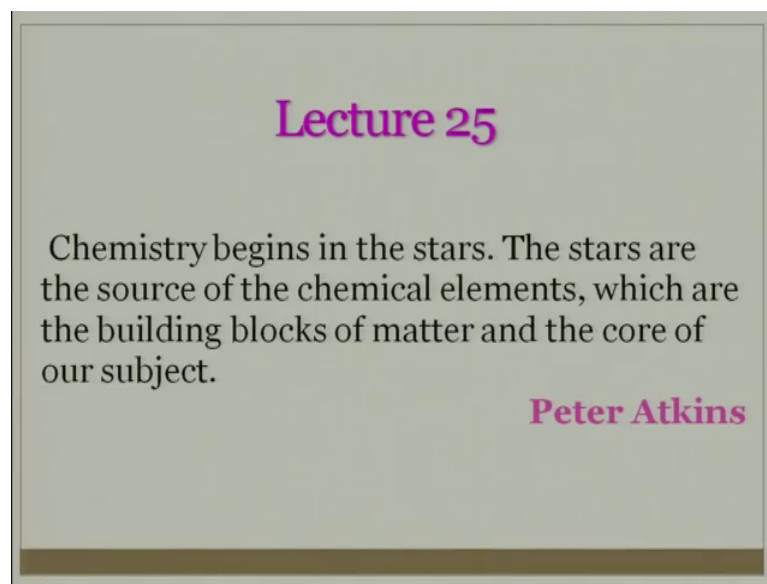


Fundamentals Of Combustion (Part 1)
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Lecture - 25
First order, Second order and Third-order reactions

Let us start this lecture with the third process from the Peter Atkins chemistry begins in the stars.

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The stars are the source of the chemical elements, which are the building blocks of matter and the core of our subject. So, that is his belief, but of course, one can question it, that one um, let us, you know if you recall that in the last lecture. We talked about arenius form of reactions and then it is limitation. And keep in mind that you should not use that for a very long range of temperature; however, the temperature range is not too long. You can use it and we have seen how we can evaluate the activation energy provided. You know the specific reaction rate constant at two different temperature.

Generally, people use of course the several of temperature and then, put a curve fitting and then do that right. It is not that they will take two points and then calculate no first. They will calculate the data and then they will calculate what will be the activation energy provided. It is linear in nature and if it is not little bit deviation, they will make it linear. So, now, let us look at, you know elementary reactions.

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Elementary Reactions

If the reaction occurs successfully at molecular level, the reaction is termed as elementary.

$$\text{OH} + \text{H}_2 \rightarrow \text{H}_2\text{O} + \text{H}$$

Molecularity:
Number of molecules/atoms participating in each reaction leading to product.

1. Unimolecular reaction ($\text{N}_2\text{O}_5 \rightarrow \text{N}_2\text{O}_4 + 0.5 \text{O}_2$)
2. Bimolecular reaction ($\text{CO}_2 + \text{H}_2 \rightarrow \text{H}_2\text{O} + \text{CO}$)
3. Trimolecular reaction ($\text{CO} + \text{O} + \text{M} \rightarrow \text{CO}_2 + \text{M}$)

Order of Reaction: For elementary reaction: molecularity ≤ 3
Number of molecules or atoms whose concentration would determine the reaction rate.

$$\text{N}_2\text{O}_5 \xrightarrow{k_f} \text{N}_2\text{O}_4 + 0.5 \text{O}_2$$

$$\frac{dC_{\text{N}_2\text{O}_5}}{dt} = -k_f C_{\text{N}_2\text{O}_5}$$

Order of reaction = 1
Molecularity = 1.

Because in case of elementary reactions, the reaction occurs at a molecular level right and we are taking an example O H is reacting with hydrogen and leading to water and H and keep in mind that H is a radical and O H also radical and we have seen that molecularity. We have discussed earlier, but I want to again discuss these things and, because, you know is important to learn, what is difference between the molecularity and the order of reaction.

