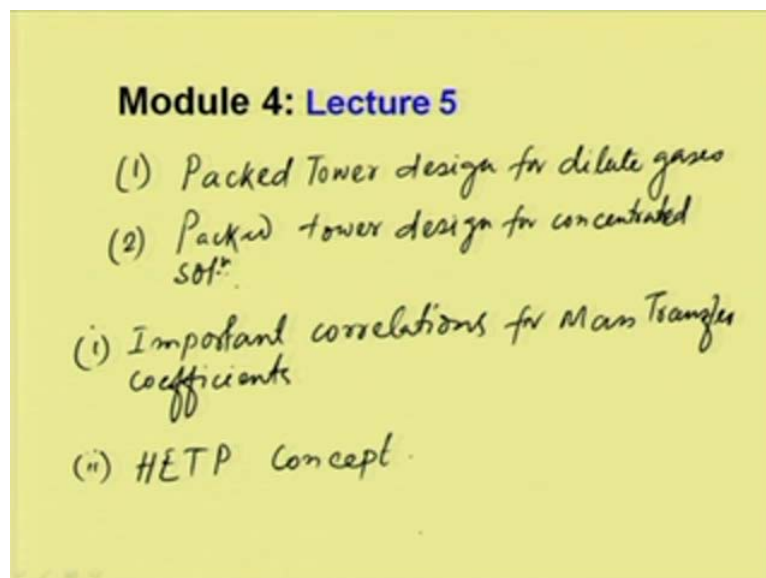


Mass Transfer Operations I
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Module - 4
Absorption
Lecture - 5
Mass Transfer Coefficients
Correlation and HETP Concept

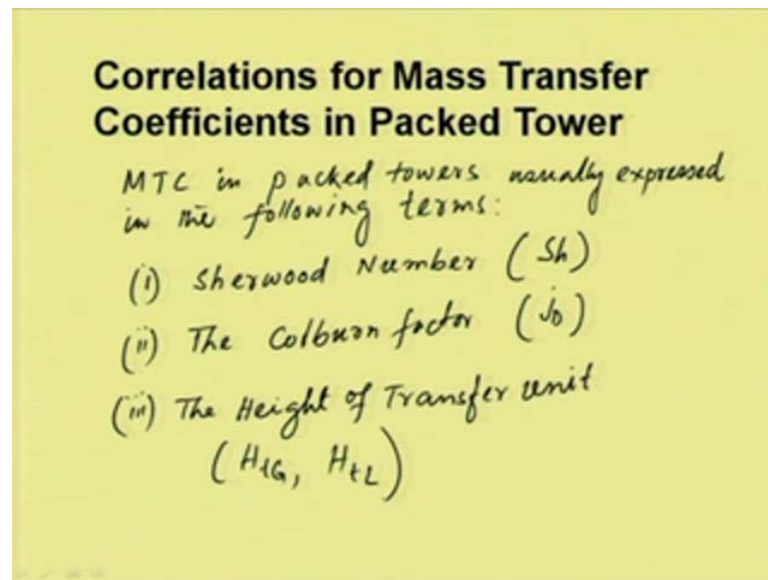
Welcome to the fifth lecture of module 4. We are discussing absorption.

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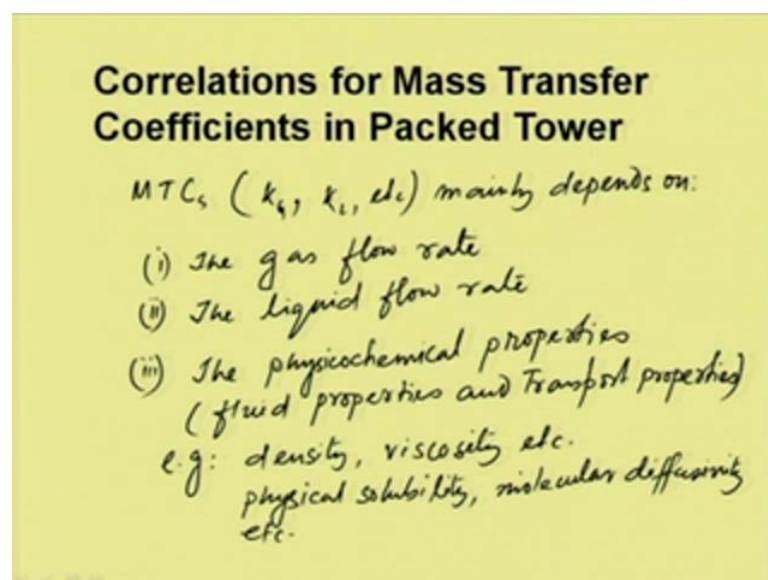
In the previous lecture, we have mainly considered two things; one is packed tower design for dilute gases, and second thing we have discussed, packed tower design for concentrated. So, for dilute solutions, we generally consider the mole fractions of the solute both in gas as well as liquid phases, should be less than 0.1 that is 10 percent, and above that we should consider concentrated solution. So, these two methods we have discussed, and we have seen the examples how to solve different problems. In this lecture, we will discuss the correlations, some of the important correlations for mass transfer coefficient and second thing we will discuss HETP concept that is height equivalent to a theoretical plate HETP concept.

