

Course on Industrial Biotechnology
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Lecture No 05
Chemical Reaction Kinetics

My next presentation is that chemical reaction kinetics, now in the chemical in the last class I discuss the how the different chemical reactions we can write the rate equations for the different type of reactions and we can remember that I told you that that if you look at the biochemical process the mostly the reactions that takes place either they are reversible in nature and also they are the chain reaction.

In the microorganism we have metabolic pathways in the metabolic pathways that that you have a series of reactions and you have you have different steps and the different steps and the individual steps are we have the reversible in nature. So we try to in the last lecture we come across this the reversible and in the reversible reaction we have forward reaction, we have backward reaction and we have come across the equilibrium constant K_C which is nothing but equal to concentration of product divided by concentration of substrate.

Then also in the chain reaction we try to establish that how the concentration of different component in the reaction mixture can be expressed, that in the in the chain reaction we have different components A, B, C, D so how the different these components will keep on changing with respect to time and how we can develop the equation for that.

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Irreversible parallel reaction

$$\left. \begin{array}{l} A \xrightarrow{k_1} R \\ A \xrightarrow{k_2} S \end{array} \right\}$$

□ The rates of change of the three component

$$-r_A = -\frac{dC_A}{dt} = k_1C_A + k_2C_A = (k_1 + k_2)C_A$$
$$r_R = \frac{dC_R}{dt} = k_1C_A$$
$$r_S = \frac{dC_S}{dt} = k_2C_A$$

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Now today I want to go little bit more on this and you will find that other type of reaction that we have we have parallel reaction parallel reaction means that this is the substrate same substrate may be it is producing two different products this is R and S. So if you have this kind of two different products so we call it parallel reaction or site reaction, then the rate expression rate of substrate that degradation can be expressed as k_1 into C_A plus k_2 into C_A and here you can you can C_A take the common k_1 plus k_2 .

Then rate of formation R you can always express as k_1 into C_A and rate of formation of S you can the this is parallel reaction also we can write like this.

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Autocatalytic reaction

□ Product itself acts as a catalyst

$$A + R \rightarrow R + R$$

The rate equation $-r_A = -\frac{dC_A}{dt} = kC_A C_R$

Total numbers of moles remain constant

$$C_0 = C_A + C_R = C_{A0} + C_{R0} = \text{constant}$$

Thus the rate equation become

$$-r_A = -\frac{dC_A}{dt} = kC_A(C_0 - C_A)$$

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Another very interesting thing is that autocatalytic reaction what is the autocatalytic reaction where A plus R and produce R and R is the product and R itself again as a catalyst to carry out the reaction. So that is that is why we call it autocatalytic reaction and if you take into the account in the microbial system particular it is largely applicable in the microbial system what is happening particularly in the (()) (3:31) fermentation process we use sugar for the formation of cell mass.

Now sugar is converted to cell mass and again again cell mass again it will like the substrate and produce cell mass. So this is a kind of autocatalytic reaction we can we can take into account.

Now if you have that kind of reaction how you can express this is r_A equal to minus dC_A by dt equal to k into C_A by C_R , when C_0 is the initial concentration it can be expressed as C_A

plus CR, CA0 plus CR0 is constant and rate expression can be written like this. So this is how we can express the autocatalytic reaction.

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Problems

Problem 1:

Reactant A decomposes in a batch reactor
 $A \longrightarrow B$

The composition of A in the reactor is measured at various times with results shown in the table.
 Find a rate equation to represent the data

t (h)	C_A (g/L)
0	10.00
1	9.80
2	9.60
3	8.90
4	8.50
5	6.90
6	5.50
7	4.80
8	3.20
9	2.60
10	1.70
11	1.00
12	0.80

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Solution:



Suppose order of the reaction is n, and kinetic rate constant is k.
 Then, the rate equation is $\frac{dC_A}{dt} = -kC_A^n$

