

Enzyme Science and Technology
Prof. Vishal Trivedi
Department of Biosciences and Bioengineering
Indian Institute of Technology, Guwahati

Module - VIII
Enzyme assay system and Kinetics
Lecture - 38
Enzyme Kinetic

Hello, everyone. This is Dr Vishal Trivedi from Department of Biosciences and Bioengineering IIT, Guwahati and what we were discussing? We were discussing about the different properties of the enzyme in the course, enzyme science and technology. And in the current module, we were discussing about how you can be able to measure the enzyme activity.

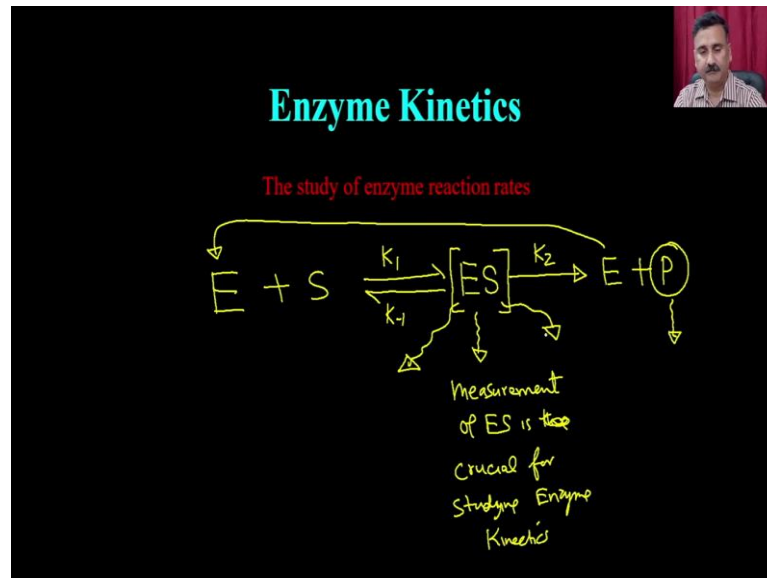
So, if you recall, we have said that or we have in fact, discussed that enzymes play crucial role in two different pathways. Either it is the anabolic pathway or the catabolic pathway. In the catabolic pathway, the enzymes are catalyzing the breakdowns of this multimeric substrates, such as starch or glycogen. And, that is how they are generating the glucose and from the glucose, it is oxidizing or degrading the glucose to carbon dioxide and water.

And, in this process, the catabolic reactions are withdrawing the energy, which is bound into the bonds and you know making the energy from these reactions. Apart from that, we also have the anabolic reactions where the enzymes are also you know synthesizing the new biomolecules. So, and both of these catabolic reactions or the anabolic reactions are very crucial for running the metabolism of the particular organisms.

Now, what we have discussed so far is that how the enzyme, you can actually be able to design the different types of assays, different types of radiometric assays, colorimetric assays, fluorometric assays and so on, and you can actually be able to measure the enzyme activity. But the question comes that how you can be able to study the enzyme kinetics or how fast an enzyme is actually forming the product?

So, in the today's lecture, we are going to discuss about the Enzyme Kinetics and how you can be able to determine the different types of enzymatic parameters and how you can be able to compare even the two different types of enzymes.

(Refer Slide Time: 03:04)



When we talk about the enzyme kinetics, the enzyme kinetics starts by the enzyme when it recognizes the substrate and it is forming the enzyme substrate complex. And, then that enzyme substrate complex, you know make the re-arrangement of the bonds and that is how the it forms the enzyme product complex. And then ultimately, since the product does not have the much affinity, it actually going to be released from the active site.

So, what we have is, we have the enzyme which is recognizing a substrate and, in this process, it is forming the enzyme substrate complex. As soon as the enzyme substrate complex is formed, it is actually going to be get fractionated into the two pathway. One, it is actually going to be fractionated that the enzyme substrate complex is going to be broken down into the enzyme and the substrate.

And, the second pathway is that the enzyme substrate complex is actually going to be form the enzyme plus product right. This product is actually was the readout when we were talking about the enzyme assays, right and while we were discussing the different types of methods to measure this enzyme assays, you can be able to say ok what is the enzymatic activity at that particular moment. But, when we talk about the enzyme kinetics, we have to see what are the different types of kinetic parameters, which are going to happen.

Now, once the enzyme is actually going to be released, if this enzyme is actually going to come back into the this state right and that is how it is actually going to participate

into the another round. And, that is how this cyclic events will continue and that is how you are going to have the large quantity of the product which is going to be accumulated.

Now, the major question is in the enzyme kinetics is that imagine that the enzyme is interacting with the substrate and it is having the rate constant of K_1 with it is which is catalyzing and then it is forming the ES. Now, when you have the breakdown of these ES, you can actually have the K_{-1} , right. And, that is actually going to denote the rate constant for the ES breakdown into the E plus S. Whereas this K_2 , this can be K_2 which is actually going to be the breakdown of or the convergent of ES into the enzyme plus product.

Now, the first and the most important question is that if you want to calculate or if you want to study the enzyme kinetics, you have to actually measure the concentration of the enzyme substrate complex, right. And, enzyme substrate complex measuring the enzyme substrate complex is the bottleneck of the enzyme is studying the enzyme kinetics, right. So, measurement of ES is the is crucial actually, right it is crucial for studying the enzyme kinetics.

Now, the question comes how you can be able to measure the enzyme substrate transition state right or enzyme substrate complex for measures because the timeline of the half-life of this particular complex is very small, right. And, that is how you cannot be able to do any kind of you know the analytical methods.

So, you cannot actually isolate this enzyme substrate complex or you cannot actually trap the enzyme-substrate complex, so that you can be able to measure, right. And, that is why if you cannot measure the enzyme-substrate complex, you have to make the different types of assumptions and different types of assumptions to measure the enzyme-substrate complex.

(Refer Slide Time: 07:34)

ENZYME KINETIC DEFINITIONS

E Enzyme; [E] enzyme concentration; [E]_T total enzyme ES
enzyme substrate complex [ES] complex concentration P, Q,
R,... "products" A, B, C ... "substrates"
I, J, K... "inhibitors"
k rate constant k₁ forward rate constant k₋₁ reverse
rate constant
k_p the catalytic rate constant.
v = reaction velocity
v₀ = initial reaction velocity, when [P] ~ 0

But, before getting to detail of these issues, let us understand that in this particular discussion what are different types of symbols we are actually going to use so that it is easier for you to follow the content. What we are going to say is when we are going to say E, it is actually going to enzyme; when we say E bracket, it is actually going to denote the enzyme concentration.

When we say E T that is the total enzyme, ok, total enzyme; when we say ES, it is actually going to say the enzyme-substrate complex. When we say ES in the bracket, it is going to called as enzyme-substrate complex concentrations. P, Q, R are the letters which are actually always being used. For denoting the products, whereas, the A, B, C can be used for the substrates.

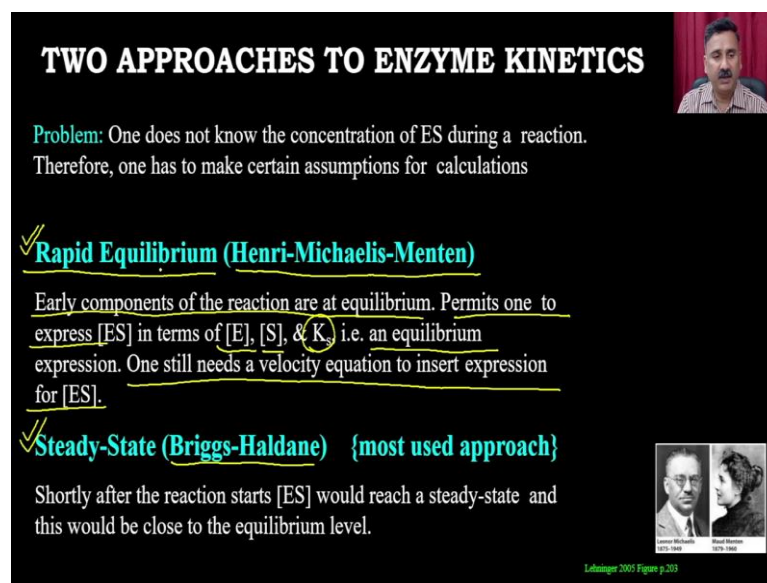
Then you can also use the I, J, K that is for the inhibitors and then you can also use the k, which is for the rate constant. k 1 is actually going to be the forward reactions. k minus 1 is actually going to be the reverse reactions. k p is actually the catalytic rate constant or the k 2. Then v is the reaction velocity and v 0 is the initial velocity when the product formation is 0.

So, after getting into the detail of these enzyme-kinetics definitions, we will come back to the same problem that you are actually going to or you are supposed to measure the enzyme-substrate complex. And, there is no way that you can be able to measure the enzyme-substrate complex concentrations because it is difficult to isolate. You cannot

have any kind of the techniques so that you can be able to isolate the enzyme-substrate complex.

And, on the other hand, the enzyme-substrate is a very, very transient, right. So, it actually going to be formed and then it is actually going to be broken down. So, that is why it is difficult to measure the accurate amount of enzyme-substrate complex. So, if we cannot measure the enzyme-substrate complex, you have to make the different types of assumptions in case you want to study the enzyme-kinetics.

(Refer Slide Time: 09:38)



TWO APPROACHES TO ENZYME KINETICS


Problem: One does not know the concentration of ES during a reaction. Therefore, one has to make certain assumptions for calculations

✓ **Rapid Equilibrium (Henri-Michaelis-Menten)**

Early components of the reaction are at equilibrium. Permits one to express [ES] in terms of [E], [S], & K_s i.e. an equilibrium expression. One still needs a velocity equation to insert expression for [ES].

✓ **Steady-State (Briggs-Haldane) {most used approach}**

Shortly after the reaction starts [ES] would reach a steady-state and this would be close to the equilibrium level.

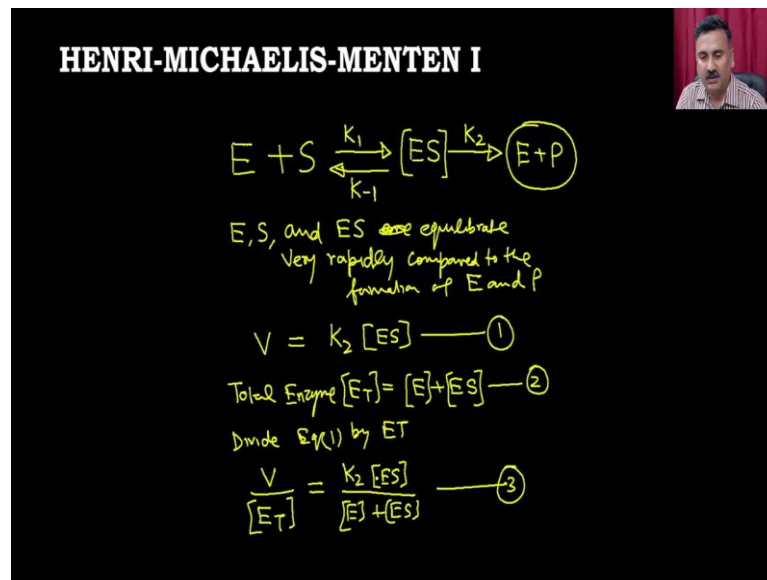


Lehninger 2005 Figure p.203

So, we have two different types of assumptions. One is called as the rapid equilibrium which is the assumption being made by the Henri-Michaelis-Menten and the second is the steady state assumptions, which is being done by the Briggs-Haldane. And, this is the latest approach. This is the older approach.