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So, let us consider the first thing correlations for mass transfer coefficients. The mass transfer coefficient that is MTC mass transfer coefficients in packed towers generally expressed, usually expressed in the following terms. What are those Sherwood number Sh and secondly the Colburn factor which is defined as j_D , the height of transfer unit height of transfer unit which is H_{tG} or H_{tL} .

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The mass transfer coefficients generally k_G , small k_G , k_L etcetera mainly depends on the gas flow rate, second the liquid flow rate and third the physicochemical properties

that is fluid properties and transport properties. So, the fluid properties like for example, density, viscosity etcetera and the transport properties like physical solubility, molecular diffusivity etcetera.

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Correlations for Mass Transfer Coefficients in Packed Tower

Simple eqns

i) Gas-phase mass transfer in packed bed
Packing: Rashing ring or Berl shaddle
Shulman and Co-workers (1955) proposed:

$$j_D = 1.195 \left[\frac{d_s G'}{\mu_G (1 - \mu_L)} \right]^{-0.36}$$

d_s = dia. of the sphere having same surface area of a piece of packing particle.
 μ_G = gas viscosity, μ_L = liquid viscosity.

→ mass flow rate of the gas

So, there are several correlations available in the literature, which are derived mainly from the experimental data for different systems. So, some of the important equations we will discuss here. So, very simple equations, one is for gas phase mass transfer in packed bed. Here the packing used is Rashing ring or Berl Shaddle and Shulman and Coworkers in 1955 proposed the equation, proposed the following equations j_D is equal to $1.195 d_s G$ dash divided by $\mu_G (1 - \mu_L)$ whole to the power minus 0.36 d_s is the diameter of sphere having the same surface area of a piece of packing particle and μ_G is the gas viscosity, μ_L is the liquid viscosity and G dash is the mass flow rate of the gas. G dash, this is the mass flow rate of the gas.

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Correlations for Mass Transfer Coefficients in Packed Tower

2) Absorption of SO_2 in water in a packed bed
Packing used: 1 inch Rasching ring
Dutta (2007) given the following correlation:

$$H_{tG} = 1.24 (G')^{0.3} / (L')^{0.25} \text{ ft.}$$

$$H_{tL} = 0.37 / (L')^{0.18} \text{ ft.}$$

G' and L' = gas and liquid flow rates in lb/hr ft².

Let us consider another system absorption of SO_2 in water, in a packed bed. The packing used is 1 inch Rasching ring and there is a correlations which is given by Dutta 2007, following correlation H_{tG} is equal to 1.24 G' dash to the power 0.3 divided by L' dash to the power 0.25 feet and H_{tL} is equal to 0.37 divided by L' dash to the power 0.18 feet where G' dash and L' dash, gas and liquid flow rates in pound per hour feet square.