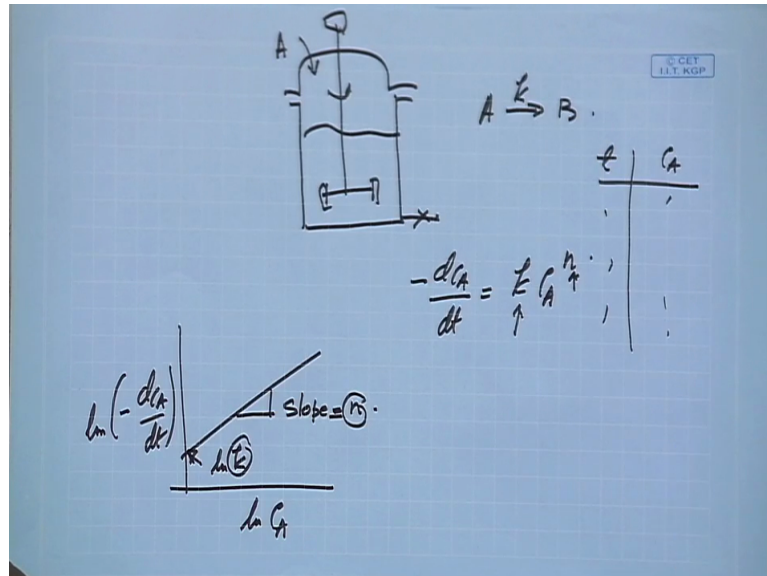
Taking exponential log both side of the equation

$$\ln\left(-\frac{dC_A}{dt}\right) = n\ln(C_A) + \ln k$$

By plotting $\ln\left(-\frac{dS}{dt}\right)$ vs $\ln(C_A)$

Slope=n, intercept= $\ln k$

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Now I am going to discuss some problems, now first problem that I want to discuss that is let us assume the reactant A decomposes in a batch reactor A to B and the composition in the A in the reactor is measured at various time with results showing in the table. Find the rate equation to represent the data, this is very simple simplest this problem that we have, what basically what I told suppose this is a reactor, we have reactor and what is the reaction we have A to B am I right.

So you take the A in the in the system A you take and let the batch process you take the material at a time, let the reaction takes place. Now at different time you draw the sample and and find out at different time what is the concentration of CA, that has been given in this problem. So you have to find out the rate equation, what is the rate equation, actually we have we have shown you this rate equation for this will be minus dCA by dt equal to k into CA to the power n, am I right. Where k is the rate constant and n is the order of reaction.

So we shall have to find out both these things, so if we want to do what we shall have to do that that we can take a log here you can see you can take a log here minus dCA by dt equal to n log minus sign I can take it here lnCA and (ln) plus lnk there I can write like this and if you plot log log graph paper. Now what we can plot this is (()) (6:25) I can I can plot ln minus dCA by dt and this is ln CA, if you do this you will get a straight line and slope this is slope will give you the value of n and and this intercept will give you the value of lnk. So you can find out the A and k value.

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t (h)	C_A (g/L)	$\frac{dC_A}{dt}$	$-\frac{dC_A}{dt}$	$\ln(-\frac{dC_A}{dt})$	$\ln(C_A)$
0	10.00				
1	9.80	-0.20	0.20	-0.61	2.28
2	9.60	-0.45	0.45	-0.80	2.26
3	8.90	-0.55	0.55	-0.60	2.18
4	8.50	-1.00	1.00	0.00	2.14
5	6.90	-1.40	1.40	0.33	1.93
6	5.50	-1.05	1.05	0.05	1.70
7	4.80	-1.15	1.15	0.14	1.57
8	3.20	-1.10	1.10	0.10	1.16
9	2.60	-0.75	0.75	-0.30	0.95
10	1.70	-0.80	0.80	-0.22	0.53
11	1.00	-0.45	0.45	-0.80	0.00
12	0.80				

The handwritten notes include a diagram of a stirred tank reactor with a stirrer and an outlet stream. To the right, the reaction $A \xrightarrow{k} B$ is shown. A table with columns h , C_A , and $-\frac{dC_A}{dt}$ is partially filled. Below the table, the differential technique is derived: $-\frac{dC_A}{dt} = \sum C_A R_A$. A graph shows $\ln(-\frac{dC_A}{dt})$ vs $\ln C_A$ with a slope of R . The final equation is $-\frac{dC_A}{dt} = \frac{C_{A_{n+1}} - C_{A_{n-1}}}{2 \Delta T}$. A note states $n \rightarrow$ Sampling no.

