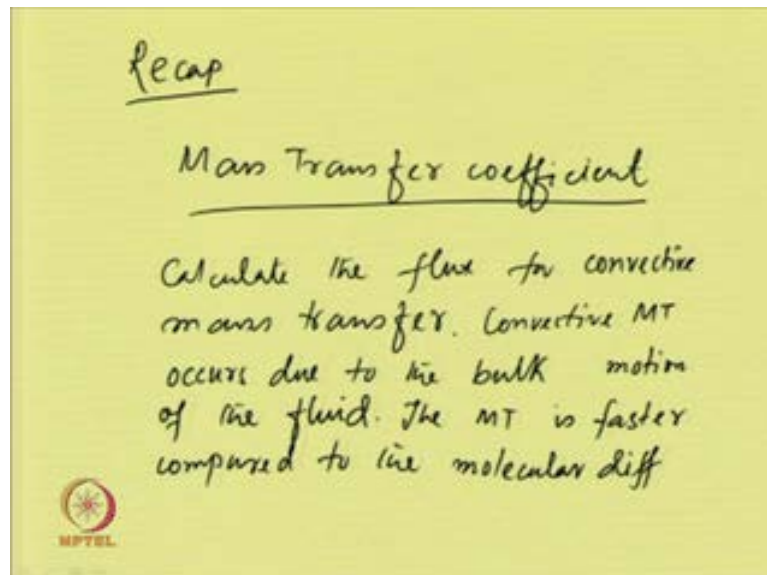


Mass Transfer Operations-I
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Module - 2
Mass Transfer Coefficients
Lecture - 1
Concept of Mass Transfer Coefficient

Welcome to the first lecture of module two which is on mass transfer coefficient. So, before going to this lecture, let us have a small recap of the module one, what we have covered.

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So, in module one, we have considered the diffusion mass transfer. The diffusion occurs mainly due to the molecular diffusions, and we know how to calculate the flux. And we have also discussed the difference between the molecular transfer or molecular diffusion, and the convective mass transfer or convective diffusion. In case of convective diffusions, we have seen that the rate of mass transfer is much faster compared to the molecular diffusion, and reason for higher rate of mass transfer in case of convective mass transfer is due to the bulk motion of the fluid. So, to account how to calculate the flux in case of convective mass transfer, we need to know a simpler method, which is the mass transfer coefficient method; mass transfer coefficient. So, by this way, we can simplify or we can very easily calculate the flux for convective mass transfer.


Convective mass transfer occurs due to the bulk motion of the fluid, and the mass transfer is faster compared to the molecular diffusion.

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Module 2: Lecture 1

Concept of Mass Transfer Coefficients

Rate of mass Transfer \propto conc driving force
Rate of mass Transfer \propto area of contact betⁿ the phases
 W_A = rate of mass transfer in kmol/s
 $W_A \propto a \Delta C \Rightarrow W_A = k_c a \Delta C$
Mass Transfer coefficient, $k_c = \frac{N_A}{\Delta C} = \frac{\text{molar flux}}{\text{conc. driving force}}$



So what are the concepts of mass transfer coefficients. The mass transfer coefficient can be defined, the rate of mass transfer, we know rate of mass transfer is proportional to the driving force, concentration driving force. And also the rate of mass transfer is also proportional to the area of contact between the phases. So, if we consider W_A is the rate of mass transfer in K mole per second, then we can write W_A is proportional to A into concentration gradient, ΔC . So, from this we can write W_A is equal to k_c into A into concentration gradient. This k_c is proportionality constant of this equation, and is known as the mass transfer coefficient. So, mass transfer coefficient k_c is equal to flux divided by concentration gradient, which is equal to molar flux divided by concentration driving force. In this case, there are other mass transfer coefficients; one is called local mass transfer coefficient. The local mass transfer coefficient we can define by the local flux, divided by the local driving force.