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Correlations for Mass Transfer Coefficients in Packed Tower

3) Onda and co-workers (1968) for the mass transfer parameters:

$$\frac{a_{eff}}{a_p} = 1 - \exp \left[-1.45 \left(\frac{G_L}{G} \right)^{0.75} (Re_L)^{0.1} (F_L)^{-0.05} \right]$$

$$k_L \left(\frac{\rho_L}{\mu_L g} \right)^{1/3} = 0.0051 (Re_L)^{2/3} \left(\frac{a_p}{a_{eff}} \right)^{2/3} (Sc_L)^{-1/2} (a_p d_p)^{0.4}$$

$$k_c / (a_p D_g) = C (Re_g)^{0.7} (Sc_g)^{1/3} (a_p d_p)^{-2.0}$$

So, another correlation which is given by Onda and co-workers in 1968 for the mass transfer parameters, a effective divided by a p is equal to 1 minus exponential 1.45 sigma

c by σ to the power 0.75 Reynolds number to the power 0.1 Froude number to the power minus 0.05 and Wave 1 number to the power 0.2. So, each number we will discuss later and k_L into ρL divided by μL into g to the power one third is equal to 0.0051, Reynolds number to the power two by three a_p by a effective to the power two third Schmidt number to the power minus half $a_p d_p$ to the power 0.4. Another correlations for k_c , k_c divided by $a_p D G$ is equal to c , c is a constant Reg to the power 0.7 Schmidt number to the power one third $a_p d_p$ to the power minus 2.

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Correlations for Mass Transfer Coefficients in Packed Tower

$$c = 2.0 \text{ for } d_p < 15 \text{ mm}$$

$$= 5.23 \text{ for } d_p > 15 \text{ mm}$$

d_p = nominal packing size
 σ_c = critical surface tension at the packing surface, dynes/cm
 ceramic - 61, polyethylene - 33,
 glass - 73, metal - 75

So, here this c , c is equal to 2.0 for d_p less than 15 millimeter and this equal to 5.23 for d_p greater than 15 millimeter, d_p is the nominal packing size, σ_c is the critical surface tension at the packing surface in dynes per centimeter and it varies like for ceramic it is 61, polyethylene 33, glass 73 and metal 75.

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Correlations for Mass Transfer Coefficients in Packed Tower

$$Re_G = \frac{\mu_g \rho_g}{a_p \mu_g} ; \quad Sc_g = \frac{\mu_g}{\rho_g D_g}$$

$$Re_L = \frac{\mu_L \rho_L}{a_p \mu_L} ; \quad Fr_L = \frac{u_L^2 a_p}{g}$$

$$We = \text{weber number} = \frac{u_L^2 \rho_L}{\sigma_L a_p}$$

Re G is equal to mu G rho G by a p mu G. Schmidt number is equal to mu G by rho G into D G. Re L is equal to mu L rho L divided by a p by mu L, this is G, this is equal to u L square a p divided by g, weber number is equal to, weber number which is equal to u L square rho L by sigma L a p.

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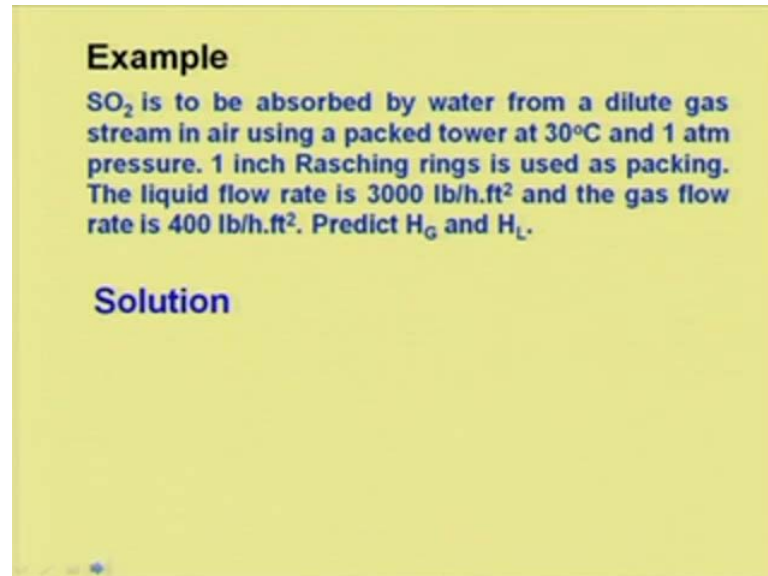
Correlations for Mass Transfer Coefficients in Packed Tower

$k_c, k_L \rightarrow$ mass transfer coefficients.
 $\rho_L =$ density
 $\mu_L =$ viscosity
 $D =$ diffusivity, m^2/s
 $\bar{a}_{eff} =$ effective gas-liquid specific interfacial area of contact
 $a =$ sp surface area of dry packing, m^2/s
 $u =$ superficial velocity.