So, what is the rapid equilibrium? In the rapid equilibrium, the early components of the reactions are at equilibrium permits one to express the enzyme-substrate complex in terms of the enzyme concentration, substrate concentration and the K_s which is an equilibrium expressions. So, one still need a velocity equation to insert the expression for the enzyme-substrate complex concentrations. So, let us first discuss about the rapid equilibrium, right.

(Refer Slide Time: 10:33)



In a rapid equilibrium, what you have is you have this, right. So, enzyme is interacting with the substrate, right and then it is actually going to have the forward reaction which is going to be responsible for the formation of the enzyme-substrate complex and the rate constant for this is actually going to be k_1 .

Then this is actually going to be broken down into the enzyme plus product, right and this is going to be called as k_2 . Now, enzyme-substrate is actually going to be broken down into the enzyme and substrate, right at the equilibrium right. So, it is actually going to have a rate constant of k_{-1} .

Now, E, S and E S, so, as soon as you start the reactions in the initial time points, the E and ES are equilibrate right. So, it is actually going to have the equilibrate, very rapidly, right compared to. So, it is going to be equilibrate very rapidly, right. So, at the initial time points, it is E, S and ES are actually going to be under the equilibrium because there will be no product which is going to be formed rapidly compare to the formation of compare to the formation of E and P, right.

So, until the E and P is not being formed, the E, S and ES are actually going to be under the equilibrium. That is why the velocity of this reaction is going to be called or velocity of this reaction like the formation of the ES concentration right. So, ES formation of ES is the velocity to form the ES is actually going to be that you can actually have the k_2 and the concentration of E, S right. So, this is called as equation 1.

Now, you know that the total enzyme. So, the total enzyme E_T is. So, you have the enzyme here, you have the enzyme here. So, you can actually be able to add this, right. So, E plus ES , right. So, that is the total enzyme, but it is being present at this particular moment when the velocity is $k_2 ES$. So, if you add this enzyme question number 2.

Now, if you divide the equation 1 to by the E_T , right. So, what will happen is that it is actually going to give you the V by E_T and this is the concentration ok. So, we are talking about the total concentrations ok, and which is equivalent to the concentration of the enzyme and concentration of the enzyme-substrate complex.

So, remember that we our main objective is to calculate the concentration of the ES , right, and by doing this we are actually doing this, right. So, then it is going to be $k_2 ES$ divided by, and instead of writing the E_T , I am writing this E plus ES , right. So, it is going to be right E plus ES right, and this is the equation number 3. Now, let us move to the next step, right.

(Refer Slide Time: 14:21)

HENRI-MICHAELIS-MENTEN II

$$E + S \xrightleftharpoons[k_{-1}]{k_1} [ES] \xrightarrow{k_2} E + P$$

ES can be expressed in terms of $[S]$ $[E]$ and $[K_S]$ = dissociation constant of $[ES]$

$$K_S = [E][S] = k_{-1}$$

$$[ES] = \frac{[S][E]}{K_S} \quad \text{--- (4)}$$

$$\frac{V}{E_T} = \frac{k_2 [S] / K_S [E]}{[E] + [S] / K_S [E]} \quad \text{--- (5)}$$

So, next step is, we will write here again. So, so E plus S is k_1 right, and it is going to form the ES , and k_{-1} , and k_2 is going to be k_2 , E plus P , right. So, since the equilibrium is very rapid right, ES can be expressed. So, ES can be expressed in terms of, in terms of S , right E and K_S . K_S is the dissociation constant, K_S is the dissociation constant of ES , right.

So, you can write K_S , which is equivalent to ES , ok. Since the ES , the concentration of ES is equivalent to the S divided by K_S into E , right, ok. So, this is the going to be the equation number 4, right, and if you substitute the value of E into equation 3. So, remember the equation 3 here, right. So, this is the equation 3, right.

So, if we take this equation and put the values of the ES , this value in this equation, right, then what you are going to get is, you are going to get the V by E equal to K_2 bracket $[FL]$ S by K_S into the total enzyme configuration of E , right, divided by E plus S by K_S , sorry, K_S into E , right. And, in this the E is actually going to be cancelled out, right. So, ultimately so, this is equation number 5, ok, and in this you will see that the E is can be cancelled out from this, right, and ultimately this is going to be equation number 6.

(Refer Slide Time: 17:43)

HENRI-MICHAELIS-MENTEN III

$$\frac{V}{K_2[E]_T} = \frac{[S]/K_S}{1 + \frac{[S]}{K_S}} \quad \text{--- (6)}$$

if $V = K_p[ES]$, then $K_p[E]_T = V_{max}$ --- (7)

$$\frac{V}{V_{max}} = \frac{[S]/K_S}{1 + [S]/K_S} \quad \text{--- (8)}$$

"ES"

$$\frac{V}{V_{max}} = \frac{[S]}{K_S + [S]} \quad \text{--- (9)}$$

Now, once you have this, you can actually be able to say this, right, V is equal to V by K_2 E T , ok, which is equivalent to. So, if you cross multiply both the side by K_2 and cancelled out E on the right side, it is actually going to give you the V by K_2 by E T , that is equivalent to S divided by K_S divided by 1 plus S by K_S , ok. And, if V is equivalent to K_P into ES , right, then K_P E T is going to be the V max, ok, because the enzyme is going to be get saturated at this particular level.

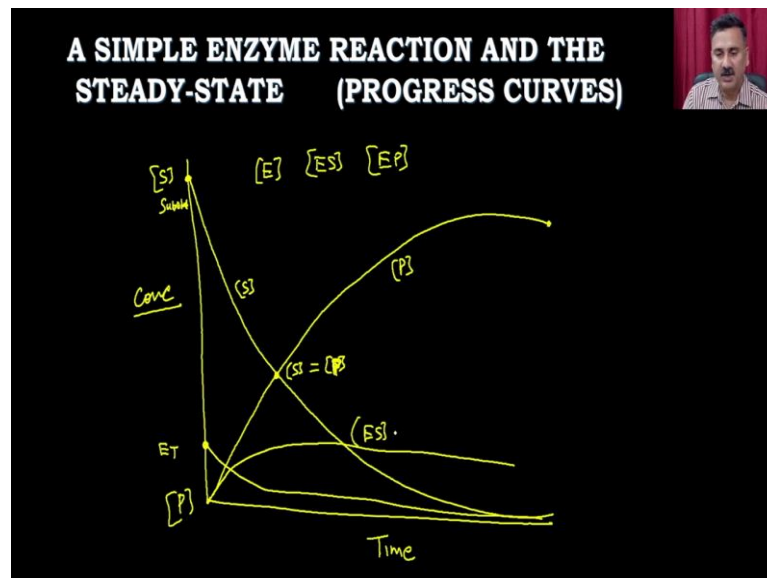
So, this is the equation number 6, this is the equation number 7. So, now, if you take the equation number 6 and 7 and you will put all these values, then it becomes V by V max equivalent to S by K_S divided by 1 plus S by K_S , ok, and if you simplify. So, this is

going to be the equation number 8 and if you simplify this, it is actually going to say that V by V_{max} is equal to S divided by $K_S + S$ and this is going to be the final equation, what you can actually be able to use and you can be able to calculate the enzyme kinetics.

Now, if this is this equation has a lot of significance because this equation can give you the many types of answers, right. Remember that in this particular equation, you can be able to still be able to calculate the enzyme velocity, you can actually do lot of calculations, but there is no term of ES .

So, so we are actually get rid of this ES term simply by expressing the ES in terms of the S , E and S , E and other kinds of parameters. Now, see how we can be able to use this equation to understand the different aspects of the enzyme kinetics.

(Refer Slide Time: 20:48)



So, if you plot, take the plot, you take the time on one angle and the concentration of the different species, right. So, if you take the concentration on this side, what will happen is that your enzyme? So, first talk about the concentration of the substrate ok. Now, substrate is going to be very high in the beginning, right and then ultimately it is actually going to come down, right, because the substrate is going to be utilized and that is how the substrate.

So, substrate concentration is going to be very high, right, whereas, it is actually going to be come down, right and ultimately it is going to be around to 0. Similarly, for the product, like if you see the product. So, at this particular time the product is going to be 0, but as you are actually going to increase, it is actually going to increase, right. So, this is here, the product is going to be the maximum and where the place you will see, this is the this is the curve of the substrate, this is the curve of the product and you see the intersection, right.

At this intersection, the concentration of the product is actually going to be equivalent to the concentration of the so, concentration of the substrate is equivalent to the concentration of the product. Let us also see how the enzyme is actually going to be get saturated, ok. So, initially you are going to start with this amount of enzyme which is actually going to be the total enzyme and it is going to be the enzyme only.

Now, as the reaction will proceed, the enzyme is actually going to be get fractionated into the 2 3, this species, it is actually going to be E, which is the plain enzyme, it is going to be ES and it is also going to be the E P, right, and you will see that the initially the enzyme is going to be the total enzyme, right, which is like this and then it is actually going to come down, right.

And, that in reduction in the enzyme is actually going to be used up in terms of the formation of the enzyme substrate complexes, right. So, this is the curve for the enzyme substrate complex, right. But, at this point the enzyme substrate formation and the conversion of the enzyme substrate into the enzyme is also going to be the same, ok. So, this is all about the simple reaction and how the modulation or the dynamics or the different types of species which are involved into the enzyme reactions are going to be change.

(Refer Slide Time: 23:45)

TWO APPROACHES TO ENZYME KINETICS



Problem: One does not know the concentration of ES during a reaction. Therefore, one has to make certain assumptions for calculations

Rapid Equilibrium (Henri-Michaelis-Menten)

Early components of the reaction are at equilibrium. Permits one to express [ES] in terms of [E], [S], & K_s , i.e. an equilibrium expression. One still needs a velocity equation to insert expression for [ES].

✓ **Steady-State (Briggs-Haldane) (most used approach)**

Shortly after the reaction starts [ES] would reach a steady-state and this would be close to the equilibrium level.