So, in molecularity basically, number of molecules are atom that participate in each reaction leading to a product right and let us consider some of the you know, reactions, which is unimolecular and then like for example, N_2O_5 is the composite, N_2O_4 and oxygen, in this case, the reaction. The molecularity is for this reaction is only one that is why, we call it as a unimolecular reaction and bimolecular reactions, if you consider CO_2 is reacting with the hydrogen going to water and carbon monoxide, the two molecules are participating, leading to a product. So, therefore, we are calling it as a bimolecular, trimolecular of course, three molecule will be, reacting to getting into product right. In this case carbon monoxide is reacting with O, with third body, which is not participating, but; however, without that reaction may not occur and that is CO_2 plus M, right.

And keep in mind that for elementary reaction right, and these are, not really elementary reaction, this is the elementary reactions. For elementary reaction, what will be the, you know molecularity. For example, this is like, in this elementary reaction two molecules

are reacting. So, therefore, molecularity will be 2. So, can I have a, elementary reaction, where molecularity will be 5 or 4.

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So, generally it is not true. Generally, for elementary reaction molecularity will be always less than equal to 3 ok. Beyond that, it is not possible for elementary reaction whereas, for you know global reactions, which is hypothetical reactions that I mean theoretic, I mean like what we assume there, you can have right. So, whereas, order of reactions talk about the, you know will be different than the molecularity, because that will tell you that whether the reaction rate will be dependent on the concentration and the what is it is power right, coefficients right, power.

For example, if I consider this N_2O_5 leading to N_2O_4 and half O_2 , in this case reaction rate. What it would be? It would be the, the change in concentrate N_2O_5 divide by dt is equal to minus k f N_2O_5 , if I say this is your k f right that means. In this case, order of reaction will be one right, order of reaction right. Order of reaction will be 1 and molecularity is also 1 right. So, but molecularity need not to be order of reaction, for all the reaction, for you know reaction that might be, this is a one example, where it is looks to be same, but need not to be same all the time.

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First Order Reaction

Consider the first order reaction,

$$\text{H}_2 \xrightarrow{k_f} 2\text{H}$$

Reaction rate,

$$-\frac{dC_{\text{H}_2}}{dt} = k_f C_{\text{H}_2} = \frac{1}{2} \frac{dC_{\text{H}}}{dt}$$

Separating the variables and integrating,

$$-\ln C_{\text{H}_2} \Big|_{t=0}^{t=t} = k_f (t - 0)$$

At $t=0$, $C_{\text{H}_2} = C_{\text{H}_2,0} \rightarrow -\ln C_{\text{H}_2,0} = k_f t + C$

$$\ln \left(\frac{C_{\text{H}_2,0}}{C_{\text{H}_2,t}} \right) = k_f t \Rightarrow C = \ln C_{\text{H}_2,0}$$

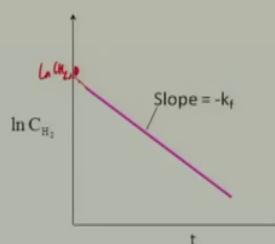
First order combustion reactions !

$\text{O}_2 \xrightarrow{k_f} 2\text{O} - \text{unimolecular}$

$\frac{dC_{\text{O}_2}}{dt} = -k_f C_{\text{O}_2}$

Note: H_2 concentration decreases exponentially with time ,
 All unimolecular reactions obey first order kinetics !
 All first order reactions need not to be unimolecular !!

1st order Reaction

$$\text{A} + \text{B} \xrightarrow{k_f} \text{C} + \text{D} \quad -\frac{dC_{\text{A}}}{dt} = k_f C_{\text{A}} C_{\text{B}} \approx k_f C_{\text{A}} \quad C_{\text{B}} \gg C_{\text{A}}$$


So, let us consider the first order reaction, as we have already seen that O_2 is reaction with $2O$ right and in this case, the what will be BC , if I take BC O_2 by dt . If I say this is k_f is equal to minus $k_f C_{O_2}$ right. So, this is basically first order reactions. So, similarly you can consider H_2 going into the $2H$, which is then the reaction rate will be dCH_2 divide by d, t is equal to $k_f dH_2$ and that also you can write on equal to half dCH by dt right. And keep in mind, this is being consumed. Therefore, there is negative sign and BH is being produced therefore, this a positive sign right.