So, here k c and k L which is the mass transfer coefficients, rho L is the density, mu L is the viscosity, D is the diffusivity meter square per second, a effective is the effective gas liquid specific inter facial area of contact and a is the specific surface area of dry

packing, specific surface area of dry packing say meter square per meter cube and u is the superficial velocity.

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Example
 SO_2 is to be absorbed by water from a dilute gas stream in air using a packed tower at 30°C and 1 atm pressure. 1 inch Rasching rings is used as packing. The liquid flow rate is 3000 lb/h.ft^2 and the gas flow rate is 400 lb/h.ft^2 . Predict H_G and H_L .

Solution

Now, let us take a very simple example, how to calculate the height of transfer units H_G and H_L . So, if we take the example sulphur dioxide is to be absorbed by water from a dilute gas stream in air using a packed tower at 30 degree centigrade and 1 atmosphere pressure 1 inch Rasching rings is used as packing, the liquid flow rate is 3000 pound per hour feet square and the gas flow rate is 400 pound per hour feet square. Predict H_G and H_L .

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Correlations for Mass Transfer Coefficients in Packed Tower

2) Absorption of SO_2 in water in a packed bed
Packing used: 1 inch Rasching ring
Dutta (2007) given the following correlation:

$$H_{tG} = 1.24 (G')^{0.3} / (L')^{0.25} \text{ ft.}$$

$$H_{tL} = 0.37 / (L')^{0.18} \text{ ft.}$$

G' and L' = gas and liquid flow rates
in $\text{lb}/\text{h.ft}^2$.

So, if we go back and look into the correlations given for H_G and H_L which is for 1 inch Rasching ring and absorption of sulphurdioxide H_G equation is given and it is given that liquid and gas flow rate.

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Example

SO_2 is to be absorbed by water from a dilute gas stream in air using a packed tower at 30°C and 1 atm pressure. 1 inch Rasching rings is used as packing. The liquid flow rate is $3000 \text{ lb}/\text{h.ft}^2$ and the gas flow rate is $400 \text{ lb}/\text{h.ft}^2$. Predict H_G and H_L .

Solution

$$H_G = 1.24 (G')^{0.3} / (L')^{0.25}$$
$$= 1.24 (400)^{0.3} / (3000)^{0.25} \text{ ft} = 1.01 \text{ ft}$$

$$H_L = 0.37 / (L')^{0.18}$$
$$= 0.37 / (3000)^{0.18} = 0.09 \text{ ft.}$$

So, if we write these equations H_G is equal to $1.24 G$ dash to the power 0.3 divided by L dash to the power 0.25 which is equal to 1.24, G dash is 400 pound per hour feet square to the power 0.3 divided by liquid flow rate is 3000 is to the power 0.25, this much feet. So, it is equal to 1.01 feet. H_L which is 0.37 divided by L dash to the power 0.18 feet.

So, which is equal to 0.37 divided by 3000 to the power 0.18 which is equal to 0.09 feet.

So, similar systems can be solved using this correlations and for other systems as well.

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Height Equivalent to an Equilibrium Stage (Theoretical Plate): HETP