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Module 2: Lecture 1


Concept of Mass Transfer Coefficients

Local Mass Transfer coefficient = $\frac{\text{Local flux}}{\text{Local driving force}}$

Average Mass Transfer coefficient = $\frac{\text{Average flux}}{\text{Average driving force}}$

$N_A \propto a \Delta C \Rightarrow N_A = k_c a \Delta C$

Mass Transfer coefficient, $k_c = \frac{N_A}{\Delta C} = \frac{\text{molar flux}}{\text{conc. driving force}}$



Local mass transfer coefficient, we can write local flux divided by local driving force. And the average mass transfer coefficient, can be defined as the ratio of the average flux and the average driving force is equal to average flux, average flux over a surface, and the average driving force.

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Types of Mass Transfer Coefficients

conc. driving force
partial pr. driving force
molar fraction

(i) MT in the gas or liquid phase
(ii) choice of driving force
(iii) Diffusion of A through non-diffusing B or
Equimolar counterdiffusion of A & B

δ

Flux = mass transfer coefficient \times driving force



So, there are many of mass transfer coefficient, depending on the situations. In case of mass transfer, we can use concentration as the driving force. We can use the partial pressure, if it is in the gas phase, partial pressure as the driving force. And we can also

use the molar fraction, molar fraction as the driving force and so on, but in case of heat transfer, only the temperature is the driving force. So, depending on the situation, we can define the mass transfer coefficient. So, on the following basis, mass transfer is in the gas or liquid phase. So, if it is gas phase, there is gas phase mass transfer coefficient. If it is in the liquid phase, it is liquid phase mass transfer coefficient, and also the choice of driving force. And third one is whether diffusion occurs, diffusion of a particular component, through non-diffusing B or equimolar counter current diffusion, counter diffusion of A and B. So depending on these situations, we can define the mass transfer coefficients, and as we know for a particular film thickness delta, the flux we can write as the mass transfer coefficient into the driving force.

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Diffusion of A through Non-diffusing B


Gas phase: $N_A = K_g (p_{A1} - p_{A2}) = K_y (y_{A1} - y_{A2}) = K_c (C_{A1} - C_{A2}) \rightarrow (1)$

Liquid phase: $N_A = K_L (x_{A1} - x_{A2}) = K_c (C_{A1} - C_{A2}) \rightarrow (2)$

$K_y = \frac{\text{kmol/(m}^2 \cdot \text{s)}}{\text{partial pr. of A}}$

For ideal gas $C_A = \frac{p_A}{RT}$

$N_A = \frac{D_{AB} A}{2T L p_{\text{atm}}} (p_{A1} - p_{A2})$; $p_{\text{atm}} = \frac{p_{A2} - p_{A1}}{\ln(p_{A2}/p_{A1})}$



Let us consider a case of diffusion of A through non-diffusing B, how to calculate the mass transfer coefficient. So, for the case of diffusion of A through non-diffusing B, we can write flux, is equal to k_g , the gas phase mass transfer coefficient between two points. If the partial pressure difference is p_{A1} and p_{A2} , then it is $k_g (p_{A1} - p_{A2})$, is equal to $k_y (y_{A1} - y_{A2})$. It is in mole fraction basis, molar fraction, or if in terms of concentration also we can write, mass transfer coefficient into $C_{A1} - C_{A2}$; say equation 1, this is for the gas phase. For liquid phase, we can write flux is equal to $k_L (x_{A1} - x_{A2})$ is equal to $k_L (C_{A1} - C_{A2})$. So this is equation 2, where k_g , k_y and k_c are the gas phase mass transfer coefficient. Here k_x and k_L are the liquid phase mass


transfer coefficients. The k_y has the unit like, k mole per meter square second into delta y ; delta y is the mole fraction driving force. Now, if we compare for the ideal gas, we can write C_A , C_A is equal to p_A by $R T$, where p_A is the partial pressure of A. And if we considered the thickness between the 2 point is L , we know that the flux equations for diffusion of A, through non-diffusing B, we have earlier developed N_A is equal to $d A B p_t$ divided by $R T L p_{B1m}$ into p_{A1} minus p_{A2} , p_{B1m} is the log mean pressure difference, which is p_{B2} minus p_{B1} divided by $L N p_{B2}$ by p_{B1} .