And if I consider this portion only right, what I can write down right, I can integrate that and separating the variable. I can write down dCH_2 by C_{H_2} is equal nothing, but $k_f dt$ and I will integrate this thing 0 to t time here, right ok. So, I will get $\ln CH_2$, t is equal to 0 to t and $k_f t$ at, this thing then, I can, what you call, get a relationship $\ln CH_2$ O divide by $\ln CH_2$, $k_f t$ keep in mind that plus there will be a constant right ok.

So, in this case, if you look at this will be minus $\ln C_{H_2}$ is equal $t k_f$ plus is equal to constant right, right at t is equal to 0 , at t is equal to 0 . What it will be CH_2 will be nothing, but CH_2 comma right at the initial state right. So, therefore, the constant is coming. So, if I will apply this one then this is nothing, but your CH_2 at this condition, this will be $CH_2 O$. So, and this will be t right, this will be t , t is nothing, but 0 right, at t is equal to 0 . This I am talking about then simply C is equal to $\ln CH_2$ at 0 , this will be little capital right. So, from that, you can get $\ln CH_2 O$ divide by CH_2 at time t is equal to nothing, but $k_f t$ right.

Now, if you plot this thing, you will get basically, slope that is the minus k_f right and that time is equal to t , what is this value? This is nothing, but your corresponding to $\ln CH_2$ naught at time t right and as it goes the time, this is being reduce kind of things. So, you can get basically, you know how does the hydrogen, you know concentration changing with respect to time, you can, find it out very easily, if it is a first order reaction keep in mind that in this case the hydrogen concentration decreases exponentially with time.

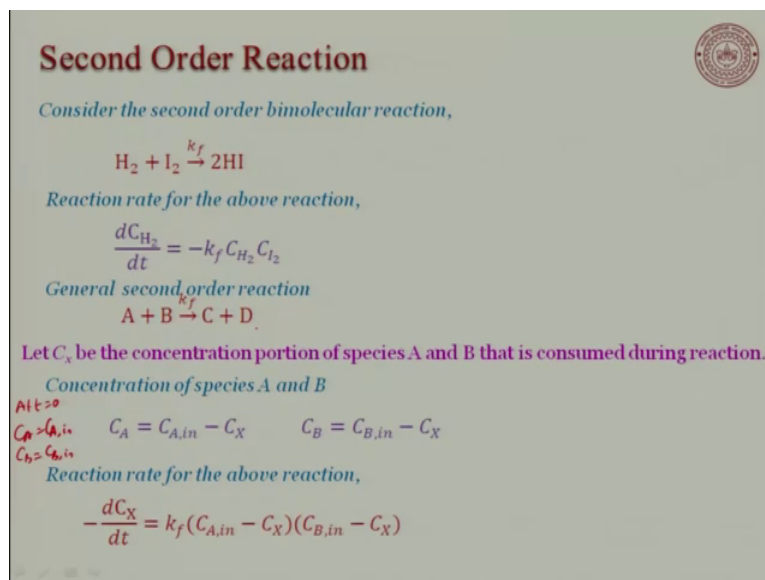
Of course, this is plot in $\ln$, but if I plot CH_2 . So, it will be very clear, it will be exponentially. You know, changing or decreasing with time. All unimolecular reactions obey the first order kinetics right. For example, this a unimolecular oxygen going to the O_2 right. This is a unimolecular reaction.

But all first order reaction need not to be unimolecular there might be a two molecules will be participating, but; however, there might be a situation where some, reaction will be first order in nature right. So, now, and that will be occurring particularly, when the one molecule concentration is too large to be changing with respect to time then you can have for example, if I say A is reacting with B going to C plus D right.

If I say, this is k_f I can write down dC_A by dt minus is equal to $k_f C_A$ and C_B right. So, if C_B is too large right, it is not really changing with respect to time, then this will be nothing, but your k_f right of course, this will be, you know C_A . So, although this is basically, kind of 2 molecules are there and then this will be, but it will be only constant with k_f 1 I can say.

So, therefore, this is A and that is possible will be C_B is very-very greater than C_A . So, therefore, it will be unimolecular reaction. In this case molecular rate is, what basically two right, but; however, the order of reaction is 1 order of reaction will be 1, first order reaction, but the molecularity in this case is 2.