Common device for absorption

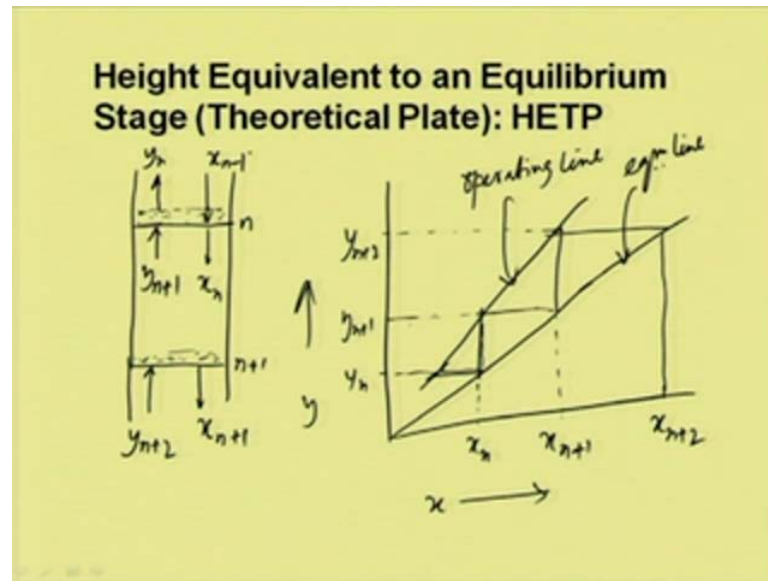
(i) Packed tower (ii) Tray column

- Simple design method for packed towers
— ignores the differences betⁿ stage wise and continuous contact.
- HETP is defined as:
$$HETP = \frac{Z}{N_T}$$

where Z = height of packing
 N_T = Number of ideal trays required to do the same job.

So, now we will discuss height equivalent to an equilibrium stage or theoretical plate. The common device for absorption, we have discussed before for absorption is packed tower and second is tray column. This HETP method is a simple design method for packed towers which is developed long before and this ignores the differences between stage wise and continuous contact. So, HETP is defined as HETP is equal to z divided by N_t , z is equal to height of packing and N_t is equal to number of ideal stage or trays required, number of ideal trays required to do the same job. So, it is the ratio between the height of packing and the number of ideal stage required for a given job.

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Now, let us consider the following figures. We have two different trays and this is named as n th tray, this is n plus 1 and say there is a liquid hold off on the tray. So, the liquid which is entering to n th plate is x_{n-1} and which is coming out from this tray is y_n , the gas which is coming out and the liquid which is coming out from this tray towards the down is x_n and the gas which is entering to this plate is y_{n+1} and the gas which is coming to the n plus 1 stage is y_{n+2} and the liquid which is coming out from this is x_{n+1} .

Now, if we plot the equilibrium curve and the operating line curve. So, this is y_{n+2} this is y_{n+1} , this is y_n and corresponding to this is x_n and this is x_{n+1} and this is x_{n+2} . So, x and y . So, this is equilibrium line and this is operating line.

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Height Equivalent to an Equilibrium Stage (Theoretical Plate): HETP

Two trays: n^{th} tray and $(n+1)^{\text{th}}$ tray

Consider the $(n+1)^{\text{th}}$ tray:

Inlet conc. of gas into $(n+1)^{\text{th}}$ tray = y_{n+2} (in mole fraction)

Outlet " " " " from " " = y_{n+1}

Inlet conc. of liquid into $(n+1)^{\text{th}}$ tray = x_n

Outlet " " " " from " " = x_{n+1}

$G' = \text{gas flow rate per unit area}$

$L' = \text{liquid " " " " " " " "}$

$\left. \begin{matrix} G' \\ L' \end{matrix} \right\} \Rightarrow \text{assumed constant}$

So, here we have used two trays, n^{th} tray and n plus one tray. Now, if we consider n plus 1 tray and if we do the balance, consider the n plus one tray inlet concentration of gas into n plus one tray is equal to y_{n+2} , This is in mole fraction. Outlet concentration, concentration of gas from this tray is y_{n+1} . Inlet concentration of liquid into n plus one tray is equal to x_n and outlet concentration of liquid from this tray is x_{n+1} and let consider G' gas flow rate per unit area and L' liquid flow rate per unit area. So, both assumed constant.

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Height Equivalent to an Equilibrium Stage (Theoretical Plate): HETP

For $(n+1)^{\text{th}}$ Plate

Rate of mass transfer = $G'(y_{n+2} - y_{n+1}) = L'(x_{n+1} - x_n)$

Rate of MT over a packing ht. of $z = K_a a_p z (y - y^*)_{\text{avg}}$

$(y - y^*)_{\text{avg}} = \text{average driving force over the packing height of } z$

Then if we do the mass balance over n plus one tray for n plus one plate. So, rate of mass transfer is equal to $G(y_{n+2} - y_{n+1})$ would be equal to $L(x_{n+1} - x_n)$. And rate of mass transfer over a packing height, height of z would be equal to $k_g \bar{a} p_t z (y - y^*)_{avg}$, where $(y - y^*)_{avg}$ is equal to average driving force over the packing height of z .