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Diffusion of A through Non-diffusing B

$$k_g = \frac{D_{AB} A}{RT \delta p_{B1m}}, \quad k_y = \frac{D_{AB} p_t^2}{RT \delta p_{B1m}}, \quad k_c = \frac{D_{AB} h_i}{\delta p_{B1m}}$$

$$N_A = \frac{D_{AB} (\rho/M)_{avg}}{\delta x_{B1m}} (x_{A1} - x_{A2})$$


$$k_x = \frac{D_{AB} (\rho/M)_{avg}}{\delta x_{B1m}}, \quad k_L = \frac{D_{AB}}{\delta x_{B1m}}$$


So, if we compare this equation with equation one, we can obtain k_g is equal to $D A B p_t$ divided by $R T L$ or delta $p B L M$ k_y $D A B p_t$ square divided by $R T$ delta $p B L M$, and k_c is $D A B p_t$ by delta $p B L M$. Similarly for the liquid phase, the diffusion of A through non-diffusing B, we know that flux equation N_A is equal to $D A B \rho$ by m average, divided by delta $x B L$, into x_{A1} minus x_{A2} . So, if we compare this equation, with this equation 2, we can obtain, so the relations this will be say delta. So, we have compared this equations with equation one, to obtain the correlations of gas phase mass transfer coefficient k_g k_y and k_c . Now, if we compare these equations for the liquid phase flux, with the second equation, we can obtain the correlations between the liquid phase mass transfer coefficients. So, from that we can write k_x is equal to $D A B \rho$ by m average, divided by delta $x B L M$, and k_L is equal to $d A B$ by delta $x B L M$.

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Diffusion of A through Non-diffusing B

$$k_c = RT k_g, \quad k_y = \frac{p}{T} k_g$$

$$k_x = \left(\frac{\rho}{M}\right)_{\text{avg}} k_L$$


We can relate among the mass transfer coefficient we can write k_c is $R T k_g$. So, from this we can clearly see that $d A B p t$ by $\Delta p B L M$, this part is k_c . So, the k_c is equal to $R T k_g$. Similarly, k_y is equal to $p t k_g$, and k_x we can write ρ by m average into k_L , so the relations between the mass transfer coefficient in the gas phase, as well as in the liquid phase.

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Equimolar Counterdiffusion of A and B

Gas Phase

$$N_A = k_g' (p_{A1} - p_{A2}) = k_y' (y_{A1} - y_{A2}) = k_c' (C_{A1} - C_{A2}) \rightarrow (1)$$


Liquid phase

$$N_A = k_x' (x_{A1} - x_{A2}) = k_L' (C_{A1} - C_{A2}) \rightarrow (2)$$

Gas Phase

$$N_A = \frac{D_{AB}}{RT\delta} (p_{A1} - p_{A2}) \rightarrow (3)$$

Liquid phase

$$N_A = \frac{D_{AB}(\rho/M)_{\text{avg}}}{\delta} (x_{A1} - x_{A2}) \rightarrow (4)$$


Now, consider another case, where equimolar counter diffusion of A and B. If we consider the flux for the gas phase, we can write flux is equal to k_g dash. So, the dash

which we distinguish between the equimolar counter diffusion, and the diffusion of A through non-diffusing B. So, into pressure driving force $p_A 2$ is equal to k_y dash, $y_A 1$ minus $y_A 2$, is equal to k_c dash, $c_A 1$ minus $c_A 2$. And for the liquid phase, we can write flux is equal to k_x dash $x_A 1$ minus $x_A 2$ is equal to k_L dash $c_A 1$ minus $c_A 2$. So, say, this is equation number three and this is equation number four. Now, for equimolar counter diffusion, we know that flux N_A is equal to D_{AB} by $R T \Delta p_A 1$ minus $p_A 2$. So, if we compare this relation; say x with equation number three, we could be able to obtain the relations between k_g , k_y and k_c .