Lehninger 2005 Figure p.303

Now, let us go to the next approach, the next approach is called as the steady state Briggs-Haldane approach. So, shortly after the reaction starts when the ES is actually going to start forming, would reach a steady-state and this would close to the equilibrium level, ok. So, the steady-state assumptions are more accurate, they are actually going to give you the better picture of how the enzyme is actually going to catalyze the reactions, ok.

(Refer Slide Time: 24:16)

STE/(BRIGGS-HALDANE) I

$$E + S \xrightleftharpoons[k_{-1}]{k_1} ES \xrightarrow{k_2} E + P$$

if rate of ES from $\rightarrow E+P \gg \gg$ ES goes back to E+S

Initial Velocity

$$V = k_2 [ES] \quad \text{--- (1)}$$
$$E_T = [E] + [ES]$$

at Steady State,

Rate of ES formation = rate of ES break down

$$\frac{d[ES]}{dt} = 0$$

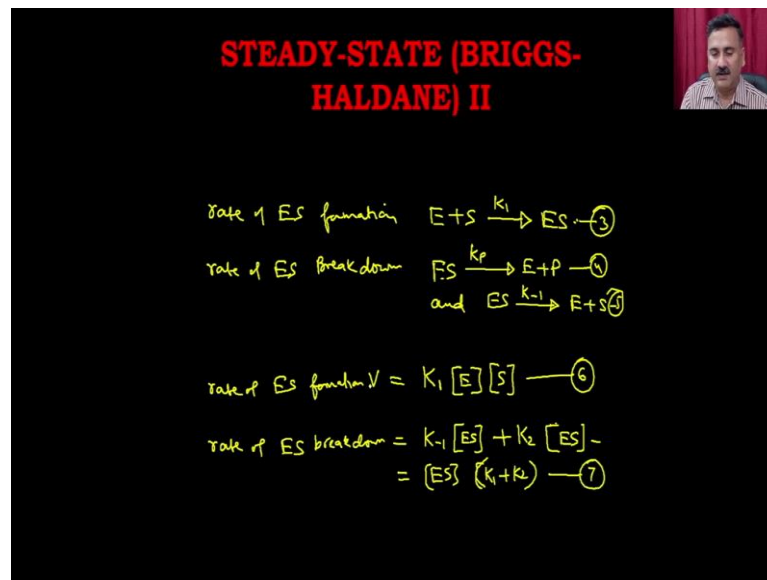
So, what happens is that we will write again the same reactions, right. So, we will write the enzyme plus substrate, then it is actually going to form the enzyme substrate complex and then it is actually going to form the enzyme plus product, right. And, then you will also have the breakdown of the enzyme substrate complex and the rate constant for this is going to be k_1 , rate constant for this one is going to be k_{-1} and this is going to be k_2 , right.

And if, now you can imagine that if the rate of ES formation, it is actually going to give you the E plus P, right, and if the E plus P is very big, then the ES can be calculated even from the ES goes back to E plus S, ok. So, if the ES formation is getting converted into the E plus P, then the ES is getting reverse, right, and it is actually going to form the E plus S.

Now, you see that the, what will be the instant velocity, ok. So, instant velocity is V , V is equal to k_2 and the concentration of ES, ok. So, this is going to be the instant velocity. Now, this is going to be the equation number 1, right, and you know that the E_T is going to be E plus ES, right. So, and you know that at the steady-state concentration, the concentration of ES is going to be the constant, right. So, at steady-state means the ES, how much ES is forming, the ES is getting breakdown, right.

So, that this means the ES is actually going to be under the equilibrium, which means the rate of ES formation is equivalent to the rate of ES breakdown, right, and this means $d[ES]/dt$ is going to be 0, which means it is not going to change, right. So, there will be no change in the rate of formation, right, and the rate of ES formation is going to be the equivalent to the rate of ES breakdown. Now, taking this into the account, you can be able to calculate or you can be able to derive the kinetic equations.

(Refer Slide Time: 27:40)



So, what will be the rate of ES formation, right? So, you know that E plus S giving rise to ES, right, that is the rate of formation, right. So, we can write. So, this is going to be the equation number. So, this is K 1, right. So, this is going to be called as equation number 3 and the rate of ES breakdown, that is going to be ES giving rise to E plus P and that is going to be calculate by the K P, right.


And, ES giving rise to E plus S and that is going to be calculated or catalyzed by the K minus 1, right. So, if you write the rate of ES formation, so, that you will write equal to K 1 and the concentration of E to the concentration of S, ok. So, this is the rate of formation, right, because you can actually have the K 1. So, this is going to be the velocity.

Then rate of ES breakdown is going to be this, and this, right. So, you can write K minus 1 ES plus K 2 ES and if you want, you can take the ES common, right. So, it becomes K 1 plus K 2. So, that is the K 1, K 2 and this is going to be. So, this is going to be the. So, this is the equation number 4, this is the equation number 5, this is going to be the equation number 6 and this is going to be the equation number 7, ok. So, we know that rate of ES formation and rate of ES breakdown, now you can just make it equal to each other, right.

(Refer Slide Time: 30:23)

STEADY-STATE (BRIGGS-HALDANE) III

rate of ES formation = rate of ES breakdown

$$k_1 [E] [S] = (k_{-1} + k_p) [ES] \quad \text{--- (8)}$$
$$[ES] = \frac{k_1 [E] [S]}{(k_{-1} + k_p)}$$
$$\frac{k_{-1} + k_p}{k_1} = K_m \quad \text{Michaelis-Menten constant}$$


So, rate of ES formation. So, add a steady state, rate of ES formation is going to be equivalent to the rate of ES breakdown, right. So, just right here, right. So, $k_1 [E] [S]$ is equal to $k_{-1} + k_p$ and rate of ES, concentration of ES, right. Now, this is going to be the equation number 8. Now, if you solve the equation number 8 for ES, right.

Then the ES is going to be the, if you solve this equation, the ES is going to be $k_1 [E] [S]$ divided by $k_{-1} + k_p$, right. Now, $k_{-1} + k_p$ upon k_1 , so, this one, right so, $k_{-1} + k_p$ divided by k_1 is going to be called as K_m or it is called as Michaelis – Menten constant, ok. This means you can actually be able to use this instead of this, right, and you can be able to calculate, right.

(Refer Slide Time: 32:26)

STEADY-STATE (BRIGGS-HALDANE) IV

$$\frac{V}{V_{max}} = \frac{[S]/K_m}{1 + \frac{[S]}{K_m}}$$
$$\frac{V}{V_{max}} = \frac{[S]}{K_m + [S]} \quad S = K_m$$
$$\frac{V}{V_{max}} = \frac{[S]}{2[S]} \quad V = \frac{V_{max}}{2}$$

So, if you put all this you will get this, ok, you will get the V by V_{max} is equal to S divided by K_m , divided by $1 + S$ by K_m , ok, or you can write like this, V by V_{max} is equal to S divided by $K_m + S$, ok, then you can bring this down and you can, if you rearrange, it is actually going to give you this, ok, and this is a very, very important equation, ok.

Now, you can imagine a situation when the S is equivalent to the level of K_m . So, if you increase the concentration of the substrate which is equivalent to the value of K_m , then what will happen? You see the V by V_{max} is equal to S and instead of K_m you can write S . So, it becomes $2S$, right, this means V is going to be $V_{max}/2$. So, if you divide this, ok, what will happen is that the V is actually going to be V_{max} by 2 .

And, that is a very, very, very important clue to calculate the value of K_m , which means if you calculate the velocity of the enzymes, wherever you will find the velocity is the velocity of V_{max} , it is actually going to give you the value of K_m and that is how it is very, very important. So, this equation is called as Michaelis – Menten equation.

(Refer Slide Time: 34:43)

SIGNIFICANCE OF K_M

Operational Definition: The substrate concentration at which the reaction velocity is half maximal, i.e. when $K_M = [S]$ then $v_o = \frac{1}{2}V_{max}$

1. It establishes an approximate value for the intracellular level of a substrate.
2. Since it is constant for a given enzyme/substrate, its numerical value provides a means of comparing enzymes from different organisms or from different tissues of the same organism, or from the same tissue at different developmental stages (V_{max} is not a constant but depends on k_p and $[E]_T$.) K_M will vary with temperature and pH.
3. K_M can be altered by ligand binding – one mode of enzyme regulation.
4. If K_M is known the assay conditions can be altered so that $[S] \gg K_M$ so that V_{max} can be determined which is a measure of $[E]_T$.
5. It indicates the relative “suitability” of alternate substrates for an enzyme. The substrate with the lowest K_M has the highest affinity for the enzyme. The “best” substrate has the highest V_{max}/K_M ratio.

$K_M = \text{Constant}$
↓
 $[E] \rightarrow [S]$

Segal Biochemical Calculations 1976 p. 218

Now, what will be the significance of the K_M into the enzyme kinetics? The substrate concentration at which, so, this is the definition of the K_M . The substrate concentration at which the reaction velocity is half of the maximal, that is the K_M is the substrate when the initial velocity is half of the velocity, maximum V_{max} , it is going to be called as K_M .

It establishes the approximate value for the intracellular level of substrate, this means if you want to attain the velocity of the half of the maximum velocity, you should have the substrate concentration which is equivalent to the K_M values. Since it is a constant for a given enzyme substrate, its numerical value provides a mean of comparing the enzyme from the different organism or the different tissue of the same organism or from the same tissue at a different developmental stages.

So, K_M is a very, very important parameter because K_M is a constant, right and it is constant for the particular enzyme substrate combination, right. So, that is why K_M is a very, very good parameter to compare the same enzyme from the different sources, same enzyme from the different organisms and even the same enzyme under the different developmental stages.

Like for example, if you talk about the lactate dehydrogenase, right. So, that LDH is an enzyme which is present in the liver, it is present in blood, it is present in the heart and other places. So, you, but the activity of the LDH is different in their different activity

right. So, you can be able to calculate the K_m of the LDH and that is actually going to give you a significance in terms of who is going to be more active and who is going to be less active because if the K_m is lower, it is actually going to be a better enzyme.

K_m can be altered by the ligand binding, which is one way of enzyme regulation, right. So, it is not like the K_m is constant, it is can be altered when you alter or when you make the modifications into the enzyme. If the K_m is known, the assay condition can be altered so that the substrate concentration is going to be above to the K_m so that the V_{max} can be determined, which is a measurement of the total enzyme.

It indicates the relative suitability of the alternate substrates for an enzyme. The substrate with the lowest K_m has the high affinity for the enzyme. The best substrate has the highest V_{max} by the K_m ratio.

(Refer Slide Time: 37:36)

CATALYTIC EFFICIENCY & TURNOVER NUMBER

Define the **catalytic constant**: $k_{cat} = V_{max}/[E]_T$

This is also known as the **turnover number** – the number of reaction processes (number of moles of substrate transformed per minute per mole of catalytic site under optimal conditions - turnovers) that each active site catalyzes per unit time (Note: some enzymes have more than one active site)

However, more complex enzymes have a more complicated expression for k_{cat} , i.e. more rate constants.