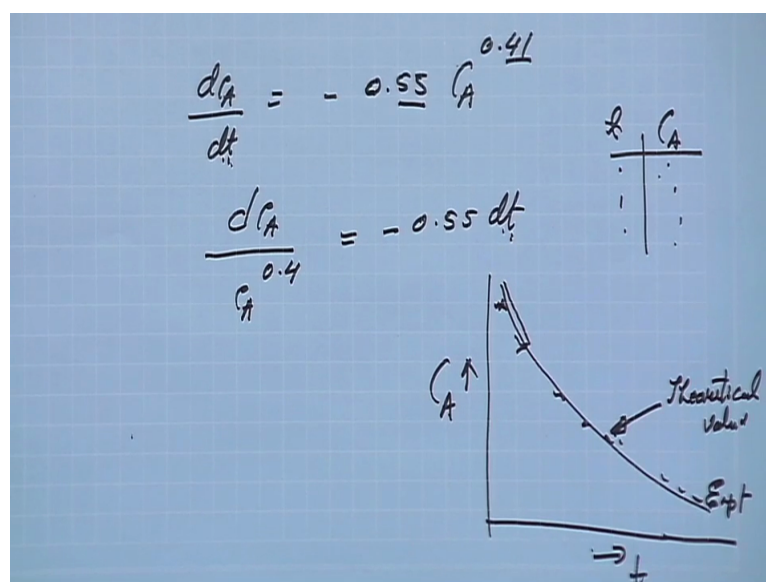
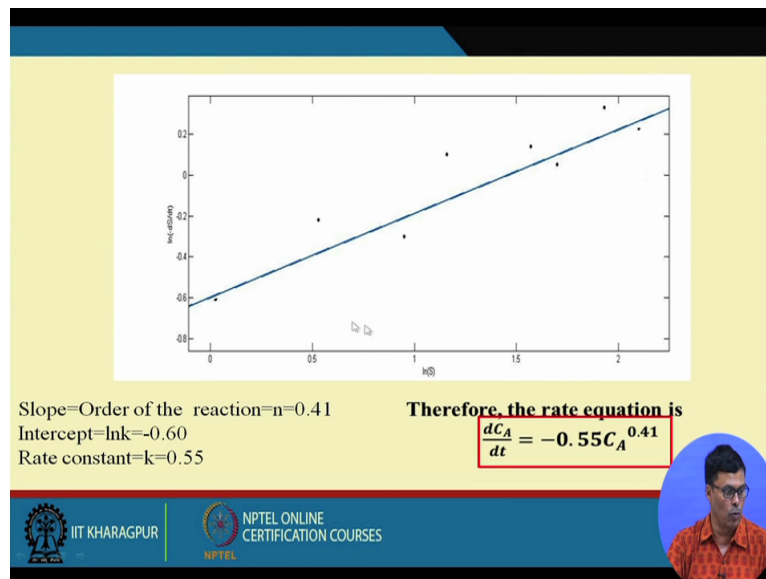
So in this problem how you will solve I can show you, so here you see that we have different C and we find out dC_A by dt . Now how you calculate the dC_A by dt let me show you, minus dC_A by dt , I can calculate like this (7:16) $C_{A_{n+1}} - C_{A_{n-1}}$ divided by $2 \Delta T$, this is called differential technique this is called differential technique, very simple what is the n is the sampling number so you have suppose here you put n and n 1, 2, 3, 4 like this you can have different numbers and this is site n you see that here $C_{A_{n+1}}$.

Now if you consider here n plus 1 means at this point if you want to calculate minus dC_A by dt , how you can calculate how you can calculate that $C_{A_{n+1}}$ that means you have to take the value here C_{A_2} , then $C_{A_{n-1}}$, that means 1 minus 1 equal to 0, so initially at the 0

(0) (8:33) whatever the concentration is there you you find out and that difference and 2T del T, what is the time difference, del T is the time difference you multiply that very simple you can do that.

So you can write this value, though this is how this table has been prepared, this is the we have this values, then we take the log value and then log CA value is given there.

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Then we can have log log graph paper, we plot this and we within we find out the value of the k value is 0.55, n value is 0.41 and so your equation is coming like this.

Now I want to add little bit here because suppose this equation is coming like this dC_A by dt equal to minus 0.55 C_A to the power 0.41, ok. So we we get the value of k, we get the value

of n. Now here this is the correlation between CA and T, so I can write this how I can write this equation dCA by CA to the power 0.41 this is equal to minus 0.55 into dt. So you can easily find out we can find out the correlation between CA.

Now we can put the value at different time we can find out the value of CA, so what you can do that this CA value we have already determined that in the (()) (10:17) system that experimental value we have this is experimental value. Now we can calculate theoretical also and we can assume the t, we can we can we can assume the value of t and we can find out the corresponding value of CA.

So these point I can I can write it here and we can find out what is the what you call theoretical value and then compare with the experimental value and try to find out the deviation and if your deviation is more than 5 percent then this equation is not valid but if it is less than 5 percent then we can (()) (11:03) this is called what you call modeling and simulation, that also I want to point out this is I can elaborate this like this.

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Problem 2:
Milk is pasteurized if it is heated to 63°C for 30 min, but if it is heated to 74°C it only needs 15 s for the same result. Find the **activation energy** of this sterilization process.