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Second Order Reaction

Consider the second order bimolecular reaction,

$$H_2 + I_2 \xrightarrow{k_f} 2HI$$

Reaction rate for the above reaction,

$$\frac{dC_{H_2}}{dt} = -k_f C_{H_2} C_{I_2}$$

General second order reaction

$$A + B \xrightarrow{k_f} C + D$$

Let C_X be the concentration portion of species A and B that is consumed during reaction.

Concentration of species A and B

At $t=0$
 $C_A = C_{A,in}$
 $C_B = C_{B,in}$

At time t ,
 $C_A = C_{A,in} - C_X$ $C_B = C_{B,in} - C_X$

Reaction rate for the above reaction,

$$-\frac{dC_X}{dt} = k_f (C_{A,in} - C_X)(C_{B,in} - C_X)$$

So, now let us look at second order reactions right, let us say that hydrogen is reacting with a iodine and going to hydrogen iodide 2, hydrogen iodide and reaction rate, if you look at this, is nothing, but dC_{H_2} dt is equal to minus $k_f C_{H_2} C_{I_2}$ and if I write down general second order reaction, we can look at A plus B going to the C and D with reaction rate. You know specific reaction k_f , this is a forward reaction. So, concentration

of species right so, if you look at this, this is basically reaction rate will be dC_A by dt minus will be $k_f C_A C_B$ right.

Let us assume that C_X , you know is the things, which is changing with respect to time of the concentration of A and B then C_A of concentration will be C at initial. When C_A is basically at t is equal to 0 C_A will be $C_{A, \text{initial}}$ right and similarly, C_B will be $C_{B, \text{initial}}$ and then that is C_B will be $C_{B, \text{initial}}$ minus C_X . C_X is what the concentration, which is changing with respect to time right and that C_B is, C_A is basically a $C_{A, \text{initial}}$ minus C_X .

All the time C_X is changing right, but C_A is initial constant, then C_A is basically changing with respect to time and keep in mind here, we are considering for the simplicity, say that both C_A and C_B is changing with the same concentration, but need not be true all the case right, but in this case, we are taking, because to make it little simplify, the thing reaction rate, above this constant will be dC_X by dt right is nothing, but your dC_A in minus C_X into $k_b dC_X$ by this thing right, because we are saying that how it changing like this is nothing, but if you look at this is I can write down as X right changing.

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Multiplying both sides by $(C_{B, \text{initial}} - C_{A, \text{initial}})$, $-\frac{dC_X}{dt} = k_f (C_{A, \text{initial}} - C_X) / (C_{B, \text{initial}} - C_X)$

$$\Rightarrow \frac{-dC_X (C_{B, \text{initial}} - C_{A, \text{initial}})}{(C_{A, \text{initial}} - C_X)(C_{B, \text{initial}} - C_X)} = k_f dt$$

Integrating,

$$-\int \left(\frac{1}{(C_{A, \text{initial}} - C_X)} - \frac{1}{(C_{B, \text{initial}} - C_X)} \right) dC_X = \int_0^t k_f (C_{B, \text{initial}} - C_{A, \text{initial}}) dt$$

$$\ln \left(\frac{(C_{B, \text{initial}} - C_X)}{(C_{A, \text{initial}} - C_X)} \right) = k_f (C_{B, \text{initial}} - C_{A, \text{initial}}) t + \text{const} \quad \text{--- (1)}$$

Initial Condition: At $t = 0$, $C_X = 0$

$$\text{const} = \ln \left(\frac{C_{B, \text{initial}}}{C_{A, \text{initial}}} \right)$$

Second order combustion reactions!

$$\text{OH} + \text{H}_2 \rightarrow \text{H}_2\text{O} + \text{H}$$

$$\text{CO} + \text{O}_3 \rightarrow \text{CO}_2 + 2\text{O}$$

$$\text{O} + \text{H}_2 \rightarrow \text{OH} + \text{H}$$

$$\text{H} + \text{O}_2 \rightarrow \text{OH} + \text{O}$$

$$\text{OH} + \text{CH}_4 \rightarrow \text{H}_2\text{O} + \text{CH}_3$$

$$k_f = \frac{1}{(C_{A, \text{initial}} - C_{B, \text{initial}}) t} \ln \left(\frac{C_{B, \text{initial}} (C_{A, \text{initial}} - C_X)}{C_{A, \text{initial}} (C_{B, \text{initial}} - C_X)} \right)$$

Now, what we will do? We will basically, multiply that thing with the both the sides, C_B into minus C_A 1 right. So, if you look at earlier, we had seen that, minus dC_X by dt is equal to $k_f C_A$ in minus, C_X into C_B in minus C_X right minus dC_X divided by $C_{A, \text{initial}}$

minus C_X into C_B in minus C_X is equal to $k_f dt$ and then in here, I will multiply it by C_B in minus C_A in and in this side also I will multiply it as C_B in minus C_A in right.