When $[S] \ll K_m$ very little ES is formed and then $[E] \approx [E]_T$

$$V_o \approx (k_c/K_m)[E]_T[S] \approx (k_{cat}/K_m)[E][S]$$

Under these conditions (k_{cat}/K_m) is a measure of the enzyme's catalytic efficiency since this apparent second order rate constant (depends on BOTH $[E]$ and $[S]$) the rate of the reaction depends on how often E and S encounter each other in solution.

Now, apart from the K_m , you also have the two more parameters which actually can be used to calculate or to compare the enzyme. One is called as the catalytic deficiency; another one is called as the turnover number. So, what is the catalytic constant? Catalytic constant the k_{cat} is called as V_{max} by the total enzyme.

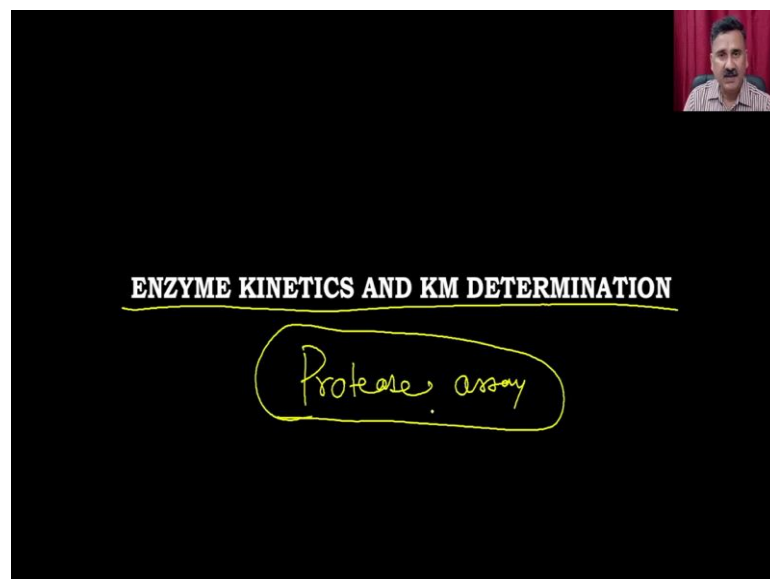
So, this is also known as the turnover number – the number of reaction processes, the number of moles of substrate transformed per minute per mole of catalytic activity, catalytic site under the optimal condition that each active site catalyzes per unit. It is

important that you should know that the enzyme may have the more than active sites and in that case the calculation has to be done accordingly.

However, more complex enzyme have a more complicated expression for the k_{cat} . When the substrate is very very low compared to the K_m , that is the very little ES is formed, then the enzyme is equivalent to the total enzyme. And in that case, it is actually going to be give you the catalytic efficiency.

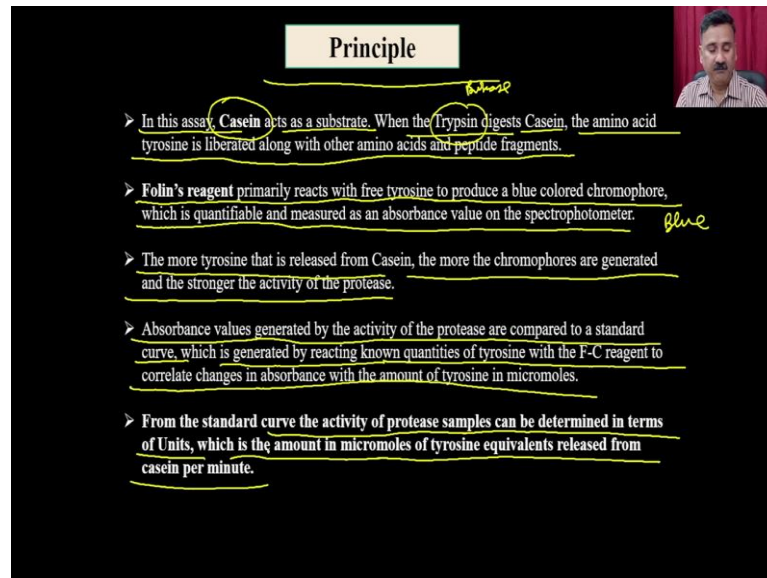
Under these conditions, the k_{cat} by K_m is a measure of the enzymes catalytic efficiency. Since this apparent second order rate constant, it depends both on the enzyme and as well as on the substrate, the rate of the reaction depends on the how often E and S encounter each other in the solution. So, both the catalytic efficiency and the turnover numbers are very, very important parameter which you can actually be able to derive from the enzyme kinetics. And, that can be used to compare the two different sources of the enzyme.

(Refer Slide Time: 39:25)



Now, let us talk about how you can be able to determine the K_m ok. So, if you want to determine the K_m of an enzyme for a particular substrate, you have to perform the enzyme assays. So, in this particular examples, what we have done is we have taken an example of a protease assay where we are actually going to you know provide the substrate to the protease and we will perform the protease assay and at the end, we are actually going to calculate the K_m of the substrate for the enzyme.

(Refer Slide Time: 40:05)



Principle

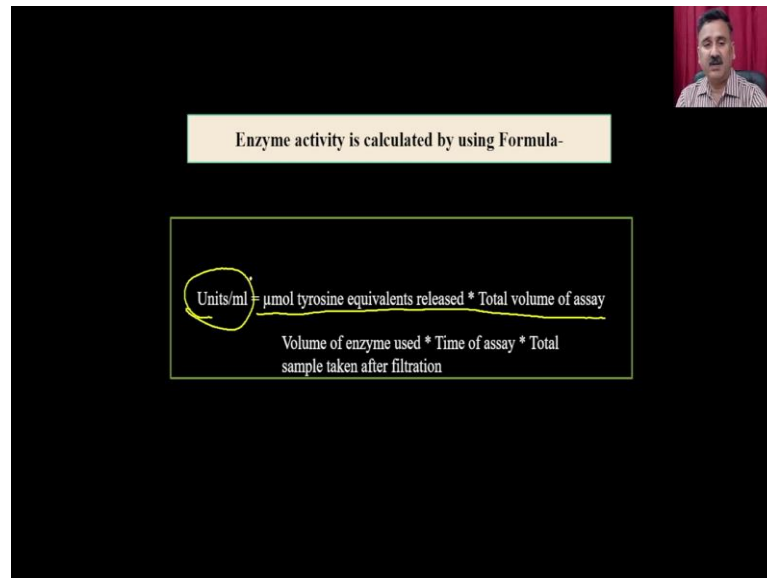
- In this assay, Casein acts as a substrate. When the Trypsin digests Casein, the amino acid tyrosine is liberated along with other amino acids and peptide fragments.
- Folin's reagent primarily reacts with free tyrosine to produce a blue colored chromophore, which is quantifiable and measured as an absorbance value on the spectrophotometer. *blue*
- The more tyrosine that is released from Casein, the more the chromophores are generated and the stronger the activity of the protease.
- Absorbance values generated by the activity of the protease are compared to a standard curve, which is generated by reacting known quantities of tyrosine with the F-C reagent to correlate changes in absorbance with the amount of tyrosine in micromoles.
- From the standard curve the activity of protease samples can be determined in terms of Units, which is the amount in micromoles of tyrosine equivalents released from casein per minute.

So, what is the principle of this particular assay? So, in this assay, the casein, which is a protein is act as a substrate. When the trypsin which is actually a protease. So, this is actually an enzyme, this is the substrate, digest the casein, the amino acid tyrosine is liberated along with the other amino acid and peptide fragment. And, then you can, since the tyrosine is being liberated, you can actually be able to use the folin's reagent to detect the free tyrosine, which has been which and it is actually going to give you the blue color reactions.

And, you can actually be able to measure that using the colorimetric assays and it is going to give you the blue color, right. Now, you can imagine that if the more tyrosine is released from the casein, the more chromophore are generated and the stronger the activity of the protease.

So, what you can do is you can calculate the absorbance values generated by the activity of the protease and compared it to the standard curve which is generated by reacting the known amount of tyrosine with the folins ciocalteu reagents to correlate the changes in the absorbance with the amount of tyrosine in the micromoles. From the standard curve, the activity of protease sample can be determined in terms of the units, which is the amount of micromoles of tyrosine equivalent released from the casein per minute.

(Refer Slide Time: 41:32)

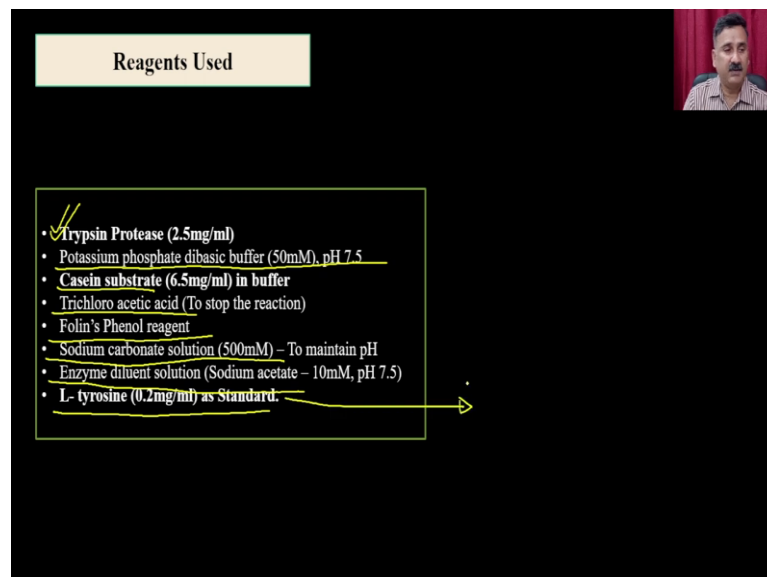


Enzyme activity is calculated by using Formula-

$$\text{Units/ml} = \frac{\mu\text{mol tyrosine equivalents released} * \text{Total volume of assay}}{\text{Volume of enzyme used} * \text{Time of assay} * \text{Total sample taken after filtration}}$$

So, the activity what you are going to determine it is actually going to be calculated in the units per ml that is the micromole of tyrosine, which is going to be released. And you can use this formula to calculate the units.