Solution:
Given data

$$t_1 = 30 \text{ min at } T_1 = 273 + 63 = 336K$$

$$t_2 = 15 \text{ min at } T_2 = 273 + 74 = 347K$$

From the Arrhenius equation


$$k = k_0 e^{-E/RT}$$

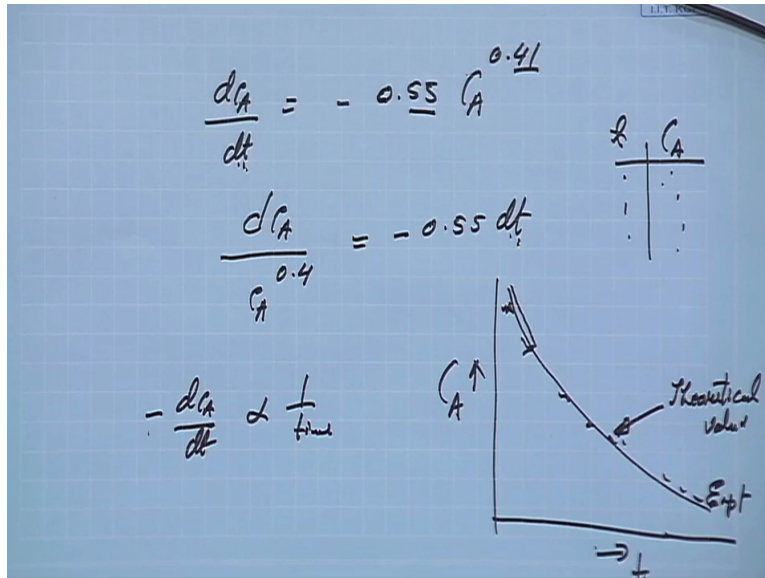
Taking exponential log both side for T_1 and T_2

$$\ln(k_1) = \ln(k_0) - \frac{E_a}{R} \left(\frac{1}{T_1} \right) \quad \dots\dots\dots (1)$$

$$\ln(k_2) = \ln(k_0) - \frac{E_a}{R} \left(\frac{1}{T_2} \right) \quad \dots\dots\dots (2)$$

It is known that **the rate of reaction ($-r_A$) \propto the reaction rate constant**
also, **the rate of reaction \propto (1/time)**





Therefore, **the reaction rate constant α (1/time)**

Equation (2) – equation (1)

$$\ln\left(\frac{k_2}{k_1}\right) = \ln\left(\frac{t_1}{t_2}\right) = \frac{E_a}{R}\left(\frac{1}{T_1} - \frac{1}{T_2}\right)$$

$$\ln\left(\frac{30}{0.25}\right) = \frac{E_a}{8.314}\left(\frac{1}{336} - \frac{1}{347}\right)$$

From which **the activation energy**

$$E_a = 422000 \frac{J}{mol}$$

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Now second problem is very interesting that milk is pasteurized if it is heated to 63 degree centigrade for 30 minutes, we know pasteurization what is pasteurization pasteurization is process through which we can remove the pathogenic organisms, ok and but if it is heated to 74 degree centigrade it only needs 15 seconds for the same results. You know that there is a technique called HTST technique what is the HTST technique high temperature short time, this is usually applicable with the industry, why because if you use the HTST technique then the quality of the product we can maintain to a great extent and what in this problem what you have to find out the activation energy of this sterilization process, very interesting that problem that we have.

So what is the data given that 30 minutes at temperature T this is the 63 degree centigrade so equivalent kelvin temperature will be 336 degree kelvin, the 15 then 15 seconds this is

mistake this is 15 seconds and this is this is will be 347 so please make the correction here and and this equation is like this k equal to $k_0 e^{-E/RT}$, what is k_0 it is (12:41) constant E is the activation energy, R is the gas constant, this is the absolute temperature.

Now I can write this equation like this and and reaction time we have already seen what is the reaction time rate of reaction minus dC_A by dt , reaction time always inversely proportional to time. If the time the time time is less than the rate of reaction should be high the inversely proportional, if the time is more that means the rate of reaction will be less. So this is the this is the so we can write $\ln k_2$ by k_1 equal to $\ln t_1$ by t_2 , E_a/R and $1/T_2$ minus $1/T_1$ by then we can find out the E_a equal to 422000 Jules per mole. So this is the activation energy of this reaction.

So this is simply how we can calculate the activation energy (13:43) chemical reaction. So we we if we anybody interested to find out the activation energy of a chemical process that you taken it will be find out if they have the data with the with the at different temperatures.

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Problem:
Liquid A decomposes by **first-order kinetics**, and in a batch reactor 50% of A is converted in a 5-minute run. How much longer would it take to reach 75% conversion?