For both the side; left hand, right hand side, I am multiplying that is nothing, but this one now, this case I can write down as, as what can I write down here? I can write down as 1 by C_A in minus C_X minus 1 by C_B in minus C_X right of course, there will be minus sign here dC_X is equal to $k_f C_B$ in minus C_A in into dt , right. Yes or no.

So, then I will integrate it, if I will integrate this thing, I will get this integrating, for thing and this is basically 0 to t I can write down right. So, initial condition, if you look at at t is equal to 0 what will be C_X ? C_X will be 0 is not it, because there is no change in the concentration right of that. So, right at t is equal to 0 C_X will be 0 and then if it is 0 , this thing what I, what I will be getting? This will be at t is equal to 0 , this will be 0 right and, this will be 0 , this will be 0 right.

So, I can get basically, in this case what I will get, I will get $\ln$ right, constant is equal to $\ln C_B$ in by C_A in right is not it that I will get, because this constant, this is 0 . This is 0 , that is nothing, but $\ln B$. So, if I substitute over this and this constant, this equation, let say this is equation 1 right, then I will get k_f as is equal to 1 over C_A in minus C_B in t right. This portion is $\ln$, this portion right into C_B in divide by C_A in.

So, this I will get a expression right and of course, these are all known C_B in I , all are known and C_X , if I know this concentration I can measure with respect to time then I can find out, you know what will be, how this, you know k_f right. So, by this you can find out, the, relationship for the k_f with respect to C and if I know this k_f , you can also find out how this C_X will be vary with respect to time right.

So, there are several you know second order, combustion reaction, which will be taking place in the elementary level, if you will look at like these are the reaction O H reacting with the hydrogen, getting into water and H atom and C O plus ozone, you getting into CO_2 and 2 O and O is reacting with hydrogen, getting into OH plus H and H is reacting with O_2 getting into O H plus O and of course, this O H is reacting with methane getting into water and CH_3 of course, some of the examples I have given here.

There might be several of them, which will be you know, there in that case. So, let us now look at the third order reactions.

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Third Order Reaction

Consider the third order, trimolecular reaction,

$$2NO + O_2 \xrightarrow{k_f} 2NO_2$$

$$\frac{dC_{NO_2}}{dt} = k_f C_{NO}^2 C_{O_2} \quad \text{--- 3rd order Reaction}$$

RR proportional to third power of concentration of participating species,

Third order combustion reactions !

$$HO + O + M \rightarrow H_2O + M$$

$$H + H + H \rightarrow H_2 + H$$

$$2NO + O_2 \rightarrow 2NO_2$$

So, let us consider the third order reaction, which is trimolecular reactions, right. 2 N O is reacting with oxygen, getting with 2 N O 2. This we are already discussed. So, if you, write down this reaction is basically 2 C NO 2 dt is equal to 2 kf right, CNO 2 and C O 2 right, because this is being formed therefore, there is no negative sign and this reaction rate, keep in mind that this is proportional to right, third power of concentration right, of the participating species. Therefore, this is the third order reaction right, because this is 2 index and this is 1.

So, basically 2 so, therefore, and third order combustion reactions, some of the examples, I have shown here that is H O, reacting with O getting in and also with a third body and became O H 2 plus M H O plus O H O 2 ok. This will be H O 2 plus M and H 3 H is reacting getting into hydrogen plus H right 2 N O reacting with O 2, getting into 2 N O 2 right.

So, these are the third order reaction, what will be, considering and in the next lecture what will be discussing? Will be basically discussing about the reverse reaction and how to handle those things, and later on will be looking at the chain reactions right. So, with this we will stop over here.

Thank you very much.