(Refer Slide Time: 41:48)



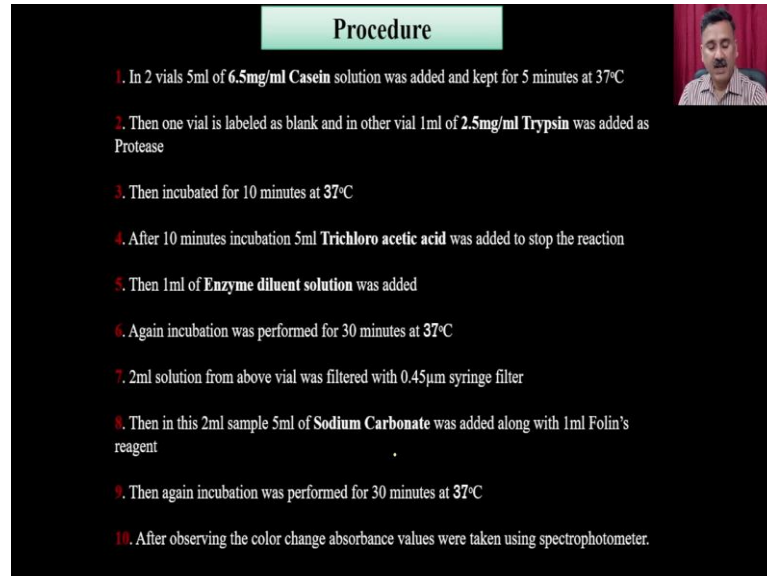
Reagents Used

- Trypsin Protease (2.5mg/ml)
- Potassium phosphate dibasic buffer (50mM), pH 7.5
- Casein substrate (6.5mg/ml) in buffer
- Trichloro acetic acid (To stop the reaction)
- Folin's Phenol reagent
- Sodium carbonate solution (500mM) – To maintain pH
- Enzyme diluent solution (Sodium acetate – 10mM, pH 7.5)
- L- tyrosine (0.2mg/ml) as Standard.

If you want to do this experiment, what are the different types of reagents are required? So, you require the trypsin which is actually the protease, you require the buffers. So, you require the phosphate buffers, you require the casein, you require the TCA, you require the folins ciocalteu reagents, you require the sodium bicarbonate, enzyme

diluents and then you also require the L tyrosine which is going to be the standard (Refer Time: 42:11) And, how you are going to perform this?

(Refer Slide Time: 42:13)

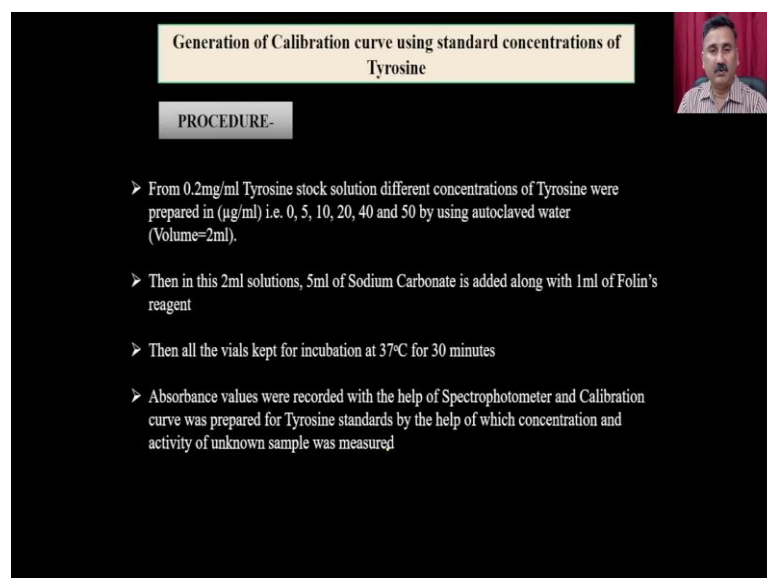


Procedure

1. In 2 vials 5ml of 6.5mg/ml Casein solution was added and kept for 5 minutes at 37°C
2. Then one vial is labeled as blank and in other vial 1ml of 2.5mg/ml Trypsin was added as Protease
3. Then incubated for 10 minutes at 37°C
4. After 10 minutes incubation 5ml Trichloro acetic acid was added to stop the reaction
5. Then 1ml of Enzyme diluent solution was added
6. Again incubation was performed for 30 minutes at 37°C
7. 2ml solution from above vial was filtered with 0.45µm syringe filter
8. Then in this 2ml sample 5ml of Sodium Carbonate was added along with 1ml Folin's reagent
9. Then again incubation was performed for 30 minutes at 37°C
10. After observing the color change absorbance values were taken using spectrophotometer.

So, you are going to follow this particular procedure. So, where you are going to incubate the casein with the enzyme and other kinds of reactions and you are going to follow this particular reactions and then ultimately you are going to have the you know the tyrosine standard curve.

(Refer Slide Time: 42:27)



Generation of Calibration curve using standard concentrations of Tyrosine

PROCEDURE-

- From 0.2mg/ml Tyrosine stock solution different concentrations of Tyrosine were prepared in (µg/ml) i.e. 0, 5, 10, 20, 40 and 50 by using autoclaved water (Volume=2ml).
- Then in this 2ml solutions, 5ml of Sodium Carbonate is added along with 1ml of Folin's reagent
- Then all the vials kept for incubation at 37°C for 30 minutes
- Absorbance values were recorded with the help of Spectrophotometer and Calibration curve was prepared for Tyrosine standards by the help of which concentration and activity of unknown sample was measured

So, you are going to run the tyrosine standard curve and that is how you can be able to calculate the amount of tyrosine which is going to be liberated. In every reactions what you are going to perform and ultimately you can be able to plot that in terms of calculating the K_m values.

(Refer Slide Time: 42:51)

Results

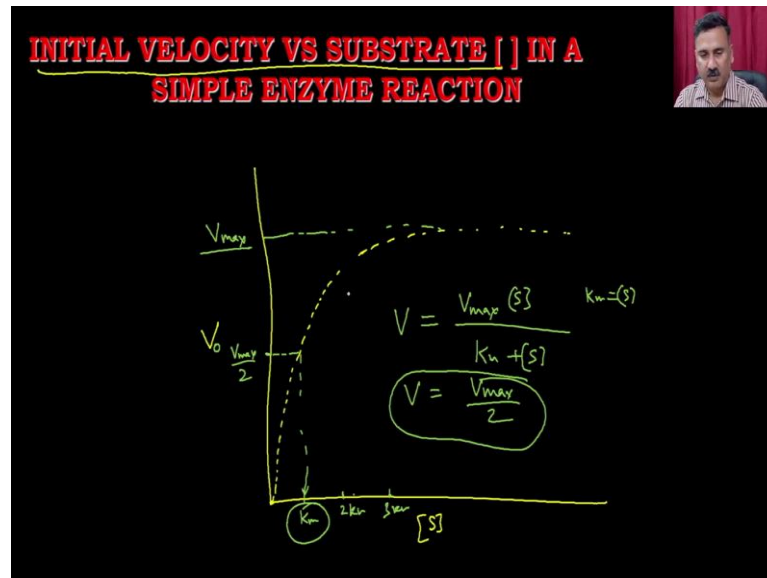
- Concentration of Tyrosine present in the sample calculated from the experiment = 32 µg/ml
- Activity of Trypsin according to the experiment performed = 0.194 units/ml.

The intensity of Blue color is directly proportional to amount of Tyrosine present in the reaction mixture which corresponds to the activity of protease being assayed i.e. Trypsin

Now, the result what you are going to get, so, the concentration of tyrosine present in the sample calculated from the experiment is going to be this and you can actually be able to use this to calculate the activity of trypsin according to this. It is actually going to be this, right.

Now, how you are going to calculate the K_m values? So, K_m actually determination of K_m by using this kind of data is having you can have the two options. One you can actually be able to do the Michaelis – Menten curve and you can be able to calculate the K_m values or you can actually be able to have the Lineweaver plot.

(Refer Slide Time: 43:25)



So, when you are actually going to plot the initial velocity versus the substrate it is actually going to give you the Michaelis-Menten curve. So, what you are going to do is you are going to do the substrate concentration on the x-axis and you are going to plot the velocity on the y-axis.

And, when you are going to do this what you are going to see is you are going to see that the initially the velocity is going to be logarithm linear and then ultimately it is actually going to form the platform, right. Because with time with increasing substrate it is not going to increase because now at this particular stage the enzymes are saturated, right.

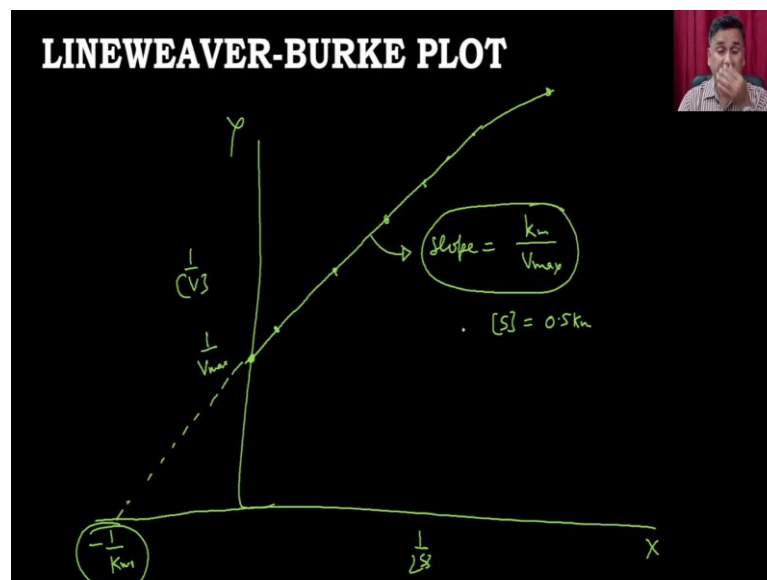
And this is actually going to give you the. So, this is actually going to give you the V_{max} ok. So, because this is the maximum what you got right. So, this is the V_{max} , right. Now, and this is the initial velocity, right, what you have plotted against the substrate concentrations, right. And, remember that this is the Michaelis-Menten curve equation right V_{max} concentration of substrate divided by K_m plus S , right and remember that is.

So, V_{max} we got the V_{max} , right and what you can do is you can just go by the half of V_{max} , right. So, this is suppose this is the half of V_{max} right. So, V_{max} by 2 and you if you go like this it is actually going to give you a concentration of the substrate and that is going to be the K_m , right. If you remember right, we have put that if you if the K_m is equal to the substrate concentration, then V is actually going to be half of V_{max} , right.

Same way you can have the 2 K_m , you can have 2 K_m , you can have 3 K_m like that ok.

And that is how you are actually reaching to a saturation point. So, this is one of the way in which you can be able to draw the Michaelis-Menten curve and you can be able to calculate the K_m values. Now, the question is that the K_m in this is actually going to be on the assumption that this is you know so, this kinetics is less reliable because of the so many issues ok. So, that is why people are now preferring that we you should also go with the Lineweaver plot.