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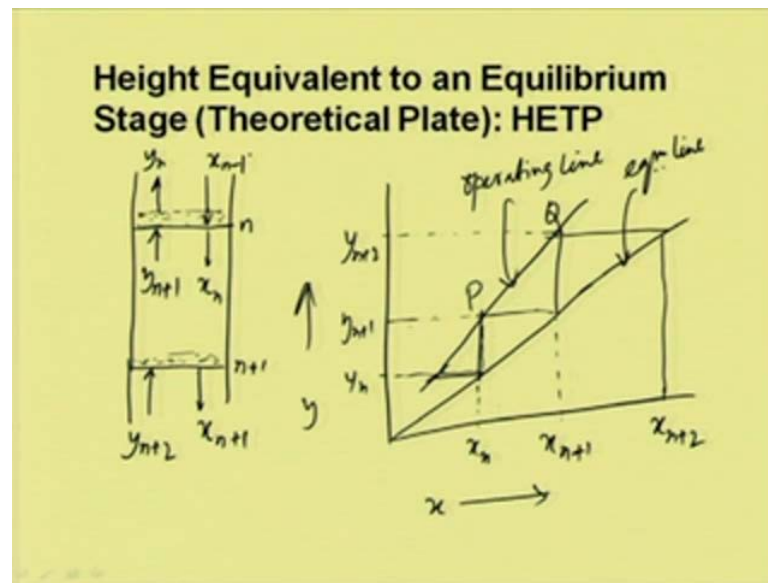
Height Equivalent to an Equilibrium Stage (Theoretical Plate): HETP

$$k_g \bar{a} p_t z (y - y^*)_{avg} = G(y_{n+2} - y_{n+1})$$

$$\Rightarrow z = \frac{G(y_{n+2} - y_{n+1})}{k_g \bar{a} p_t (y - y^*)_{avg}}$$

So, then if the rate of mass transfer on a tray is same as the rate of mass transfer over a packing surface we can write $k_g \bar{a} p_t z (y - y^*)_{avg}$ would be $G(y_{n+2} - y_{n+1})$. So, from which z we can calculate, it is $G(y_{n+2} - y_{n+1})$ divided by $k_g \bar{a} p_t (y - y^*)_{avg}$, it is reasonable to take this $(y - y^*)_{avg}$ as a log mean overall gas phase driving force between the point P and Q.

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So, between this, this is operating line. So, between this point P and Q, it is reasonable to take the log mean overall driving force for y minus y star average.

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Height Equivalent to an Equilibrium Stage (Theoretical Plate): HETP

$$(y - y^*)_{\text{avg}} = \frac{(y - y^*)_Q - (y - y^*)_P}{\ln \frac{(y - y^*)_Q}{(y - y^*)_P}}$$

$$= \frac{(y_{n+2} - y_{n+1}) - (y_{n+1} - y_n)}{\ln \left[\frac{y_{n+2} - y_{n+1}}{y_{n+1} - y_n} \right]}$$

So, if we take that y minus y star average would be y minus y star Q minus y minus y star P divided by ln y minus y star Q divided by y minus y star P. So, this would be y n plus 2 minus y n minus 1 minus y n plus 1 minus y n divided by ln y n plus 2 minus y n plus 1 divided by y n plus 1 minus y n.

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Height Equivalent to an Equilibrium Stage (Theoretical Plate): HETP

From the fig:

$$\frac{y_{n+1} - y_n}{y_{n+2} - y_{n+1}} = \frac{(y_{n+1} - y_n) / (x_{n+1} - x_n)}{(y_{n+2} - y_{n+1}) / (x_{n+1} - x_n)}$$

$$= \frac{\text{slope of equilibrium line}}{\text{slope of operating line}} = \frac{m}{L/G}$$

$$\Rightarrow \frac{mG}{L} - 1 = \frac{y_{n+1} - y_n}{y_{n+2} - y_{n+1}} - 1$$

$$= \frac{(y_{n+1} - y_n) - (y_{n+2} - y_{n+1})}{y_{n+2} - y_{n+1}}$$

So, from the figure we can write $y_{n+1} - y_n$ divided by $y_{n+2} - y_{n+1}$ is equal to $y_{n+1} - y_n$ divided by $x_{n+1} - x_n$ divided by $y_{n+2} - y_{n+1}$ divided by $x_{n+1} - x_n$. So, which is equal to slope of the equilibrium line, line divided by slope of the operating line. So, which is we can write m by L dash by G dash.