Solution:
Given data,

$$X_{A1} = 0.50, t_1 = 5 \text{ min}$$

$$X_{A2} = 0.75, t_2 = ?$$



For **1st order reaction**

$$-r_A = -\frac{dC_A}{dt} = kC_A$$

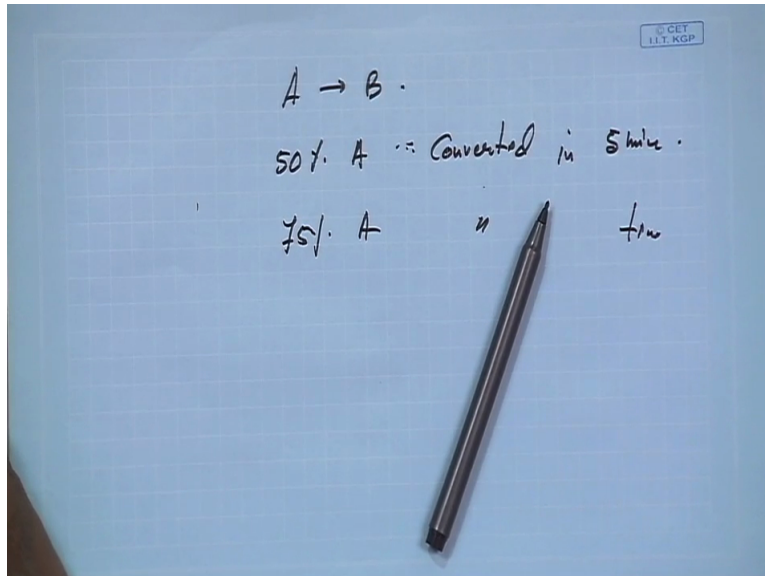
Where, $k \rightarrow$ reaction rate constant

Integrating,

$$-\int_{C_{A0}}^{C_A} \frac{dC_A}{C_A} = \int_0^t k dt$$

$$-\ln\left(\frac{C_A}{C_{A0}}\right) = kt$$



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The next problem that I have the liquid A decomposes by first-order kinetics (14:10) this is A liquid A decomposes first-order kinetics in a batch reaction 50 percent A is converted in 5 minutes run. How much how longer would it take to reach 75 percent conversion?

So the simple the reaction is the situation is something like this, so you have A to B reaction that we have so what is saying the 50 percent of A will be converted in 5 minutes, am I right. Now what the question comes that for the conversion of 75 percent of A how much time is required, ok how much time is required, ok.

So what we have done here is see that minus r_A as rightly we know that that will be minus $\frac{dC_A}{dt}$ in a k into C_A we assume this is the first-order this is already mention first-order kinetics. Now this is the this is range between C_{A0} to C_A and k into dt , this we can write $\ln C_A$ by $C_{A0} - kt$.

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Integrating,

$$-\int_{C_{A0}}^{C_A} \frac{dC_A}{C_A} = \int_0^t k dt$$
$$-\ln\left(\frac{C_A}{C_{A0}}\right) = kt$$

It is known that

$$C_A = C_{A0}(1 - X_A)$$

Now,

$$-\ln\left(\frac{C_{A0}(1 - X_A)}{C_{A0}}\right) = kt$$
$$-\ln\left(\frac{(1 - X_A)}{1}\right) = kt$$


Then then we can we have come across this equation C_A equal to $C_{A0} (1 - X_A)$ X_A is the fraction of A that is converted so we can come across this equation.

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It can be written

$$\frac{\ln(1 - X_{A2})}{\ln(1 - X_{A1})} = \frac{t_2}{t_1}$$
$$t_2 = t_1 \times \frac{\ln(1 - X_{A2})}{\ln(1 - X_{A1})}$$

Putting all the known values

$$t_2 = 5 \times \frac{\ln(1 - 0.75)}{\ln(1 - 0.50)}$$
$$t_2 = 5 \times 2$$
$$t_2 = 10 \text{ min}$$

Therefore, 75% conversion will be achieved in 10 minutes



And finally we we can write that the conversion of A this is this is the t_2 and t_1 , the two time conversion and if you take the ratio and finally we can find out the t_2 that is coming about 10 minutes. So 75 percent initially that we the question was that for (()) (16:10) conversion take place 5 mean 5 minutes 75 percent conversion take place how much time is required, answer is 10 minutes, so very simple that we have.