(Refer Slide Time: 46:12)



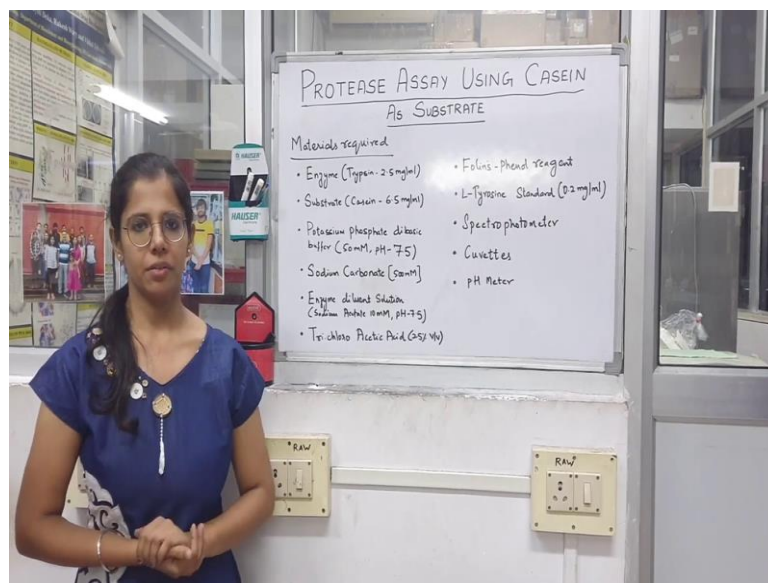
So, in a Lineweaver plot what you are doing is you are actually going to do the plotting of $1/v$ versus $1/s$, right. And in that case what you are going to do is you are going to get the curve like this ok. Because remember that in this particular curve we are actually making the assumption of V_{max} simply by going with the saturation curve, right. But, that may or may not be correct, right. So, in that case your calculation of the K_m is not going to be accurate.

And to make the things more accurate people are going with the Lineweaver plot where you are not going to have any saturation. And this is the point where it is actually hitting the y-axis is actually the $1/v_{max}$ ok and this is the $1/v_{max}$. And if you have the different time points right different concentrations right of the substrate you are actually going to have these values.

And, when you extrapolate this curve, it is actually going to hit the x-axis. So, x-axis this is the y-axis. And this is the value what you are going to get 1 by minus 1 by K_m ok and, if you take this value and you can be able to calculate the K_m values. So, if the substrate is at $0.5 K_m$ right, it is actually going to give you the maximum saturation maximum point.

Whereas for the slope you can be able to calculate the K_m by V_{max} ok and that is also very very important parameter to compare the two different types of enzymes. So, to explain you much in detail how you can be able to do the protease assay how you can be able to use that data to calculate the Michaelis-Menten constant we have prepared a small demo clip. And, in this clip the students have explained you that how you can be able to calculate the K_m from the velocity data.

(Refer Slide Time: 48:45)



Hello, everyone. This is Eena Dodwani from Malaria Research group IIT, Guwahati. Today in this video we will be performing protease assay using casein as substrate. Many other proteins can be used as substrate that is BSA, gelatin etcetera. But we will be using casein because casein is easily available and stable under storage conditions.

We are using casein as substrate and trypsin which is a serine protease whose enzyme activity is to be determined. The basic principle for this experiment is S proteases called peptide bonds. So, it is necessary to measure and compare the activity of different

proteases. Here in this experiment trypsin which is serine proteases digest, casein and releases amino acid tyrosine along with other amino acids and many peptide fragments.

Folins, phenol reagents detect free tyrosine in the reaction and give produce blue color chromophore. The more the number of tyrosine produces in the reaction, more will be the chromophores generated and more intense will be the blue color. The intensity of blue color is directly proportional to the activity of proteases.

Absorbance value obtained from the activity of proteases are compared with standard curve which is obtained with tyrosine known quantity of tyrosine reacted with folins reagent. The change in absorbance is mainly correlated with amount of tyrosine in micro moles. We can determine we can determine the activity of proteases with the help of plotted standard curve.

(Refer Slide Time: 50:17)



For the preparation of standard curve, we will be using different reagents such as potassium phosphate buffer having 50 millimolar concentration and pH 6.5; sodium carbonate buffer having 500 millimolar concentration; enzyme diluent solution that is sodium acetate buffer having concentration 10 millimolar and pH 7.5; TCA that is trichloroacetic acid 25 percent.

Folins phenol reagent and here trypsin having concentration 2.5 mg per ml which will be which we will be using as protease; L tyrosine which we will be using as standard having

concentration 0.2 mg per ml and casein having concentration 6.5 mg per ml which is our substrate.

For this experiment we have to prepare a standard curve. For this we need different concentrations of tyrosine that is 5 micrograms per ml 10, 20, 40 and 50 micrograms per ml. For the sake of simplicity, we will be preparing we will be setting one reaction of 5 micrograms per ml in which already I have added 950 micro liters of water.

(Refer Slide Time: 51:26)



Then from the stock concentration of tyrosine that is 0.2 mg per ml, we will be adding 50 micro liters of tyrosine. Then for setting the reaction sodium carbonate and folins reagent is to be added. Sodium carbonate is added to maintain pH which can be changed due to this folins reagent. So, now we will be adding 1 ml of sodium carbonate and 100 microliters of folins reagent.

Ok, now as we have set the reactions for different concentrations of tyrosine now, we will incubate it at 37 degree Celsius for 30 minutes. We have prepared different concentrations of casein as we have prepared for L tyrosine. Casein is prepared with the help of stock solution 6.5 mg per ml which is prepared in potassium phosphate buffer. Different concentrations of caseins have been prepared from 0 mg per ml to 6.5 mg per ml.

Now, for setting reaction in 6.5 mg per ml, we will be adding trypsin that is 100 micro liters of trypsin. Same amount of trypsin is added in all the eppendorfs and now, all these eppendorfs are kept for incubation for 30 minutes at 37 degree Celsius. After incubation of 30 minutes at 37 degree Celsius, now 500 microliters of trichloroacetic acid is added in the reaction.

This trichloroacetic acid is added to stop the reaction of substrate and protease. Now, 100 microliters of enzyme diluent solution is also added in the reaction. This enzyme diluent solution is added to dissolve the solid proteases and now, these all eppendorfs are kept for incubation at 37 degree Celsius for 10 minutes. After incubation of 10 minutes we have performed centrifugation at 10,000 rpm for 10 minutes in order to settle down the pellet obtained due to the protein precipitation caused by trichloroacetic acid.

Now, from this eppendorf we will collect 200 microliters of filtrate in another eppendorf tube. Now, in this tube 500 microliters of sodium carbonate is added as we have discussed previously sodium carbonate is added in order to maintain the pH change caused by folins reagent. Now, 200 microliters of folins reagent is added in all the reactions. Now, all the eppendorfs are kept for incubation at 37 degree Celsius for 30 minutes in order to develop the blue color chromophores.

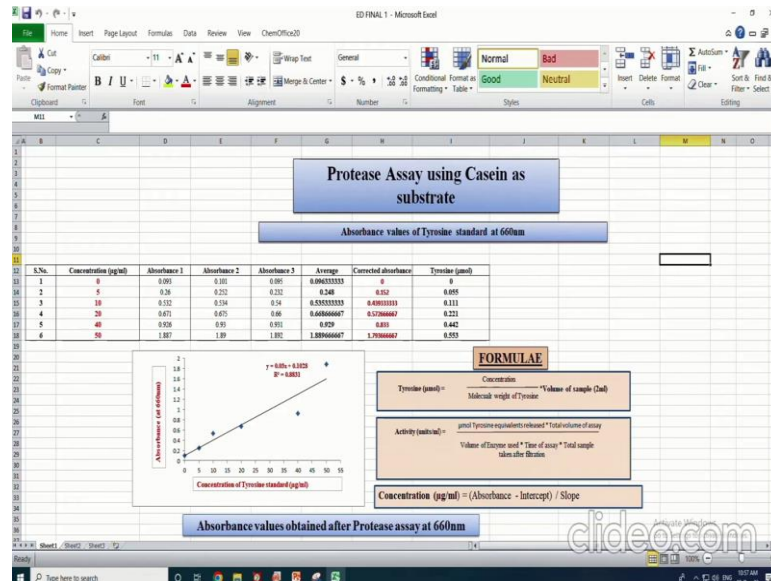
(Refer Slide Time: 55:15)



After incubating the samples for 30 minutes, we have taken readings in UV visible spectrophotometer at 660 nanometer. The now then we have observed that absorbance

values were increasing with increasing concentration as well as blue color intensity was also increasing with increasing concentrations of both standards as well as casein protease assay samples. Now, in order to in order to determine enzymatic activity of trypsin and K_m value we will plot Michaelis-Menten curve which we will be discussing further.

(Refer Slide Time: 55:49)



After completing the experiment now we are going to plot calibration curve for tyrosine standards. Here are the different concentrations of L tyrosine from 0 micrograms per ml to 50 microgram per ml. The absorbance value which were taken in triplicates at 660 nanometer in UV visible spectrophotometer are shown here. Firstly, we have calculated average of different absorbance as shown here and corrected absorbance has been calculated by subtracting absorbance of blank that is 0.096 from all other absorbance values.

Then a standard graph is plotted by taking absorbance at y-axis and concentration of tyrosine standard at x-axis. Here we are getting R square of 0.8831. Then amount of tyrosine in micromoles has been calculated by using this formula that is concentration upon molecular weight of tyrosine into volume of sample. Here molecular weight of tyrosine is 181.19 grams per mole.