So, from this we can write mG dash by L dash minus 1 is equal to $y_{n+1} - y_n$ divided by $y_{n+2} - y_{n+1}$ minus 1. So, which is equal to $y_{n+1} - y_n$ minus $y_{n+2} - y_{n+1}$ divided by $y_{n+2} - y_{n+1}$.

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Height Equivalent to an Equilibrium Stage (Theoretical Plate): HETP

$$(y - y^*)_{avg} = \frac{(mG/L' - 1)(y_{n+2} - y_{n+1})}{\ln(mG/L')}$$

$$\therefore z = \frac{G'}{K_G a P_t} \times \frac{\ln(mG/L')}{(mG/L' - 1)} = H_{OG} \frac{\ln(mG/L')}{(mG/L' - 1)}$$

$$\therefore HETP = z = H_{OG} \frac{\ln(mG/L')}{(mG/L' - 1)} = H_{OG} \frac{\ln S}{S - 1}$$

The eqⁿ will not be valid for $mG = L$

Now, we can substitute this in the equations of $y - y^*$ average is equal to mG dash by L dash minus 1 into $y_{n+2} - y_{n+1}$ divided by $\ln mG$ dash by L dash. So, therefore, z would be G dash divided by capital k_G a bar p_t into $\ln mG$ dash by L dash divided by mG dash by L dash minus 1. So, which is equal to H_{OG} $\ln mG$ dash by L dash divided by mG dash by L dash minus 1. Therefore, HETP which is equal to z you can write is equal to H_{OG} $\ln mG$ dash by L dash divided by mG dash by L dash minus 1, which is we can write H_{OG} \ln of the stripping factor S divided by S minus 1. The equation will not be valid for mG equal to L .

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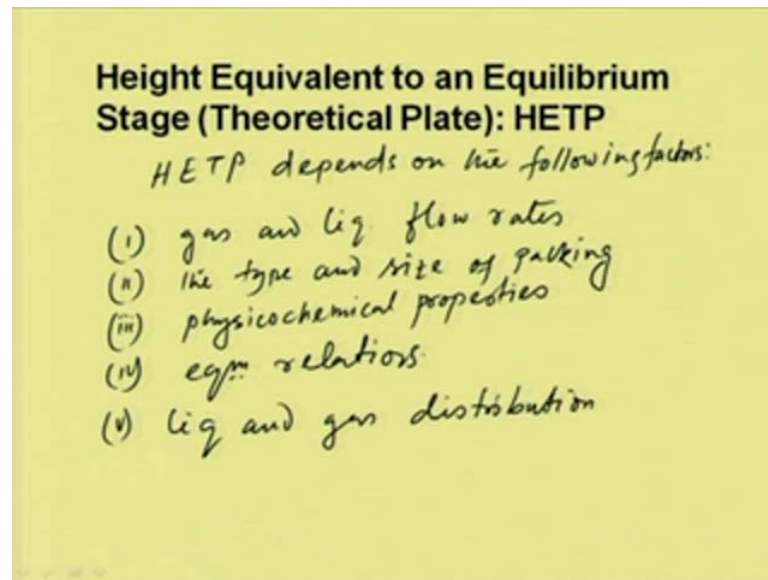
Height Equivalent to an Equilibrium Stage (Theoretical Plate): HETP

HETP is used to characterize the performance of packing

- A good packing will have small HETP
- widely used in packed distillation
- usually varies betⁿ 1 to 3 ft.

This HETP is generally used to characterize the performance of packing, HETP is used to characterize the performance of packing. So, the a good packing will have small HETP. This is widely used in packed distillation and its usually varies between 1 to 3 feet.

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This HETP depends on the following factors, one is the gas and liquid flow rates, second the type and size of packing, physicochemical properties, the equilibrium relations and the liquid and gas distribution.

Thank you