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Equimolar Counterdiffusion of A and B

Gas Phase

$$k_g' = \frac{D_{AB}}{RT\delta}, \quad k_y' = \frac{D_{AB}P}{RT\delta}, \quad k_c' = \frac{D_{AB}}{\delta}$$

Liquid Phase:

$$k_x' = \frac{D_{AB}(\rho/M)_{avg}}{\delta}; \quad k_L' = \frac{D_{AB}}{\delta}$$


So, the equation for the gas phase, we obtain k_g dash will be D_{AB} by $R T \Delta$, and k_y dash is $D_{AB} p$ by $R T \Delta$, and k_c dash is equal to D_{AB} by δ . Similarly, for the case of liquid phase, we know that flux. This is for gas phase, and this is for liquid phase, flux is equal to D_{AB} into ρ by M average by δ into $x_A 1$ minus $x_A 2$. So, if we compare this equation y with equation four, we could be obtain the relations between k_x and k_L . So, for liquid phase, k_x dash would be $D_{AB} \rho$ by M average, divided by δ and k_L dash D_{AB} by δ .

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Equimolar Counterdiffusion of A and B

$$k'_c = \frac{RT}{P_t} k'_y = RT k'_g$$

$$k'_x = \left(\frac{P}{M}\right)_{\text{avg}} k'_L = C_{\text{avg}} k'_L$$

$$Y_A = \frac{y_A}{1-y_A}, \quad X_A = \frac{x_A}{1-x_A}$$

$$N_A = k_Y (Y_{A1} - Y_{A2}) \rightarrow \text{Gas phase}$$

$$N_A = k_X (X_{A1} - X_{A2}) \rightarrow \text{Liquid phase}$$


So, we could convert between the k_c dash is equal to RT by p_t , k_y dash is equal to RT k_g dash. Similarly, k_x dash is ρ by M average into k_L dash is equal to C average into k_L dash, so this is the conversion. Now, if the concentration terms are defined in terms of mole ratio unit; that means, y_A is equal to y_A divided by 1 minus y_A , and that is the mole ratio basis, and x_A is equal to x_A by 1 minus x_A . If we define this way, the flux equation N_A we can write $k_Y (Y_{A1} - Y_{A2})$, and incase this is for gas phase, and flux N_A is equal to $k_X (X_{A1} - X_{A2})$, this is for liquid phase, this is mole ratio unit that is air free basis.

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Mass Transfer Coefficients
Diffusion of A into Non-diffusing B Vs.
Equimolar Counterdiffusion of A and B

Diffusion of A into non-diffusing B

$k_g, k_y, k_c, k_x, k_L \Rightarrow$ related with the log mean conc. of the species B, which is non-diffusing $\rightarrow P_{B,lm}$ or $X_{B,lm}$

$k'_g, k'_y, k'_c, k'_x, k'_L \Rightarrow$ not dependent on log mean conc. diff. of species B.

$k'_c = \text{Coulburn-Drew MT Coefficient}$



Now, the mass transfer coefficients between the two systems; diffusion of A into non-diffusing B, and equimolar counter diffusion of A and B, what are the difference? In case of diffusion of A into non-diffusing B, the mass transfer coefficients which are k_g , k_y , k_c , k_x and k_l , these are related with the log mean concentrations of the species, log mean concentration of the species B which is non-diffusing. So, the mass transfer in this case, depends on p_{BLM} or x_{BLM} . But on the other hand for the equimolar counter diffusion of A and B, the mass transfer coefficient k_g , k_y and k_c , k_x and k_l , these are not dependent on log mean concentration difference of species B. This type of mass transfer coefficient is known as Colburn Drew mass transfer coefficients.