(Refer Slide Time: 57:07)

S.No.	Value of Casein substrate (µg)	(µg/ml) Concentration	Absorbance 1	Absorbance 2	Absorbance 3	Average	Corrected absorbance	(µg/ml) Concentration of Tyrosine	Tyrosine (µmole)	Activity (µmole/h)
1	0	0	0.107	0.103	0.211	0.17766667	0	0	0	0
2	50	0.45	0.451	0.436	0.403	0.43	0.258	5.58666667	0.69487145	0.03348193
3	100	1.8	0.871	0.81	0.973	0.91333333	0.74333333	20.36211111	0.3392198	0.13778124
4	150	1.95	1.018	1.128	1.205	1.11833333	0.94033333	26.94444444	0.31580215	0.173771618
5	200	2.4	1.068	1.107	1.128	1.10433333	0.93433333	27.73777778	0.36627178	0.16849083
6	250	3.25	1.08	1.082	1.101	1.09233333	0.92333333	27.35777778	0.36103893	0.16610944
7	300	3.9	1.141	1.168	1.188	1.16566667	0.99566667	28.76222222	0.32886434	0.18873384
8	350	4.55	1.239	1.222	1.201	1.24833333	1.13933333	36.45111111	0.401774708	0.22152489
9	400	5.2	1.262	1.241	1.261	1.24266667	1.07366667	31.33888889	0.377225242	0.19647391
10	450	5.85	1.3	1.314	1.364	1.32566667	1.16266667	35.32888889	0.390574463	0.214701955
11	500	6.8	1.379	1.4	1.423	1.40133333	1.23133333	37.44777778	0.415668053	0.228618329

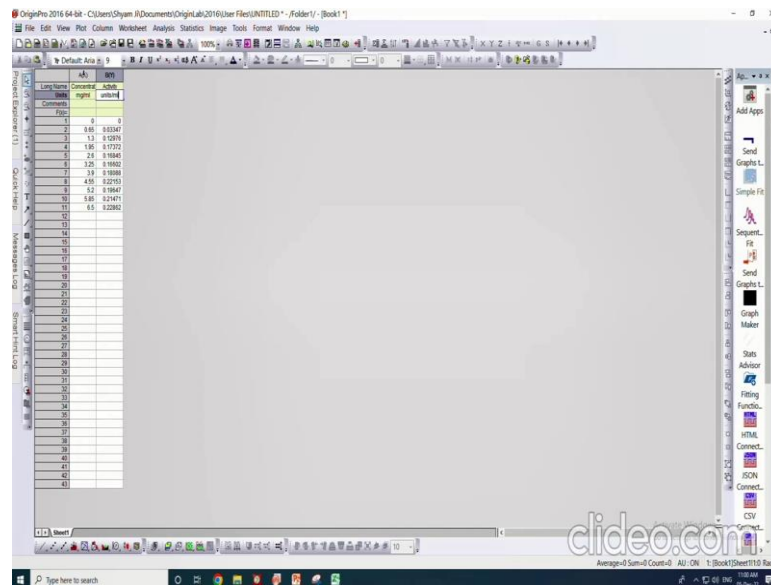
Concentration (µg/ml)	Activity (µmole/h)
0	0
0.45	0.03348193
1.8	0.13778124
1.95	0.173771618
2.4	0.16849083
3.25	0.16610944
3.9	0.18873384
4.55	0.22152489
5.2	0.19647391
5.85	0.214701955
6.8	0.228618329

Now, coming to our main experiment that is protease assay between casein and trypsin, here we have taken casein as substrate and trypsin as our protease. As after the completion of reaction tyrosine is liberated from substrate casein, to determine the concentration of liberated tyrosine we have taken absorbance values in triplicates for reaction mixture and calculated the corresponding concentration using standard curve plotted before.

The amount of tyrosine is calculated in terms of micromoles the amount of tyrosine this tyrosine is calculated in terms of micromoles by using this formula and activity of enzyme that is trypsin in units per ml has been calculated by using the formula, that is, micromoles tyrosine equivalents released into total volume of assay upon volume of enzyme used into time of assay into total sample taken after filtration.

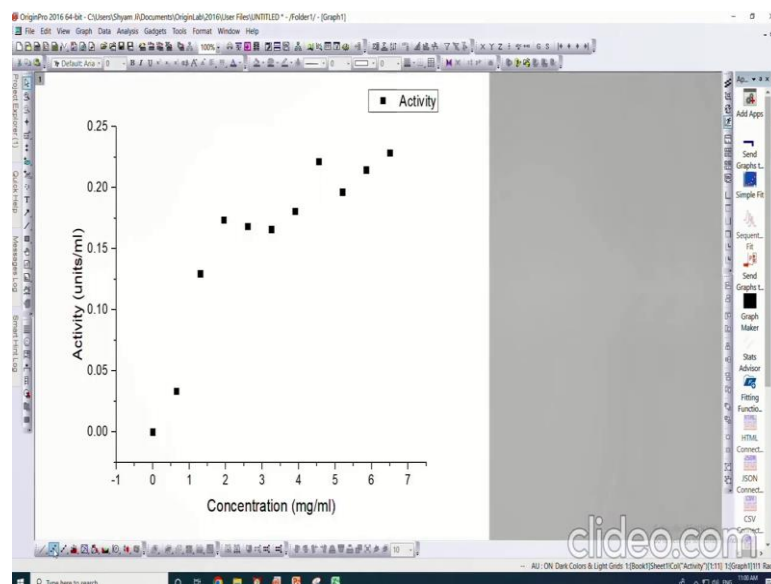
Here total volume of assay was 1.1 ml volume of enzyme used was 100 microliters; time of assay was 30 minutes and total sample taken after filtration or centrifugation was 200 microliters. Now, to plot Michaelis-Menten curve all the required parameters are summarized here. So, I am going to copy these values from here.

(Refer Slide Time: 58:43)



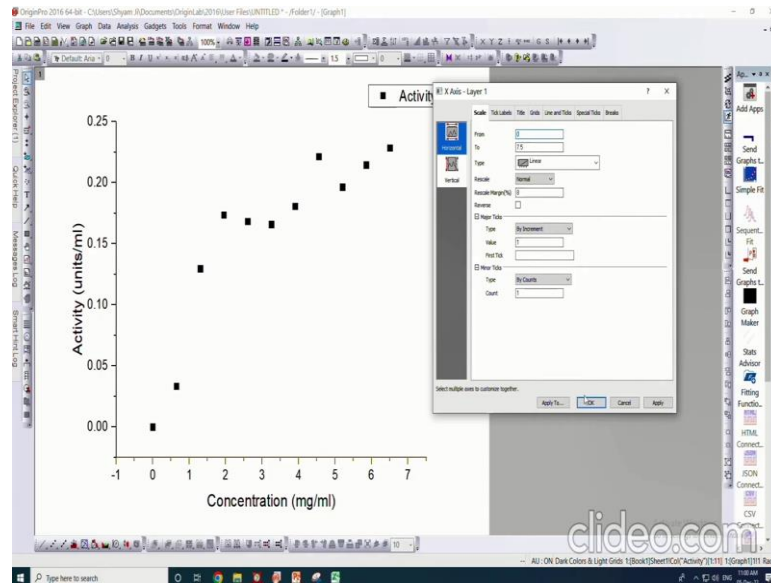
And, we will paste these values in the Origin software here we will paste these values and we will label x-axis as concentration, Concentration in mg per ml and we will label y-axis as activity, Activity in units per ml. Now, we will plot the scatter graph from here.

(Refer Slide Time: 59:29)



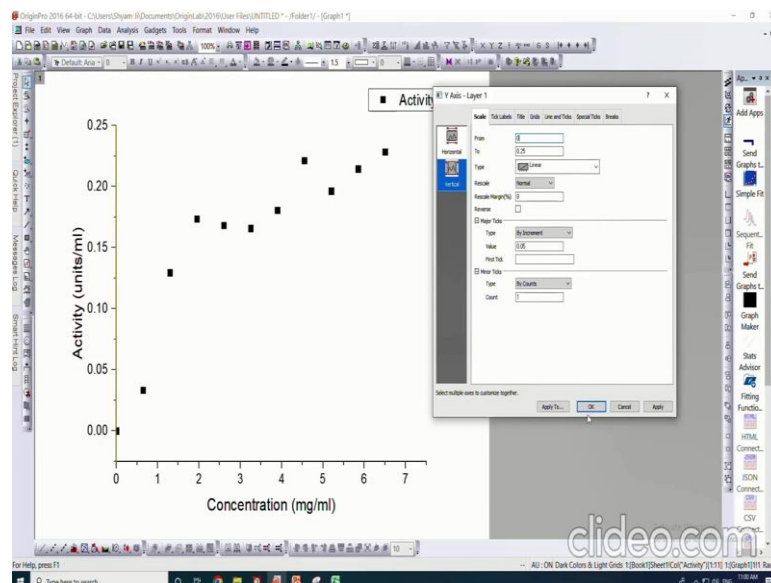
Here is this scatter graph. Firstly, scale can be corrected.

(Refer Slide Time: 59:37)

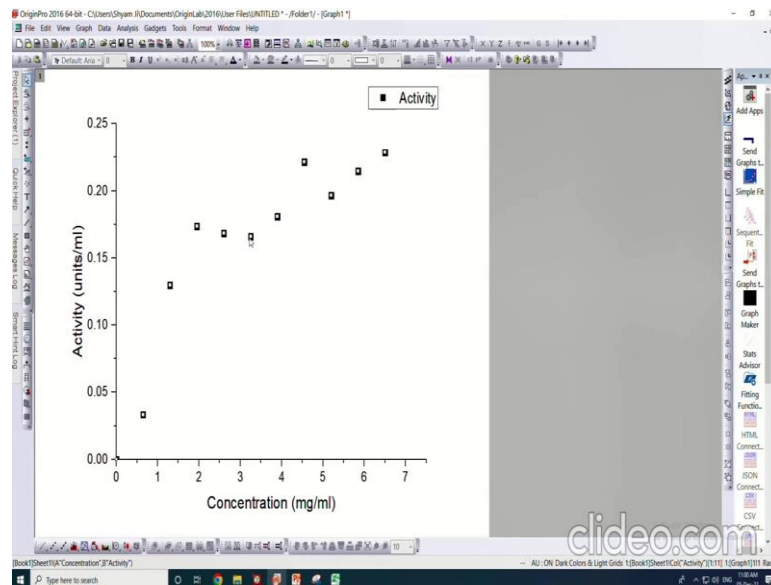


Before analysis of the graph, we will make it 0 we will do the same with y-axis also, ok.