So we can easily calculate this that if we if we know if you can do the analysis of the system and this is very much required for our biochemical processes because there our substrate is converted into product and we are interested that to find out that how much time is required to get the desired conversion of the product that you know that is that we time to time we can find out and I have several problem that there we can find out which one is economic if we go for 99 percent conversion whether it is economic or 90 percent conversion we have some problem we have some problem we can discuss in due course and we can we can do the analysis of the process.

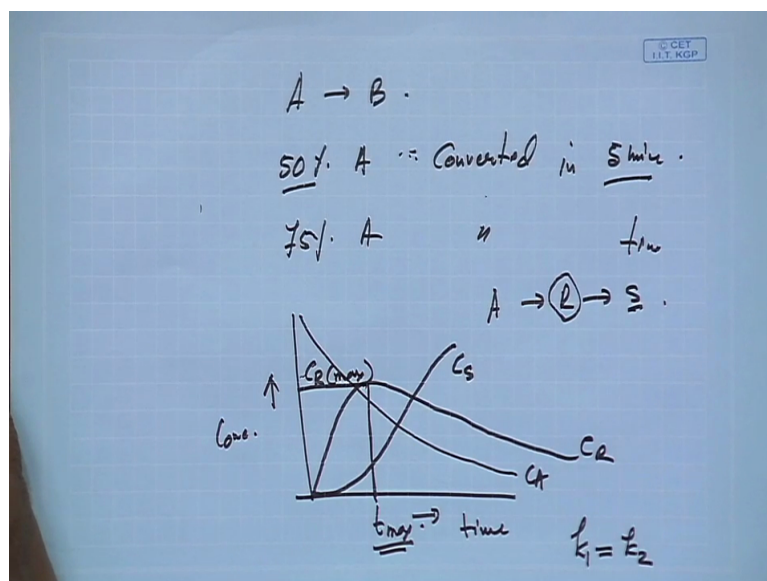
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Problem :
 For the elementary reactions in series
 $A \xrightarrow{k_1} R \xrightarrow{k_2} S$

At $t=0$ $\left\{ \begin{array}{l} C_A = C_{A0} \\ C_{R0} = C_{S0} = 0 \end{array} \right.$

Find the maximum concentration of R ($C_{R,max}$) and when it is reached (t_{max}) when $k_1 = k_2$?

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Now the last problem that I going to discuss that is the again the I told you the biological process is a chain reaction A to R and R to S, so we have two rate constant one is k1 and k2.

Now what you have to find out that at t_0 C_A equal to C_{A0} , C_R equal to C_{S0} that is the equal to 0, to find out the maximum concentration of R and when it t_{max} when k_1 equal to k_2 .

What is here what we are basically looking for that that that that we have seen in the chain reaction when you have the profile with respect to time, this is the concentration then this C_A will keep on decreasing with respect to this is A to R R to S, so this C_A will decrease with respect to time like this, then R will decrease like this, this is C_R and if you look at CS this will be like this, this is the CS, the concentration of C will be like this.

Now what we are in this problem what they are looking for that here this is the intermediate concentration of the product. Now question come at what time we can attain the maximum value this is called this is what is this is this is called C_R max and we here we call t_{max} , the t_{max} is the time at which the R the intermediate that concentration of the product that will be maximum.

So this this this problem deals with that let us and and and at the same time they mention that what will happen when k_1 equal to k_2 .

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Assignment:

The chain reaction $A \xrightarrow{k_1} R \xrightarrow{k_2} S$

The rate equations are

$$r_A = \frac{dC_A}{dt} = -k_1 C_A$$


$$r_R = \frac{dC_R}{dt} = k_1 C_A - k_2 C_R$$

$$r_S = \frac{dC_S}{dt} = k_2 C_R$$

Integrating the 1st rate equation (r_A)

$$-\ln\left(\frac{C_A}{C_{A0}}\right) = kt$$

Or,

$$C_A = C_{A0} e^{-kt}$$


$$\begin{aligned}
 -\frac{dC_A}{dt} &= k_1 C_A \\
 -\frac{dC_A}{C_A} &= k_1 \frac{dt}{t} \\
 -\int_{C_{A0}}^{C_A} \frac{dC_A}{C_A} &= k_1 \int_0^t dt \\
 -\ln \frac{C_A}{C_{A0}} &= k_1 t \\
 \frac{C_A}{C_{A0}} &= e^{-k_1 t} \\
 C_A &= C_{A0} e^{-k_1 t}
 \end{aligned}$$

Then let us see this how we have solved this problem. Now we we know the rate equation this is r_A this is the r_A equal to that dC_A by dt minus there is k_1 into C_A , r_R equal to this and this is rate of forward reaction, this is rate (forward) backward reaction and r_S equal to k_2 into C_R , that we have seen in the last class. Now here that you know that when you take the first reaction that we have already seen that minus dC_A by dt equal to k_1 into C_A , am I right.