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F-Type Mass Transfer Coefficient

$$N_A = \frac{N_A}{N_A + N_B} \frac{D_{AB} P_t}{RT \delta} \ln \frac{[N_A/(N_A + N_B)] - Y_{A2}}{[N_A/(N_A + N_B)] - Y_{A1}}$$

$$= \frac{N_A}{N_A + N_B} F \ln \frac{[N_A/(N_A + N_B)] - Y_{A2}}{[N_A/(N_A + N_B)] - Y_{A1}}$$

$$Y_A = \frac{p_A}{P_t}, \quad F = \frac{D_{AB} P_t}{RT \delta}$$

Diffusion of A through non-diffusing B
 $F = k_g P_{BLM}$, $F = k_g' P_t$
 Equimolar counter diff.



Now, there is another type of mass transfer coefficient, which is f type mass transfer coefficient, and we know earlier we have derived the flux equation N_A , is equal to N_A by $N_A + N_B$ $D_{AB} p_t$ divided by $R T \delta L$, N_A divided by $N_A + N_B$ minus Y_{A2} divided by N_A by $N_A + N_B$, minus Y_{A1} . So, this we can write equal to N_A by $N_A + N_B$ into $F L$ N_A by $N_A + N_B$ minus Y_{A2} divided by N_A by $N_A + N_B$ minus Y_{A1} . In this case we can write Y_A is equal to p_A by p_t , and F is equal to $D_{AB} p_t$ by $R T \delta$. Similarly, for diffusion of A through non-diffusing B, this correlations can be obtained F is equal to $k_g p_{BLM}$. And also for equimolar counter diffusion F , we can write k_g dash p_t , this is diffusion of A through non-diffusing B, and this is for equimolar counter diffusion.

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Relation between k_G and k_Y


For two different points 1 and 2

$$Y_{A1} = \frac{p_{A1}}{P_t - p_{A1}}, \quad Y_{A2} = \frac{p_{A2}}{P_t - p_{A2}}$$

$$Y_{A1} - Y_{A2} = \frac{p_{A1}}{P_t - p_{A1}} - \frac{p_{A2}}{P_t - p_{A2}} = \frac{p_t (p_{A1} - p_{A2})}{p_{A1} p_{A2}}$$

$$(p_{A1} - p_{A2}) = (Y_{A1} - Y_{A2}) \frac{p_{A1} p_{A2}}{p_t}$$

$$N_A = k_G (p_{A1} - p_{A2}) = \frac{D_{AB} P_t}{RT \delta_{AB} L} (p_{A1} - p_{A2}) = \frac{D_{AB} P_t (Y_{A1} - Y_{A2}) \frac{p_{A1} p_{A2}}{p_t}}{RT \delta_{AB} L}$$

$$N_A = k_Y (Y_{A1} - Y_{A2}); \quad k_Y = \frac{D_{AB} p_{A1} p_{A2}}{RT \delta_{AB} L} = k_G \frac{p_{A1} p_{A2}}{P_t}$$


So, what is the relation between k_G and k_Y , we know that for two different points 1 and 2, we can write $y_{A1} = \frac{p_{A1}}{P_t - p_{A1}}$ and $y_{A2} = \frac{p_{A2}}{P_t - p_{A2}}$. So, the difference $y_{A1} - y_{A2}$ will be equal to $\frac{p_{A1}}{P_t - p_{A1}} - \frac{p_{A2}}{P_t - p_{A2}}$, which will be equal to $\frac{p_t (p_{A1} - p_{A2})}{p_{A1} p_{A2}}$. So, we can write $p_{A1} - p_{A2}$ would be equal to $(y_{A1} - y_{A2}) \frac{p_{A1} p_{A2}}{p_t}$. Now, we know that flux N_A is equal to $k_G (p_{A1} - p_{A2})$ is equal to $\frac{D_{AB} P_t}{RT \delta_{AB} L} (p_{A1} - p_{A2})$ is equal to $\frac{D_{AB} P_t (y_{A1} - y_{A2}) \frac{p_{A1} p_{A2}}{p_t}}{RT \delta_{AB} L}$. So, we know that N_A is equal to $k_Y (y_{A1} - y_{A2})$. So, we can write k_Y is equal to $\frac{D_{AB} p_{A1} p_{A2}}{RT \delta_{AB} L}$. So, we can write k_G into $\frac{p_{A1} p_{A2}}{P_t}$. Similarly, we can derive the relations between $k_{G,dash}$ and $k_{Y,dash}$.