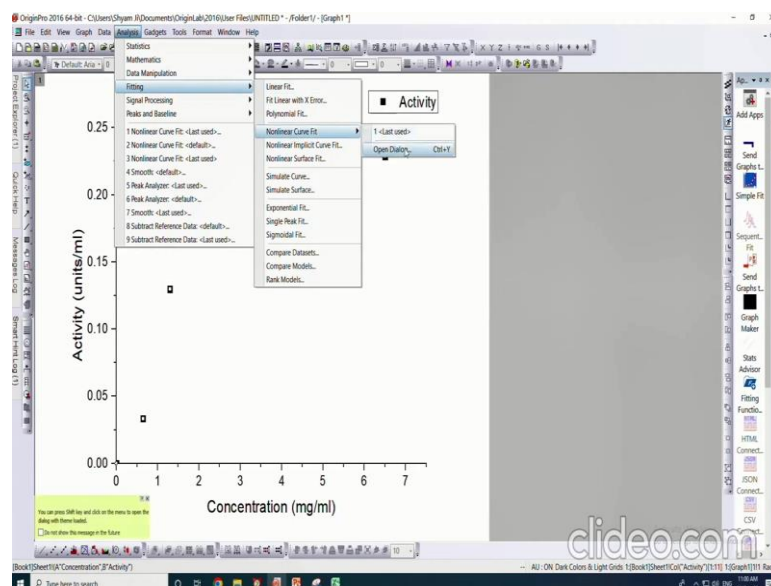
(Refer Slide Time: 59:51)



(Refer Slide Time: 59:55)

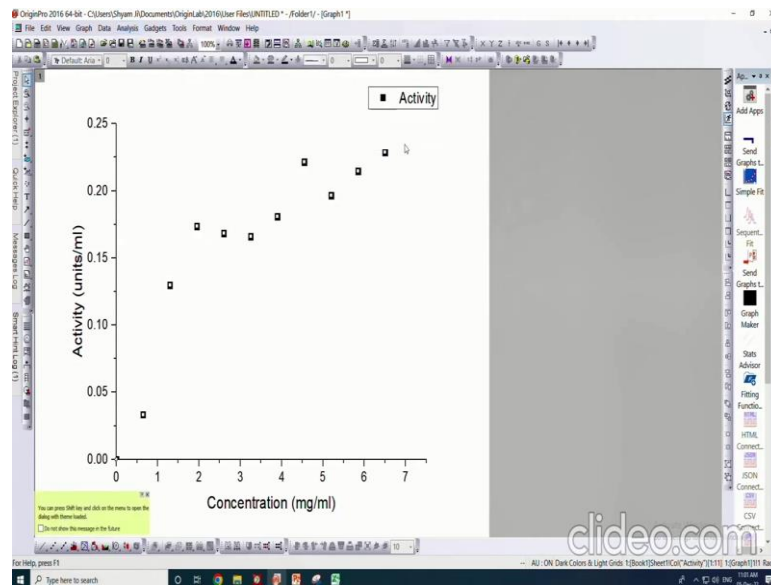


(Refer Slide Time: 60:01)

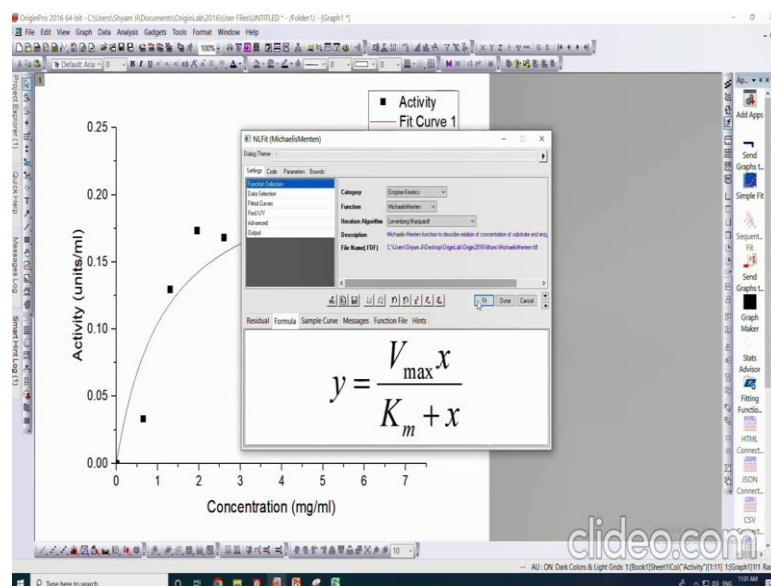


Now, for the analysis we will go to Analysis, Fitting, Nonlinear Curve Fit. A dialogue box will open.

(Refer Slide Time: 60:08)



(Refer Slide Time: 60:11)

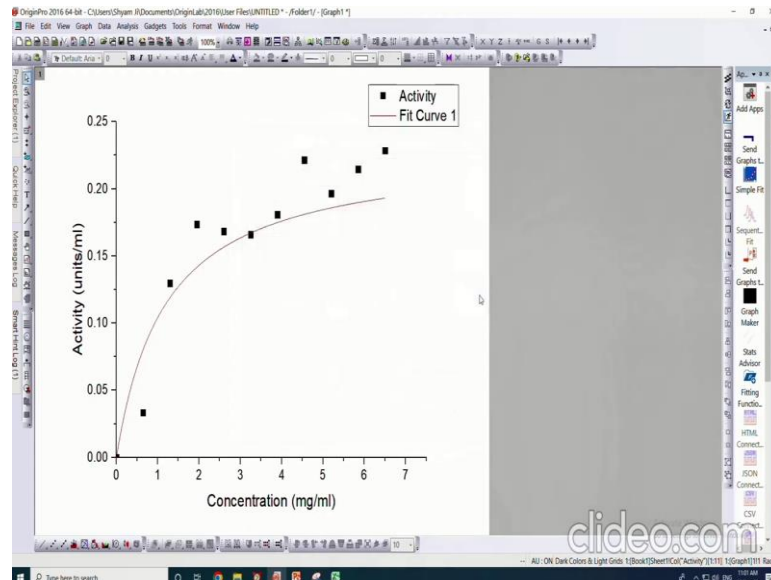


In which we have to set parameters like Category we have to set Enzyme Kinetics; Function we have to set Michaelis-Menten. This is the Michaelis-Menten equation. This is the formula for Michaelis-Menten equation that is $y = \frac{V_{\max} x}{K_m + x}$ here y is the activity of enzyme.

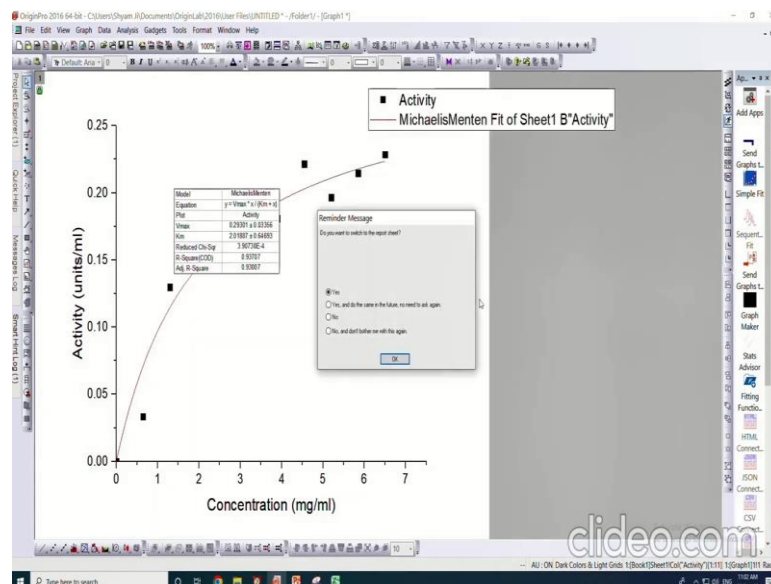
V_{\max} is the maximum activity of enzyme x stands for the substrate which is casein. In this case K_m is the Michaelis-Menten constant which denotes the affinity of enzyme for

its substrate. Theoretically, K_m is the concentration of substrate at which enzyme activity is half of maximum.

(Refer Slide Time: 61:06)

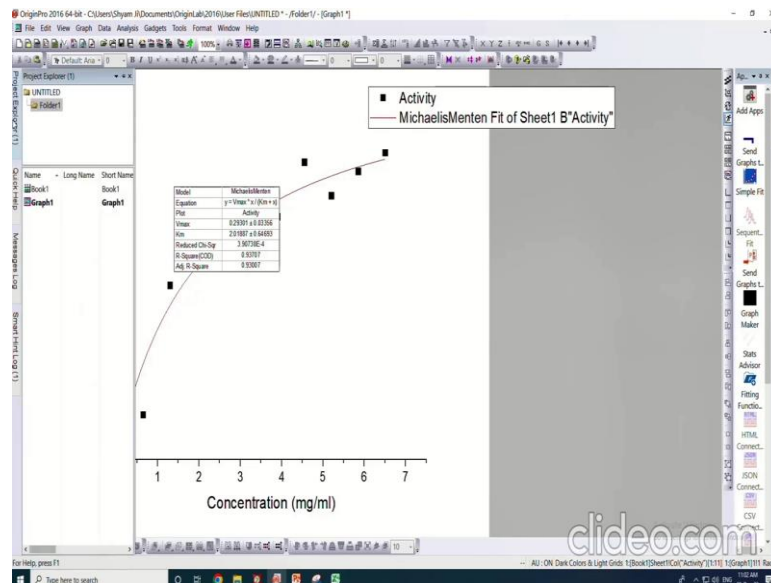


(Refer Slide Time: 61:07)



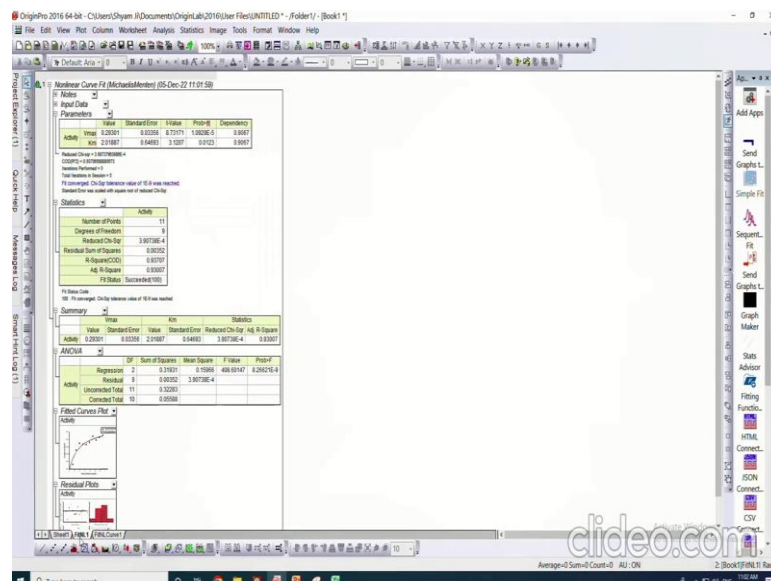
Now, we will Fit this. This dialogue box shows the V_{max} value of 0.2 and K_m of 2.0.

(Refer Slide Time: 61:20)



Now, we will open another dialogue box by clicking this Book1, ok.

(Refer Slide Time: 61:30)



This dialogue box tells us about accuracy of the curve fitting. From here we can say that Fit Status is 100 percent Succeeded that is and R square is 0.93 and as we have seen before K m is 2.0 and V max is 0.2. So, by the help of this protease assay we concluded that this protocol will enable enzyme activity of any unknown protease. In addition, this assay is useful for ensuring that proteases have precisely determined activity before using them for further experiments. Thank you.

So, with this I would like to conclude my lecture here. In our in this particular lecture we have discussed about the different aspect of the enzyme kinetics. We have discussed about the Michaelis-Menten approach and we have also discussed about the Briggs-Haldane approach, how you can be able to express the consideration of the enzyme substrate complex and how you can be able to use that for deriving the different types of kinetic parameters.

At the end we have also discussed about how you can be able to determine the K_m values from the given data and how you can be able to use and what will be the significance of the K_m in the enzyme kinetics. So, with this I would like to conclude my lecture here. In our subsequent lecture, we are going to discuss some more aspects of the enzymes in this particular course.

Thank you.