So we can write minus dC_A by C_A equal to k_1 into dt . Now here this is equal to $d \ln C_A$ minus this is equal to k into dt , this will be what C_{A0} to C_A and this is 0 to t , k is constant. So what we can write \ln minus C_A by C_{A0} k into t , so the C_A by C_{A0} will be what will be e to the power minus kt , what will be C_A C_A equal to C_{A0} into e to the power minus k into t , so we can easily find out this is how it has it has it has it has find out here we can easily see that.

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Now, form 2nd rate equation

$$\frac{dC_R}{dt} + k_2 C_R = k_1 C_{A0} e^{-k_1 t}$$



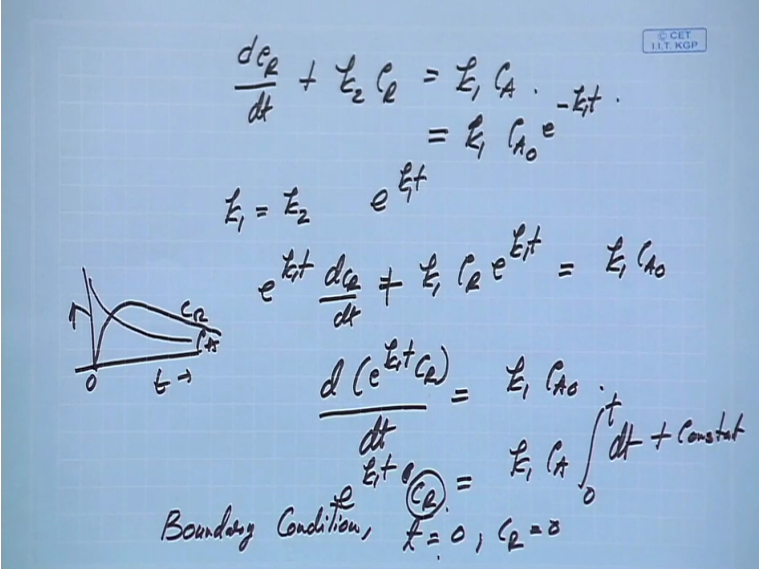
Putting $k_1 = k_2$, and multiplying both side by $e^{k_1 t}$

$$e^{k_1 t} \frac{dC_R}{dt} + k_1 C_R e^{k_1 t} = k_1 C_{A0} \times e^{k_1 t} e^{-k_1 t}$$

$$C_R e^{k_1 t} = k_1 C_{A0} \int_0^t dt + \text{constant}$$

At, $t=0, C_R = 0$ $\text{constant} = 0$

So, $C_R = k_1 C_{A0} t e^{-k_1 t}$

Handwritten derivation on a blue grid background:

$$\frac{dC_R}{dt} + k_2 C_R = k_1 C_A \cdot e^{-k_1 t}$$

$$= k_1 C_{A0} e^{-k_1 t}$$

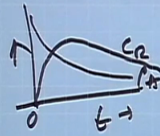
$k_1 = k_2 \quad e^{k_1 t}$

$$e^{k_1 t} \frac{dC_R}{dt} + k_1 C_R e^{k_1 t} = k_1 C_{A0}$$

$$\frac{d(e^{k_1 t} C_R)}{dt} = k_1 C_{A0}$$

$$e^{k_1 t} C_R = k_1 C_{A0} \int_0^t dt + \text{Constant}$$

Boundary Condition, $t=0, C_R=0$



And now if you if you come to the next step that we have the rate of formation of that you know that R that how this how it is so we have this equation already we have this equation how we can write that dC_R by dt plus k_2 into C_R , am I right this is equal to k_1 into C_A , this is what we have done in the last second case this is like this. Now the C_A this is $k_1 C_A$ we already we determined C_A equal to $C_{A0} e$ to the power minus $k_1 t$, ok.

Now if you multiply it both sides now here what is happening k_1 equal to k_2 k_2 equal to k_1 and multiplying both sides by by e to the power (mi) $k_1 t$, if we multiply it by this what we will what we will get we will get this equation, we will get this equation, this is e to the dC_R by dt k_1 into C_R e to the power this and this is and, now here e to the power $k_1 t$ into e to the power $k_1 t$ minus $k_1 t$ this will cancel each other this will be 1, am I right and and so this will

be what this will be nothing but this equation if you if you look at that e to the power k1t dCR by dt k1 CR e to the power k1t this is plus equal to k1 CA0 am I right, that is cancel.