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Relation between the k_G' and k_Y'

$$p_{A1} - p_{A2} = (Y_{A1} - Y_{A2}) \frac{p_{B1} p_{B2}}{p_t}$$

$$N_A = k_G' (p_{A1} - p_{A2}) = \frac{D_{AB}}{RT\delta} (p_{A1} - p_{A2}) = \frac{D_{AB}}{RT\delta} (Y_{A1} - Y_{A2}) \frac{p_{B1} p_{B2}}{p_t}$$

$$N_A = k_Y' (Y_{A1} - Y_{A2})$$


$$k_Y = \frac{D_{AB} p_{B1} p_{B2}}{RT\delta} = k_G' \frac{p_{B1} p_{B2}}{p_t}$$


As we know the relations between $p_{A1} - p_{A2}$ is equal to $y_{A1} - y_{A2}$ into $p_{B1} p_{B2}$ by p_t . We can write flux N_A is equal to k_G' $p_{A1} - p_{A2}$ is equal to $\frac{D_{AB}}{RT\delta}$, and into $p_{A1} - p_{A2}$ is equal to $\frac{D_{AB}}{RT\delta} (y_{A1} - y_{A2}) \frac{p_{B1} p_{B2}}{p_t}$. And we know that N_A is equal to k_Y' $y_{A1} - y_{A2}$. So, we can write k_Y' is equal to $\frac{D_{AB} p_{B1} p_{B2}}{RT\delta}$ is equal to $k_G' \frac{p_{B1} p_{B2}}{p_t}$. So, similar correlations like k_G and k_Y , we can also obtain the relations between k_G and k_Y .

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Conversion among the Gas Phase Mass Transfer Coefficients

$$F = k_g p_{BLM} = k_Y \frac{p_{BLM}}{p_t} = k_c \frac{p_{BLM}}{RT}$$


$$= k_g p_t = k_Y' = k_c' \frac{p_t}{RT}$$


Now, the conversion among the gas phase mass transfer coefficients. So, we know F is equal to $k_g p_{B,L,M}$, and this related with k_y ; $k_y p_{B,L,M}$ by p_t is equal to $k_c p_{B,L,M}$ by $R T$ which we can write $k_g p_t$ is equal to k_y dash is equal to k_c dash p_t divided by $R T$. Similarly, we can get the relations among the liquid phase mass transfer coefficients.

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**Conversion among the Liquid Phase
Mass Transfer Coefficients**

$$F = k_x x_{B,L,M} = k_L x_{B,L,M} C$$

$$= k'_L C = k'_L \frac{\rho}{m} = k'_x$$


So, that is also related with F time mass transfer coefficients, which is equal to $k_x x_{B,L,M}$ is equal to $k_L x_{B,L,M}$ into concentration is equal to k_L dash C is equal to k_L dash ρ by m is equal to k_x dash. So, these are the relation among the mass transfer coefficient, in the gas phase and the liquid phase.

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Example 1.1

Large volume of pure N_2 gas at atmospheric pressure is flowing over a pool of liquid of methanol, which is evaporating. N_2 is assumed to be insoluble in the liquid. The gas phase mass transfer coefficient of methanol is $k_G = 2 \times 10^{-5} \text{ kmol/m}^2 \text{ s kPa}$. Assume vapour pressure of methanol at 298K is 10 kPa.

- (i) Calculate k_y , k_c , k_f and F
- (ii) If the diffusivity of methanol at 298K is $2 \times 10^{-5} \text{ m}^2/\text{s}$, calculate the thickness of the gas film



So, let us consider an example, to calculate mass transfer coefficients in the gas phase, and also the film thickness, or the gas film thickness. So, consider large volume of pure nitrogen gas, at atmospheric pressure is flowing over a pool of liquid of methanol, which is evaporating, and nitrogen is assumed to be insoluble in liquid. The gas phase mass transfer coefficient of methanol is given; assume vapor pressure of methanol at 298 kelvin is 10 kilopascal. Calculate k_y , $k_{small y}$, k_c $k_{capital y}$ and f , and the second problem, if the diffusivity of methanol at 298 kelvin is $2 \times 10^{-5} \text{ m}^2/\text{s}$. Calculate the thickness of the gas film.

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Example 1.1: Solution

$$\begin{aligned} (1) \quad P_t &= 1 \text{ atm} = 101.3 \text{ kPa} \\ R &= 0.082 \text{ (m}^3 \text{ atm / kmol K)} = 8.314 \text{ (J / kmol K)} \\ T &= 298 \text{ K} \\ k_y &= k_G P_t = 2 \times 10^{-5} \text{ (kmol / m}^2 \text{ s kPa)} \times 101.3 \text{ kPa} \\ &= 2.03 \times 10^{-3} \text{ (kmol / m}^2 \text{ s)} \\ k_c &= k_y RT = 2 \times 10^{-5} \times 8.314 \times 298 \text{ m/s} \\ &= 0.0495 \text{ m/s} \end{aligned}$$



Now, let us consider for the first case, this is the case of diffusion of A through non-diffusing B, and given p_t is one atmosphere, which is 101.3 kilopascal, R is 0.082 meter cube atmosphere per k mole Kelvin, which is equal to 8.3066 meter cube kilopascal per k mole Kelvin, and T is given 298 kelvin. Now $k_{small y}$ is equal to $k_g p_t$ from the conversion equation. So, we can write 2 into 10 to the power minus 5 k mole per meter square second, kilopascal into p_t 101.3 kilopascal. So, this will give you 2.03 into 10 to the power minus 3 k mole per meter square second delta y . Similarly, we can calculate k_c , which is $k_g R T$. So, k_g is 2 into 10 to the power minus 5, R is equal to 8.3066, and temperature is 298 kelvin, this is meter per second, which is equal to 0.0495 meter per second.

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Example 1.1: Solution

$$p_{A1} = 10 \text{ kPa}$$


$$p_{B1} = p_t - p_{A1} = (101.3 - 10) \text{ kPa} = 91.3 \text{ kPa}$$

Also, $p_{A2} = 0$, $\therefore p_{B2} = p_t = 101.3 \text{ kPa}$

$$K_Y = k_g \frac{p_{A1} p_{B2}}{p_t} = 2 \times 10^{-5} \frac{91.3 \times 101.3}{101.3}$$

$$= 1.83 \times 10^{-3} \frac{\text{kmol}}{\text{m}^2 \text{ s } (\Delta Y)}$$

$$F = K_Y p_{B1} \ln = 2 \times 10^{-5} \times \frac{p_{B2} - p_{B1}}{\ln p_{B2}/p_{B1}} = 2 \times 10^{-5} \times \frac{101.3 - 91.3}{\ln(101.3/91.3)}$$

$$= 1.92 \times 10^{-3} \text{ kmol/m}^2 \text{ s}$$


Another is $k_{capital y}$. So, p_{A1} , the partial pressure at point at the surface is 10 kilopascal. So, p_{B1} is equal to p_t minus p_{A1} , which is equal to 101.3 minus 10 kilopascal, which is 91.3 kilopascal, and also p_{A2} is equal to 0. Therefore, p_{B2} is equal to p_t , is equal to 101.3 kilopascal. So, k_Y capital Y is equal to $k_g p_{B1}$, p_{B2} by p_t , we have derived this equation. So, if we substitute 2 into 10 to the power minus 5, 91.3 into 101.3 divided by 101.3, this is equal to 1.83 into 10 to the power minus 3 k mole per meter square second delta y . And we know the relations between F and $k_g p_{B1} \ln$. So, this is 1, and we can calculate F , which is equal to 2 into 10 to the power minus 5 into p_{B2} minus p_{B1} by \ln , p_{B2} by p_{B1} is equal to 2 into 10 to the power minus

5, 101.3 minus 91.3 by L N 101.3 by 91.3. So, this will give the value of 1.92 into 10 to the power minus 3 k mole per meter square second.