Now here this is nothing but d e to the power k1t into R CR by dt this is equal to k1 into CA0, ok. Now this equation this so the what we can write now e to the power k1t into CR here CR equal to k1 CA0 0 to t this is dt plus constant, so this we can write like this.

Now now here we can put the boundary condition what is the boundary condition boundary condition is that that at t equal to 0, because we have seen that you know profile that this is like this, this is CA and this is you have CR. So here this is the 0, this is time, this is concentration. So at time t 0 I can assume CR equal to 0, this is equal to 0, and if CR equal to 0 then this will be 0, this constant will be this they will be equal to this is the k1 constant will be will be will be 0, because this is also 0, this is also 0, so constant will be 0.

So here whole equation will be what equation will be CR will be equal to I what I can write CR equal to k1 CA0t e to the power minus k1t, because I I took this the k k k k1t this side so it is minus k1t.

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If the desired product is R, have to achieve $C_{R,max}$

For $C_{R,max}$, $\frac{dC_R}{dt} = 0$ @ $t = t_{max}$




$$\frac{dC_R}{dt} = k_1 C_{A0} \{e^{-k_1 t} - e^{-k_1 t} \times k_1 t\} = 0$$

$$e^{-k_1 t} - e^{-k_1 t} \times k_1 t = 0 \quad [e^{-k_1 t} \neq 0]$$

$$t_{max} = \frac{1}{k_1}$$

$$C_{R,max} = k_1 C_{A0} e^{-k_1 t_{max}} \times t_{max}$$

$$C_{R,max} = k_1 C_{A0} e^{-k_1 \times \frac{1}{k_1}} \times \frac{1}{k_1}$$

$$C_{R,max} = \frac{C_{A0}}{e} = 0.3678 C_{A0}$$




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$$C_R = k C_{A0} t e^{-kt} \quad k_1 = k_2 = k$$

$$\frac{dC_R}{dt} = k C_{A0} (e^{-kt} - kt e^{-kt}) = 0$$

$$e^{-kt} = kt e^{-kt}$$

$$t_{max} = \frac{1}{k}$$

$$C_{R(max)} = k C_{A0} \frac{1}{k} e^{-k \cdot \frac{1}{k}} = \frac{C_{A0}}{e} = 0.3678 C_{A0}$$

Now if you come this side, then if you do the differentiation dC_R by dt how we can do this what is the two variables we have this, this and this.

So we can write k_1 k into C_{A0} I can take this and this is differentiation with respect to t this will be minus $k_1 t$ kt not $k_1 t$ because k_1 equal to I can write k_1 equal to k_2 equal to k , I can write like this, so it is $k kt$ then we have minus then what I can write that t will be there and this will be $k_1 t$ into e to the power $k_1 t$, this we can write this and this is equal to 0 because because I I if you if you if you look at here that C_R by respect to time at this at this particular when when t_{max} the C_R by dt this will be rate of formation of C_R that should be equal to 0, that will be under steady state (cond) this will be 0, under steady state condition this will be 0.

So this is the conditions so at t_{max} it will be 0, now this cannot be 0, so if this cannot be 0 I can assume this this is equal to 0, so I can write e to the power minus kt equal to k_1 into $t e$ to the power minus kt , am I right, this, this will get cancel. So I can write the t equal to 1 minus k , this we can write. So this is the this is the t_{max} value now this t_{max} value now we have the expression for already we have the expression for C_R the in the thus I can write C_R max how we can write C_R max equal to k into C_{A0} t is what 1 by k e to the power this is minus k multiplied by 1 by k , so this is this will cancel, this will be minus and this is this will cancel.

So I can write this is C_{A0} to the power e , so and e value this is equal to 0.3678 into C_{A0} . So I can easily calculate the value of C_R what is the maximum value of C_R I can easily calculate in this particular problem. So so in conclusion I want to tell that is it is possible to write the rate equations it is any any kind of rate equation we can we can easily write we can also find out rate constant we can find out the order of reaction and then we can we can because this

this is very much required to find out the correlation between the substrate concentration and the time because the because the because the any when we carry out any kind of reaction we are interested to find out at what time we have what percentage of substrate conversion takes place.

I was talking about that in the industry when we carry out any kind of reaction that naturally most of the industry we are looking for efficient process and efficient process we wanted to have higher substrate conversion efficiency. Now when you go for the higher substrate conversion efficiencies we require more time. Now question comes whether it is economic or not.

So that we shall have to find out and for that the preliminary thing that we should know that how to determine the time required for that conversion I hope this will be very useful for you for for finding out the time of (conver) time required for getting a desired conversion of any kind of chemical or biochemical process, thank you.