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Example 1.1: Solution

$$k_g = \frac{D_{AB} P_t}{RT \delta P_{BLM}}$$

$$\Rightarrow \delta = \frac{D_{AB} P_t}{RT k_g P_{BLM}}$$

$$D_{AB} = 2 \times 10^{-5} \text{ m}^2/\text{s}$$

$$P_t = 1 \text{ atm} = 101.3 \text{ kPa}$$


So, to calculate the film thickness, we know k_g is $D_{AB} p_t$ divided by $R T \delta p_{B L M}$. So, δ , we can write is equal to $D_{AB} p_t$ divided by $R T k_g p_{B L M}$. D_{AB} is given 2 into 10 to the power minus 5 meter square per second, p_t is 1 atmosphere is equal to 101.3 kilopascal.

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Example 1.1: Solution


$$R = 0.082 \text{ m}^3 \text{ atm / (kmol K)}$$

$$= 8.3066 \text{ (m}^3 \text{ kPa / (kmol K))}$$

$$T = 298 \text{ K}$$

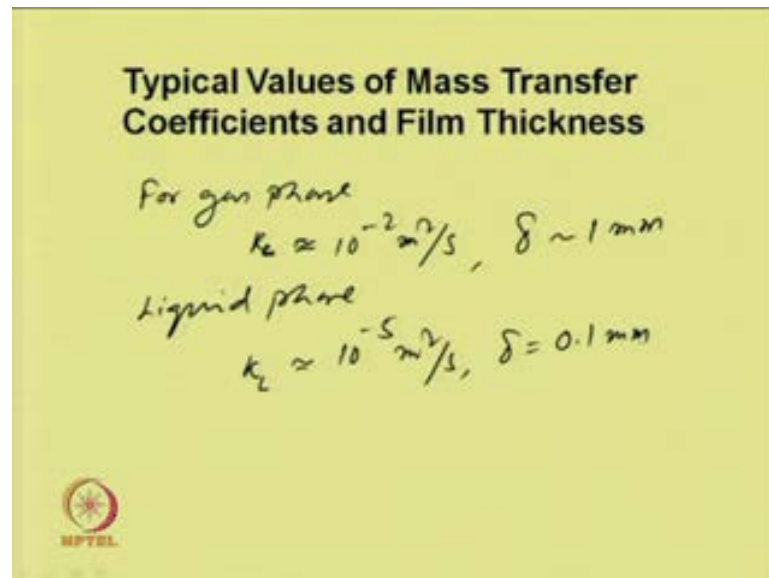
$$k_g = 2 \times 10^{-5} \text{ (kmol / (m}^2 \cdot \text{s kPa))}$$

$$P_{BLM} = \frac{101.3 - 91.3}{\ln 101.3/91.3} = 96.213$$

$$\delta = 0.425 \text{ mm}$$


And R is 0.082 meter cube atmosphere per k mole Kelvin is equal to 8.3066 meter cube kilopascal k mole Kelvin. So, T is 298 Kelvin. So, k g is equal to 2×10^{-5} k mole per meter square second kilopascal, P B L M we have already calculated $101.3 - 91.3$ L N 101.3×91.3 is equal to 96.213. So, after substitution delta will be 0.425 millimeter. So, this is the typical film thickness.

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So, the typical values for the mass transfer coefficient and the film thickness, in case of the gas phase, k_c is equal to about 10^{-2} meter square per second, and film thickness delta is approximately 1 millimeter. In case of liquid phase k_L is approximately 10^{-5} meter square per second, and delta is film thickness is around 0.1 millimeter. So, this is end of lecture 1 of module 2.

Thank you.